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AND
THE DISTRIBUTION OF PRESSURE
OVER
WESTERN EUROPE

BY
C. E. P. BROOKS, D.Sc.

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SUNSPOTS AND THE DISTRIBUTION OF PRESSURE OVER WESTERN EUROPE

By C. E. P. Brooks, D.Sc.

The following paper gives the results of an investigation into the relations between the position of any month, quarter or year in the eleven-year sunspot cycle and the distribution of pressure over western Europe and the eastern North Atlantic. Two aspects of the question were considered :—

- (1) whether there is any relation between the position of a month in the sunspot cycle and the type of pressure distribution over the area as a whole ;
- (2) whether there is any relation between the position of a quarter or year in the sunspot cycle and the actual pressure at certain individual stations.

1. The sequence of pressure types during the sunspot cycle.—

The first inquiry is concerned not so much with the actual numerical values of the pressures as with the positions of the areas with highest and lowest pressure relative to normal, i.e. the " type " of pressure distribution. For this purpose the classified list of monthly charts of pressure anomaly* was employed, the classification being extended to include 1921. The position of years in the sunspot cycle was based on the scheme given in Table I ; actually only the 40 years, 1873 to 1900 and 1910 to 1921, were employed in this instance, but the full table is given here as it will be required for reference later.

The frequencies of different pressure types are shown in Table II. For full descriptions of the types reference must be made to the original work, but the following summary gives the salient points : Group I (IA, IB, etc.) includes all charts with pressure above normal at Thorshavn, in the Faroe Islands, Group II all those with pressure below normal at Thorshavn. The centres of maximum deviation, positive in Group I, negative in Group II, are :—A, Scandinavia ; B, Western Europe ; C, British Isles ; D, Iceland ; E, Arctic. The figures given in italics are the expectations on the assumption that the numbers of each type are distributed at random through the sunspot cycle. It will be seen that the numbers actually found agree closely enough with this random distribution, and do not suggest any systematic variation of pressure type through the sunspot cycle. The only cases which may possibly be exceptions are ID and IID ; one to three years after spot minimum the frequency of ID exceeds expectation by 4, or 33 per cent, that of IID falls short of expectation by 4, or 31 per cent, while two to four years after spot

* London, Meteorological Office, *Geophysical Memoirs*, No. 31. Classification of Monthly Charts of Pressure Anomaly, 1926.

maximum this distribution is reversed, ID falling short of expectation by 22 per cent and IID exceeding expectation by 52 per cent.

TABLE I.—POSITION OF YEARS IN THE SUNSPOT CYCLE.

| Minimum. | | | | Rising. | | Maximum. | | | Falling. | | | |
|----------|------|-------------|-------------|---------|------|-------------|-------------|------|----------|------|------|------|
| 1876 | 1843 | <i>1844</i> | | 1845 | 1846 | 1847 | 1848 | 1849 | 1850 | 1851 | 1852 | 1853 |
| | 1854 | 1855 | <i>1856</i> | 1857 | 1858 | 1859 | 1860 | 1861 | 1862 | 1863 | 1864 | |
| | 1865 | 1866 | <i>1867</i> | 1868 | 1869 | 1870 | 1871 | 1872 | 1873 | 1874 | 1875 | |
| | 1877 | <i>1878</i> | 1879 | 1880 | 1881 | 1882 | 1883 | 1884 | 1885 | 1886 | 1887 | |
| | 1888 | <i>1889</i> | 1890 | 1891 | 1892 | 1893 | 1894 | 1895 | 1896 | 1897 | 1898 | |
| 1899 | 1900 | <i>1901</i> | 1902 | 1903 | 1904 | 1905 | 1906 | 1907 | 1908 | 1909 | | 1910 |
| 1911 | 1912 | <i>1913</i> | 1914 | 1915 | 1916 | 1917 | 1918 | | 1919 | 1920 | | 1921 |
| | 1922 | <i>1923</i> | 1924 | 1925 | 1926 | | | | | | | |
| | | | | | | | | | | | | |

Years of spot min., italics ; years of spot max., heavy type.

TABLE II.—FREQUENCIES (F) OF VARIOUS TYPES OF PRESSURE DISTRIBUTION, COMPARED WITH EXPECTATION (E).

| | | IA | IB | IC | ID | IE | IIA | IIB | IIC | IID | IIIE |
|--------------------|---|-----------|-----------|-----------|-----------|----------|-----------|-----------|-----------|-----------|----------|
| Spot min. 13 years | F | 12 | 15 | 19 | 24 | 4 | 18 | 16 | 15 | 26 | 7 |
| | E | <i>14</i> | <i>10</i> | <i>21</i> | <i>25</i> | <i>5</i> | <i>17</i> | <i>10</i> | <i>16</i> | <i>28</i> | <i>8</i> |
| Rising 6 years . . | F | 9 | 3 | 7 | 16 | 3 | 6 | 7 | 7 | 9 | 5 |
| | E | 7 | <i>5</i> | <i>10</i> | <i>12</i> | <i>3</i> | <i>8</i> | <i>5</i> | <i>7</i> | <i>13</i> | <i>4</i> |
| Spot max. 7 years | F | 8 | 3 | 7 | 17 | 5 | 11 | 1 | 8 | 18 | 6 |
| | E | 8 | <i>5</i> | <i>11</i> | <i>14</i> | <i>3</i> | <i>9</i> | <i>6</i> | <i>9</i> | <i>15</i> | <i>5</i> |
| Falling 14 years | F | 15 | 9 | 32 | 21 | 5 | 18 | 8 | 20 | 32 | 8 |
| | E | <i>15</i> | <i>11</i> | <i>23</i> | <i>27</i> | <i>6</i> | <i>19</i> | <i>11</i> | <i>17</i> | <i>21</i> | <i>9</i> |

This means that when sunspots are increasing in number pressure tends to be high over Iceland, while when sunspots are decreasing pressure tends to be low over Iceland. The odds against the distribution in Table II arising by chance are, however, only seven to one, so that this result is of little significance. A second count was made weighting the different months according to the numerical value of the maximum pressure deviation, but this gave no additional information.

2. Deviations of Pressure from Normal during the Sunspot cycle.—The second aspect of the problem was investigated by tabulating the actual deviations of pressure from normal over as long a period as possible.

Results for four stations are given in Table III, the periods employed being:—Stykkisholm 1846–1926, Berlin 1848–1923, Valentia 1866–1926, Ponta Delgada 1865–1926.

TABLE III.—DEVIATIONS OF PRESSURE FROM NORMAL IN DIFFERENT PARTS OF THE SUNSPOT CYCLE,
AND CORRESPONDING STANDARD ERRORS (S.E.).

| | Number of Years | Jan.—March | | April—June | | July—Sept. | | Oct.—Dec. | | Year | |
|------------------------|-----------------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| | | Dev. mb. | S.E. mb. |
| <i>Stykkisholm</i> — | | | | | | | | | | | |
| Spot minimum .. | 24 | +1.92 | 1.18 | -0.31 | 0.55 | +0.12 | 0.53 | -0.16 | 1.02 | +0.39 | 0.46 |
| Rising .. | 14 | -0.54 | 1.73 | +0.45 | 1.01 | +0.15 | 0.53 | +0.08 | 1.28 | +0.03 | 0.65 |
| Spot maximum .. | 19 | -1.57 | 1.16 | -0.85 | 0.58 | +0.05 | 0.50 | +0.11 | 0.97 | -0.14 | 0.46 |
| Falling .. | 23 | -0.39 | 1.12 | -0.65 | 0.52 | -0.21 | 0.46 | +0.04 | 0.82 | -0.30 | 0.44 |
| <i>Valentia</i> — | | | | | | | | | | | |
| Spot minimum .. | 20 | -1.08 | 0.70 | -1.17 | 0.37 | -0.38 | 0.34 | +0.59 | 0.65 | -0.51 | 0.34 |
| Rising .. | 12 | -0.40 | 1.10 | +0.13 | 0.46 | +0.08 | 0.46 | -1.84 | 1.09 | -0.51 | 0.37 |
| Spot maximum .. | 13 | +1.06 | 1.36 | +0.43 | 0.26 | -0.23 | 0.19 | +0.58 | 1.36 | +0.46 | 0.56 |
| Falling .. | 16 | +0.77 | 1.03 | +1.00 | 0.73 | +0.61 | 0.48 | +0.19 | 0.60 | +0.64 | 0.44 |
| <i>Berlin</i> — | | | | | | | | | | | |
| Spot minimum .. | 23 | -1.39 | 0.52 | -0.35 | 0.36 | -0.13 | 0.33 | -0.22 | 0.58 | -0.52 | 0.19 |
| Rising .. | 12 | 0.00 | 1.23 | +0.17 | 0.50 | -0.04 | 0.31 | -0.04 | 1.10 | +0.02 | 0.39 |
| Spot maximum .. | 18 | +0.95 | 0.67 | +0.05 | 0.43 | -0.29 | 0.36 | -0.23 | 0.48 | +0.12 | 0.25 |
| Falling .. | 23 | +0.63 | 0.65 | +0.18 | 0.31 | +0.37 | 0.22 | +0.43 | 0.67 | +0.40 | 0.28 |
| <i>Ponta Delgada</i> — | | | | | | | | | | | |
| Spot minimum .. | 21 | -0.67 | 0.75 | +0.27 | 0.50 | +0.19 | 0.30 | +0.01 | 0.74 | -0.05 | 0.33 |
| Rising .. | 12 | -0.07 | 1.29 | -0.15 | 0.48 | -0.42 | 0.34 | -0.80 | 0.77 | -0.36 | 0.41 |
| Spot maximum .. | 13 | +0.22 | 1.02 | -0.24 | 0.48 | +0.15 | 0.27 | +1.76 | 0.51 | +0.47 | 0.32 |
| Falling .. | 16 | +0.74 | 0.88 | -0.02 | 0.35 | -0.06 | 0.28 | -0.84 | 0.53 | -0.05 | 0.37 |

A preliminary test showed that little information was to be expected from the use of monthly values, but it seemed possible that a longer interval might give significant results. The work was accordingly repeated using quarterly and annual means. The results are shown in Table III, where against each mean value of pressure is shown the standard error (S.E.) of the figures composing it ; this S.E. is obtained from the expression $\sqrt{\frac{\sum (x-\bar{x})^2}{n-1}}$ where $x_1, x_2 \dots$ are the deviations in individual years or seasons, \bar{x} the average deviation and n the number of observations. Thus, for Stykkisholm, spot minimum, January to March, $\bar{x} = +1.92$ mb. and n is 24.

Considering first the sixteen annual means, if there were no relation between pressure and position in the sunspot cycle, we should expect on the theory of probability that the deviations would exceed 0.67 times their standard error on eight occasions, 1.15 times their S.E. on four occasions, and so on. The relations between expectation and observation are as follows :—

TABLE IV.—RELATION OF MEAN ANNUAL PRESSURES AT DIFFERENT PARTS OF THE SUNSPOT CYCLE TO THEIR STANDARD ERRORS

| | | | | | | | |
|----------------------------|-----|------|------|------|---------------|---------------|--|
| Ratio of Deviation to S.E. | | | | | | | |
| greater than | .67 | 1.15 | 1.53 | 1.86 | 2.15 | 2.56 | |
| Frequency expected .. | 8 | 4 | 2 | 1 | $\frac{1}{2}$ | $\frac{1}{4}$ | |
| Frequency observed .. | 10 | 6 | 1 | 1 | 1 | 1 | |

It is evident that the ratios of the deviations to their standard errors are not systematically greater than would be expected by chance. There is one outstanding ratio of 2.74 at spot minimum at Berlin, and the odds against chance figures giving a ratio of this amount once in 16 tries are about nine to one, but considering the general run of the figures the results must be held to be without significance.

Considering next the 64 quarterly values, the comparison between expectation and observation is made in Table V.

TABLE V.—RELATION OF MEAN QUARTERLY PRESSURES AT DIFFERENT PARTS OF THE SUNSPOT CYCLE TO THEIR STANDARD ERRORS.

| | | | | | | | |
|----------------------------|-----|------|------|------|------|------|--|
| Ratio of deviation to S.E. | | | | | | | |
| greater than | .67 | 1.15 | 1.53 | 1.86 | 2.15 | 2.56 | |
| Frequency expected .. | 32 | 16 | 8 | 4 | 2 | 1 | |
| Frequency observed .. | 27 | 16 | 9 | 3 | 3 | 3 | |

The three highest ratios are 3·45 at spot maximum, October to December, at Ponta Delgada ; 3·17 at spot minimum, April to June, at Valentia ; and 2·67 at spot minimum, January to March, at Berlin. The odds against a ratio of 3·45 occurring once in 64 tries are about 30 to 1, but considering the general run of the figures, the results, like those for the annual means, are probably without significance. It appears, therefore, that at present the variations of sunspots in the eleven-year cycle cannot be taken into account in predicting quarterly mean deviations of pressure in the eastern North Atlantic or western Europe.