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SEASONAL CHANGE  
OF SURFACE TEMPERATURE OF  
THE NORTH ATLANTIC OCEAN

BY

T. H. KIRK, B.Sc.

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# SEASONAL CHANGE OF SURFACE TEMPERATURE OF THE NORTH ATLANTIC OCEAN

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## SUMMARY

The facts of the seasonal change of surface temperature of the North Atlantic Ocean are presented by means of charts showing the distribution of harmonic parameters. This method makes it possible to write down by inspection an analytic expression for the process of seasonal change at any position within the area of the charts. The influence of the various factors underlying seasonal change is also briefly discussed. A new series of charts is then derived to show the distribution of the rate of change of mean sea-surface temperature for each month of the year.

## § 1—INTRODUCTION

The seasonal change of sea-surface temperature is of importance not only to oceanographers and meteorologists for its significance in the major problem of the heat exchange between ocean and atmosphere, but also to marine biologists for its effect on the growth and travel of the different forms of marine life. Whoever is interested in the effects of variations of sea-surface temperature requires a knowledge of the seasonal fluctuation, for it would appear unlikely that in temperate latitudes any other fluctuations could exceed in magnitude the seasonal one. A study of the seasonal change of sea-surface temperature should logically, therefore, precede any attempt to apply the method of anomalies of sea-surface temperature to any problem.

Climatic atlases are available depicting the mean distribution of sea-surface temperature for each month of the year, each chart being based on observations taken over a long period of years. Seasonal change can be assessed qualitatively from these charts by noting visually the changes that occur from month to month. For a detailed quantitative analysis, however, it is preferable to use the original observations. This paper summarizes a mass of sea-surface temperature data for the North Atlantic Ocean, and presents the facts of seasonal change in forms suitable for both theoretical investigation and practical use.

## § 2—SOURCES OF DATA

Tabulated values of sea-surface temperature, available for the periods 1887–99 and 1921–38, have been used. These data, based on British ships' logs, had already been used in the preparation of the sea-temperature charts in "Monthly meteorological charts of the Atlantic Ocean"<sup>1\*</sup>, and, recently, in the preparation of more detailed charts of sea temperature for the North Atlantic<sup>2</sup>. Monthly mean values for 2° squares were, therefore, already available. In this later publication<sup>2</sup> some account was given of the limitations attached to the use of sea-temperature data.

The data were found to be relatively scanty in the coastal waters of the British Isles and in the North Sea. In these areas German data have been preferred. The mean values used, for 1°

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\* The index numbers refer to the Bibliography on p. 19.

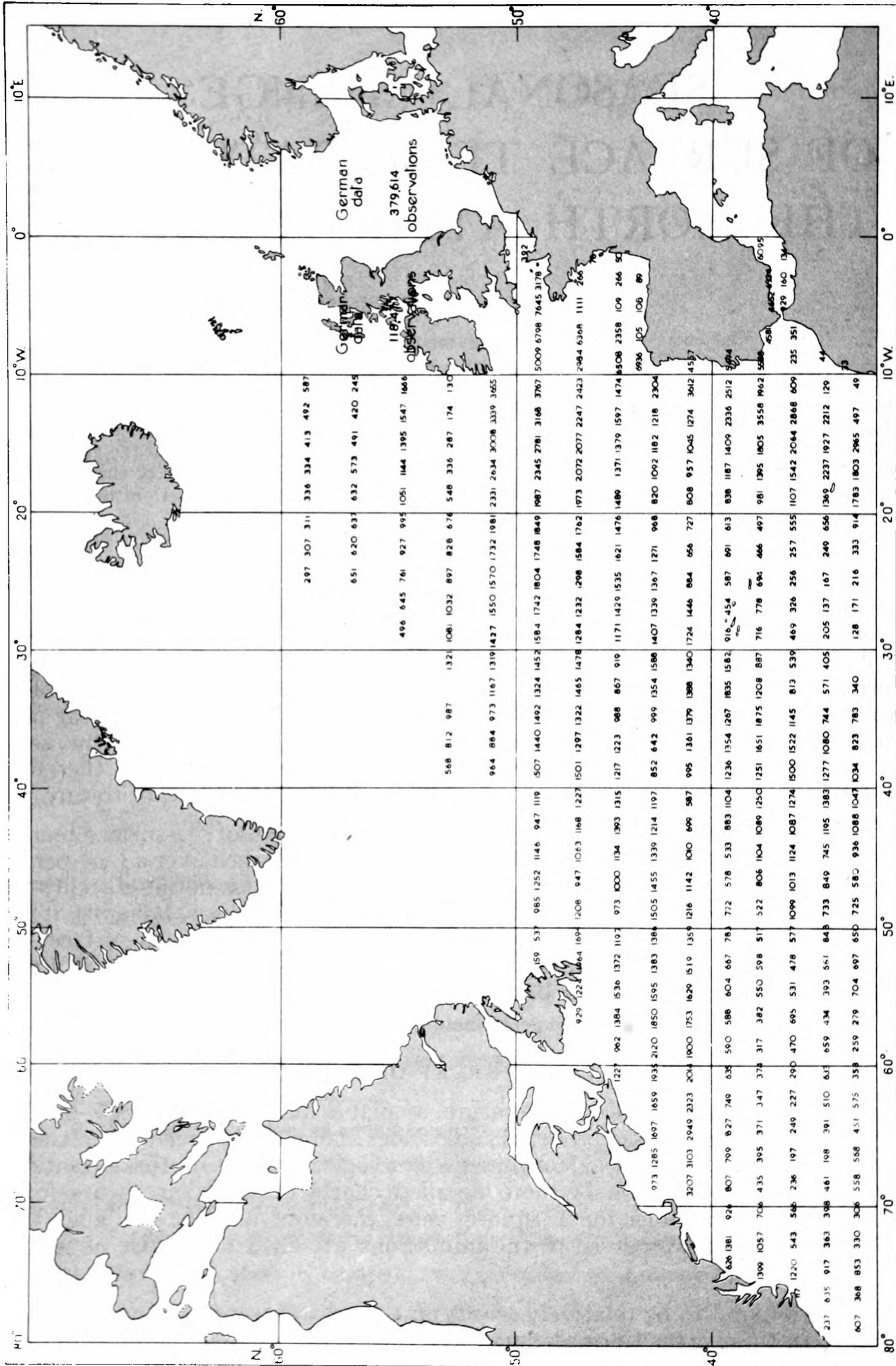


FIG. 1-DISTRIBUTION OF NUMBER OF OBSERVATIONS

squares, are based on observations made during the period 1862–1946, and hence are not directly comparable with the British data. There appears no reason to suppose, however, that the mean process of seasonal change can be significantly different.

The distribution of the number of observations used is shown in Fig. 1. Unfortunately, scarcity of observations has not permitted the investigation to be extended to northern waters. The analysis has also not been made for certain squares where the data were few in number or badly distributed throughout the year.

### § 3—ANALYSIS OF DATA

Monthly means for individual squares have been plotted. The smooth curve drawn through the values for the different months represents the course of seasonal change. By plotting data from different squares it is apparent that important differences exist between the characteristic curves. These differences are of :—

- (i) Amplitude ; maximum departure from the yearly mean value varies appreciably.
- (ii) Phase ; slight variations occur in the times of maxima and minima.
- (iii) Shape ; curves show different degrees of asymmetry.

Harmonic analysis has been used to derive parameters which facilitate the examination of variations from square to square. Representing the sea-surface temperature by  $T$ , expressed in degrees Fahrenheit in this paper, the normal expansion in a Fourier series can be written

$$T = a_0 + a_1 \sin(t + A_1) + a_2 \sin(2t + A_2) + a_3 \sin(3t + A_3) + \dots$$

where  $t$ , representing the time, takes values from  $0^\circ$  to  $360^\circ$ .

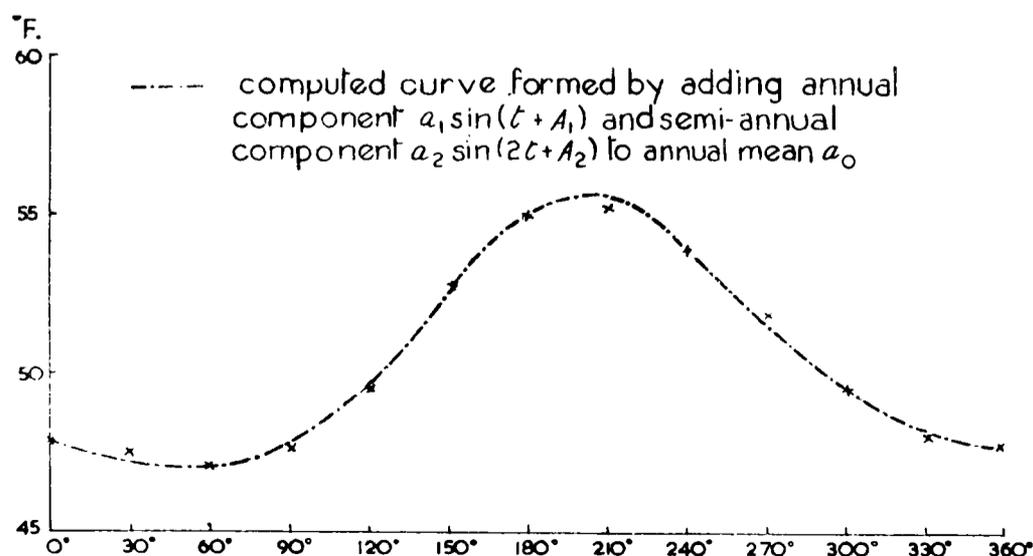
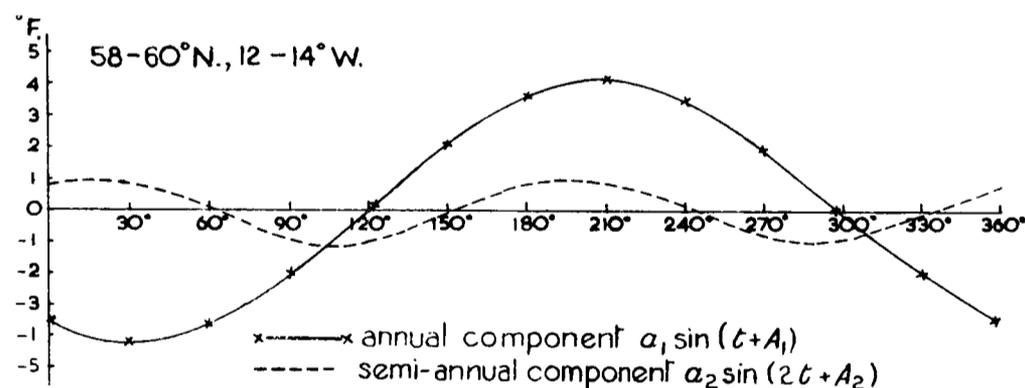


FIG. 2—FIT AFFORDED BY COMPUTED CURVE



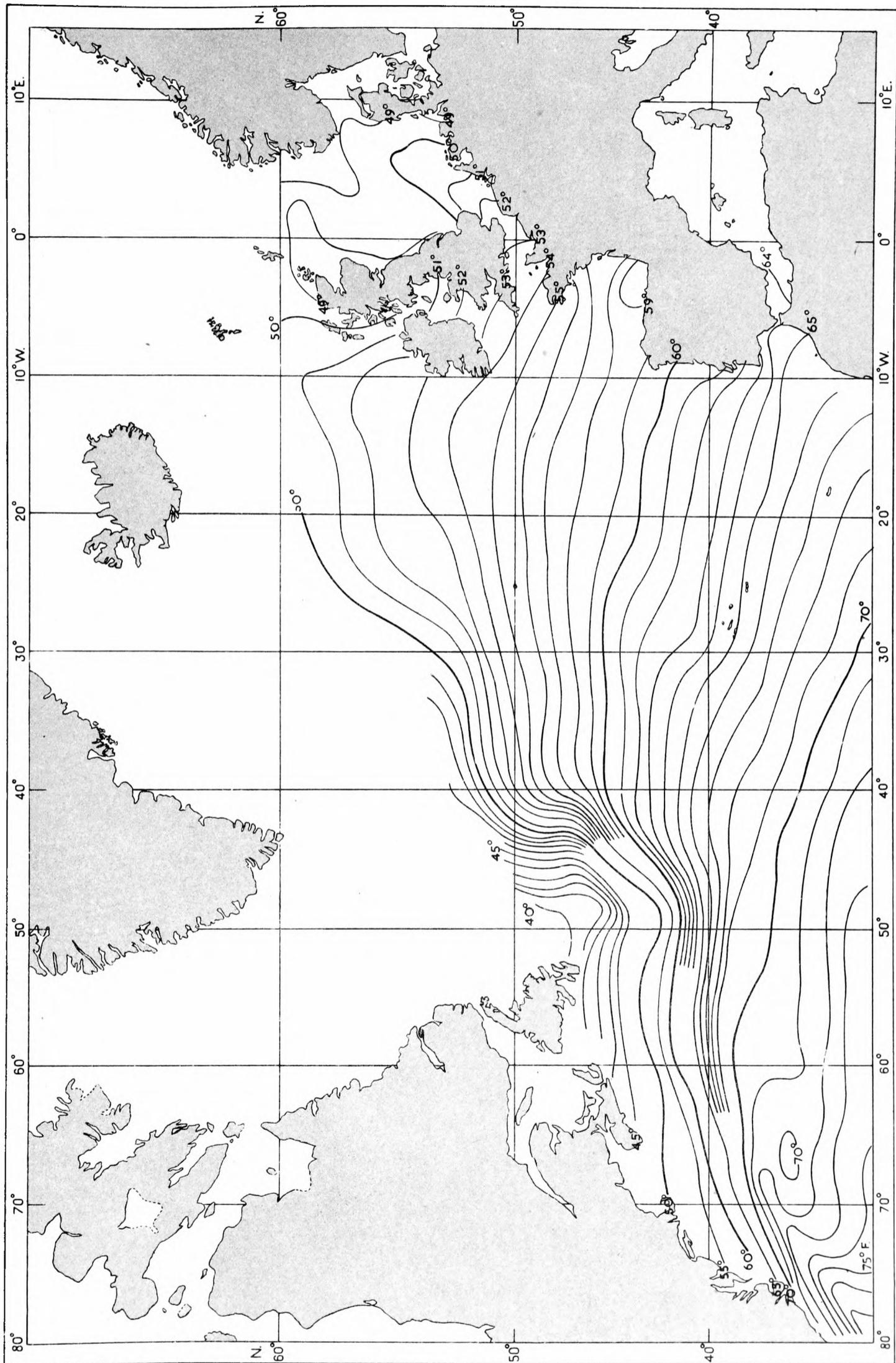


FIG. 3—DISTRIBUTION OF ANNUAL MEAN SEA-SURFACE TEMPERATURE ( $\alpha_0$ )

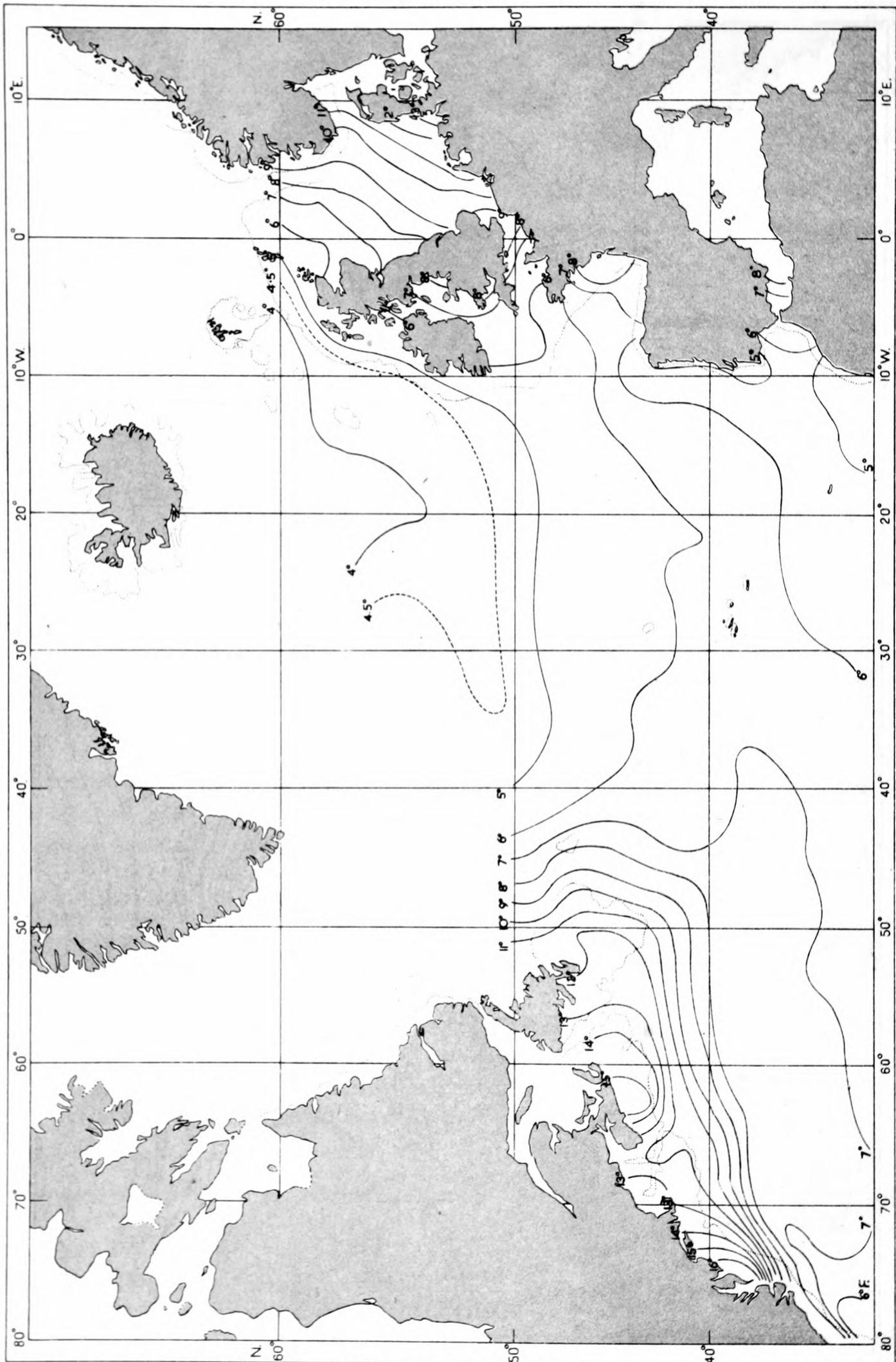


FIG. 4-DISTRIBUTION OF AMPLITUDE OF ANNUAL COMPONENT ( $a_1$ )

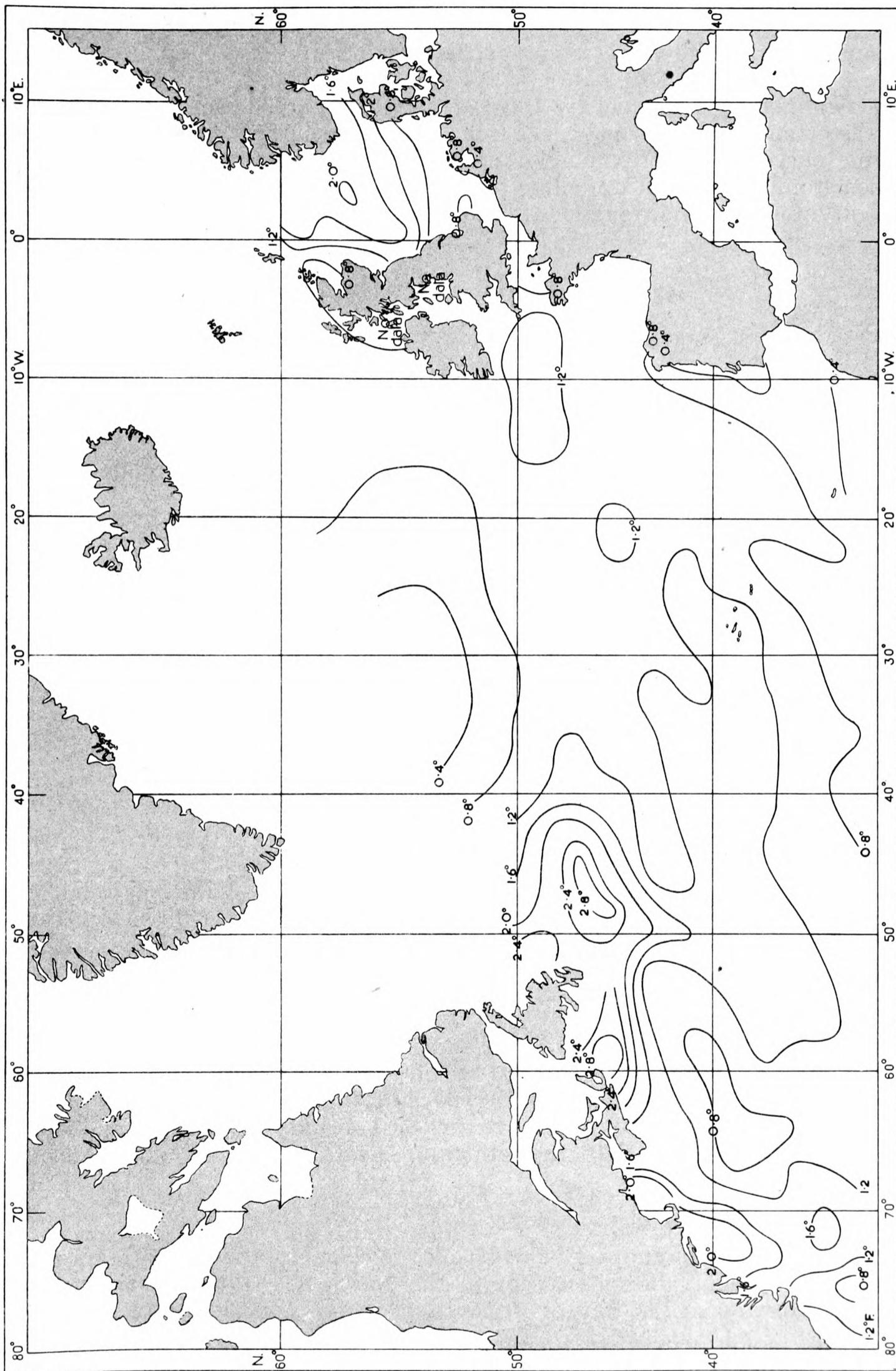


FIG.5 - DISTRIBUTION OF AMPLITUDE OF SEMI-ANNUAL COMPONENT ( $\sigma_2$ )

- (iv) Small values occur in the upwelling areas off the coasts of Portugal and Morocco.
- (v) A small area of high values occurs in the North Sea.

*Ratio of amplitudes.*—The quantity  $100a_2/a_1$  may be regarded as a measure of the degree of skewness or distortion of the seasonal curve from a pure sine curve. In areas where this quantity is small a sine curve will approximately represent the seasonal variation. Fig. 6 shows an example taken from the area of upwelling off Portugal (see p. 18). It is easily seen that the first component affords a good representation of the seasonal variation.

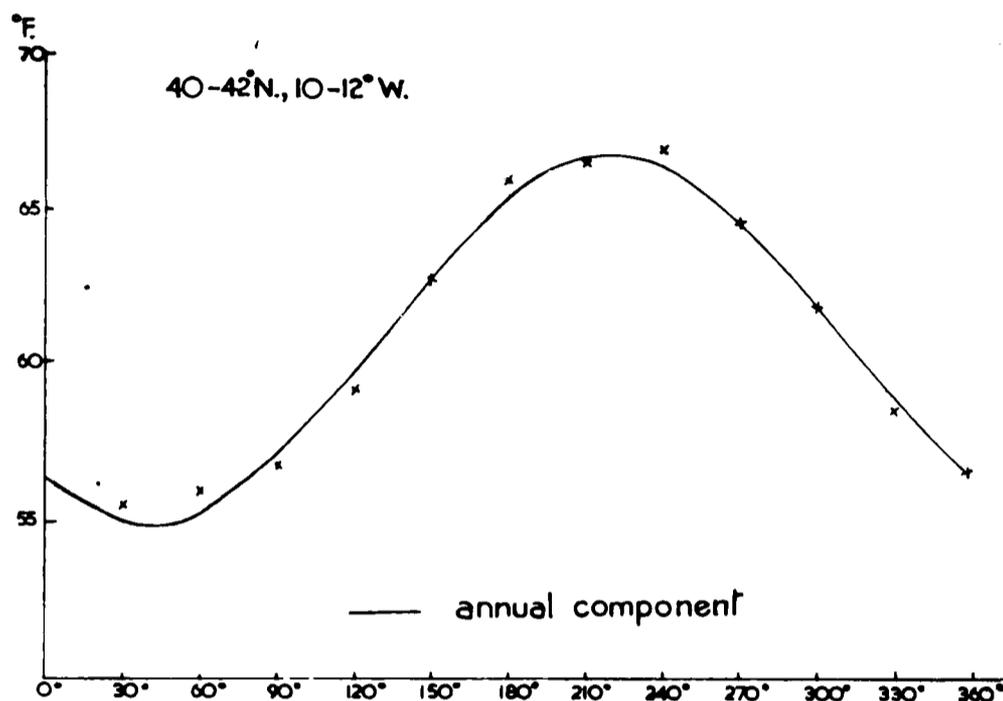


FIG. 6—GOODNESS OF FIT AFFORDED BY ANNUAL COMPONENT

Fig. 7 shows the following features :—

(i) The maximum values (over 30 per cent.) are reached in the northern part of the North Sea, north-west of Scotland and east of Newfoundland. Relatively high values also occur in a broad belt extending south-westward from the British Isles.

(ii) Low values occur in the upwelling areas off the coasts of Portugal and Morocco and south of the main belt of high values. There are also low values off the American coast, in the mid Atlantic north of  $50^{\circ}$  N., and in the southern coastal waters of the British Isles.

(iii) The greatest variability occurs in the North Sea and in the coastal waters of the British Isles.

*Phase of annual component.*—The phase angle  $A_1$  of the annual component is important inasmuch as it largely determines the time at which the sea temperature reaches maximum and minimum values. It varies for the most part between  $220^{\circ}$  and  $240^{\circ}$ . An angle of  $240^{\circ}$  indicates that the minimum value of the component occurs on February 14 and the maximum value on August 16. When the angle is  $220^{\circ}$  the minimum occurs on March 7 and the maximum on September 7.

Fig. 8 shows the following characteristics :—

(i) Centres of both high and low values flank the course of the Gulf Stream and the North Atlantic Current. High values also occur in the North Sea, along the coasts of Germany, Denmark and Norway, in the Bay of Biscay and off the north coast of Spain.

(ii) A trough of low values off the Portuguese coast appears to be associated with the course of the Portugal Current.

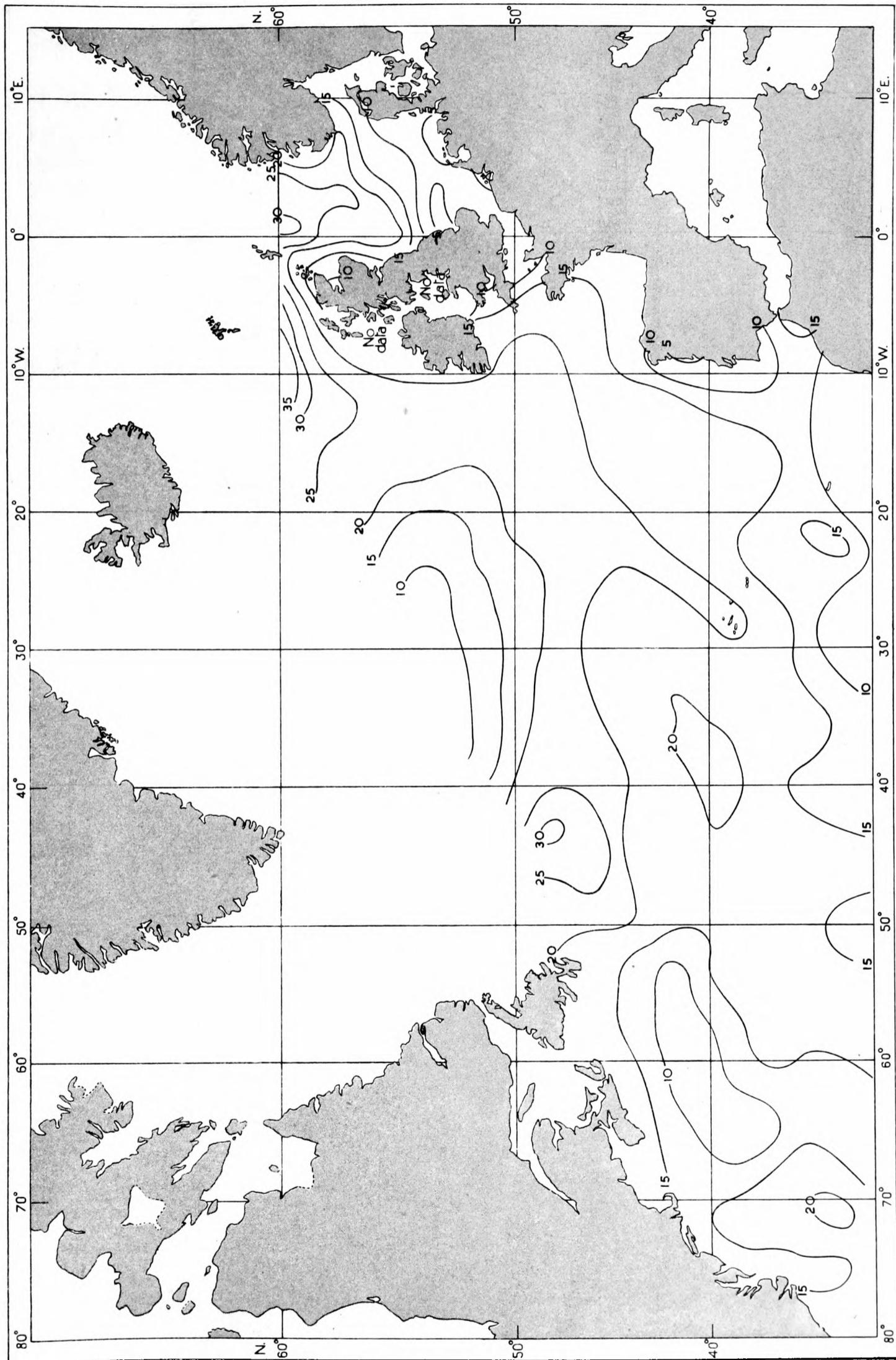


FIG. 7 — DISTRIBUTION OF  $100 a_2/a_1$

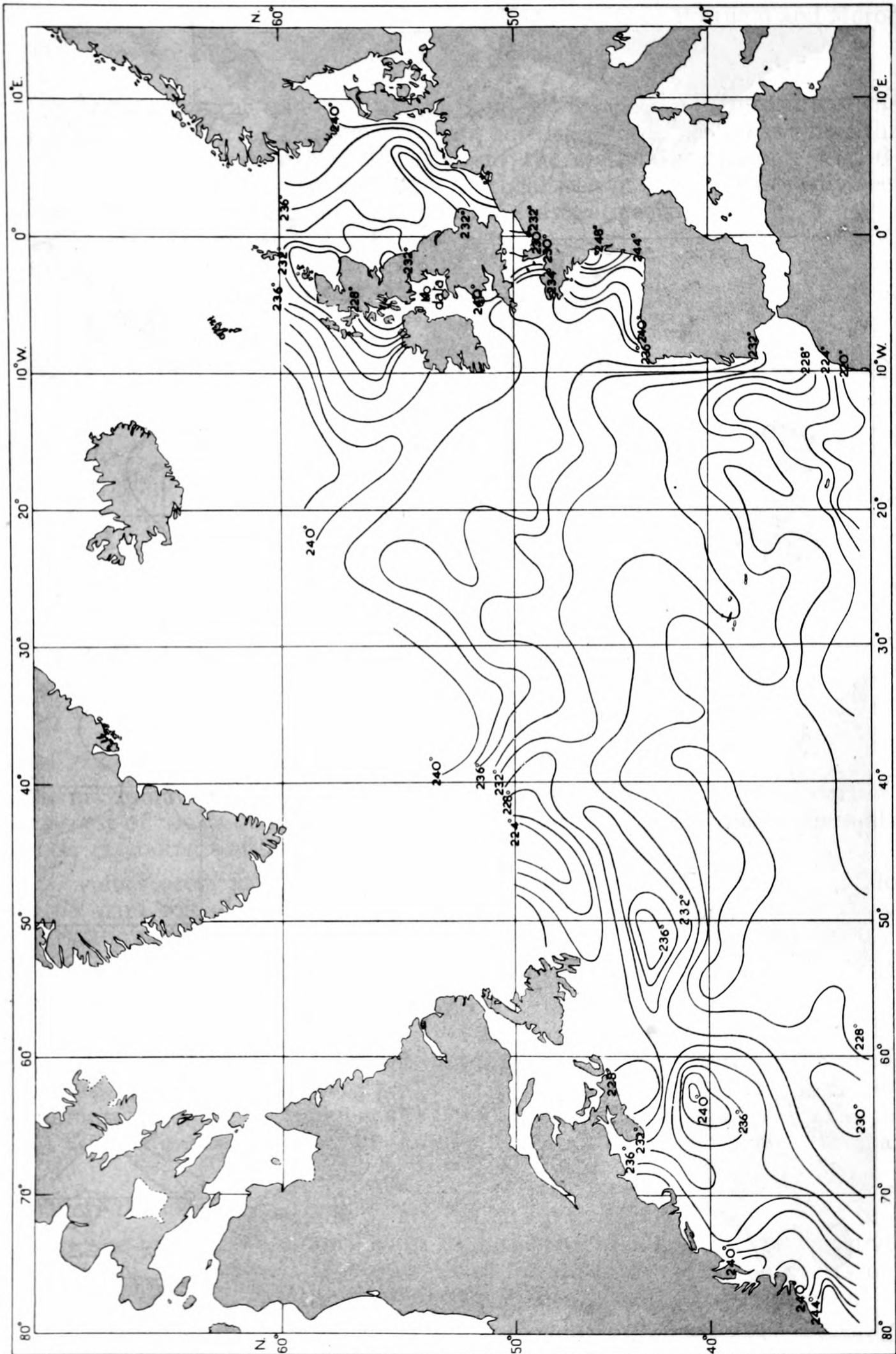


FIG.8-DISTRIBUTION OF PHASE OF ANNUAL COMPONENT (A<sub>1</sub>)

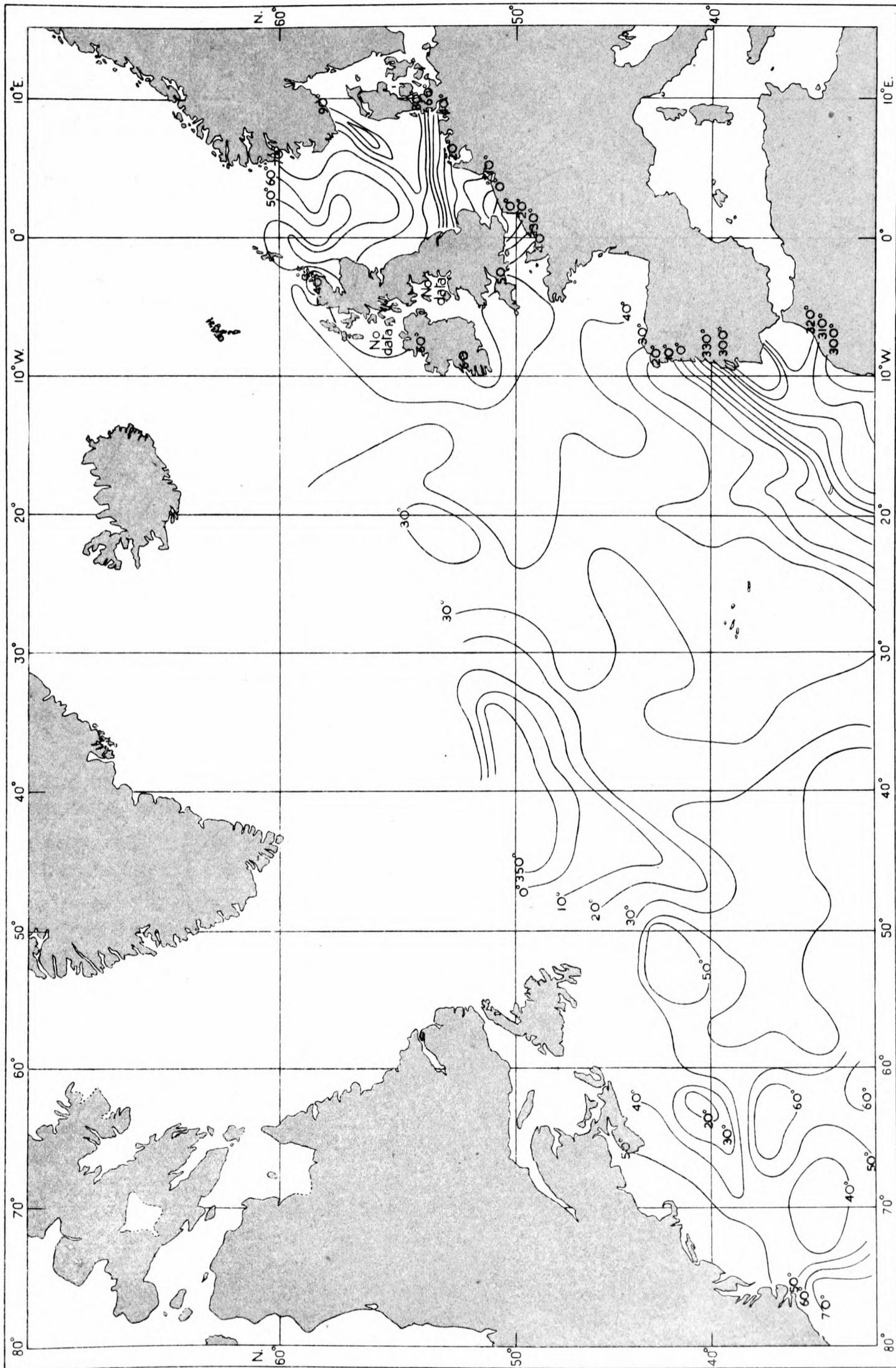


FIG. 9 - DISTRIBUTION OF PHASE OF SEMI-ANNUAL COMPONENT ( $A_2$ )

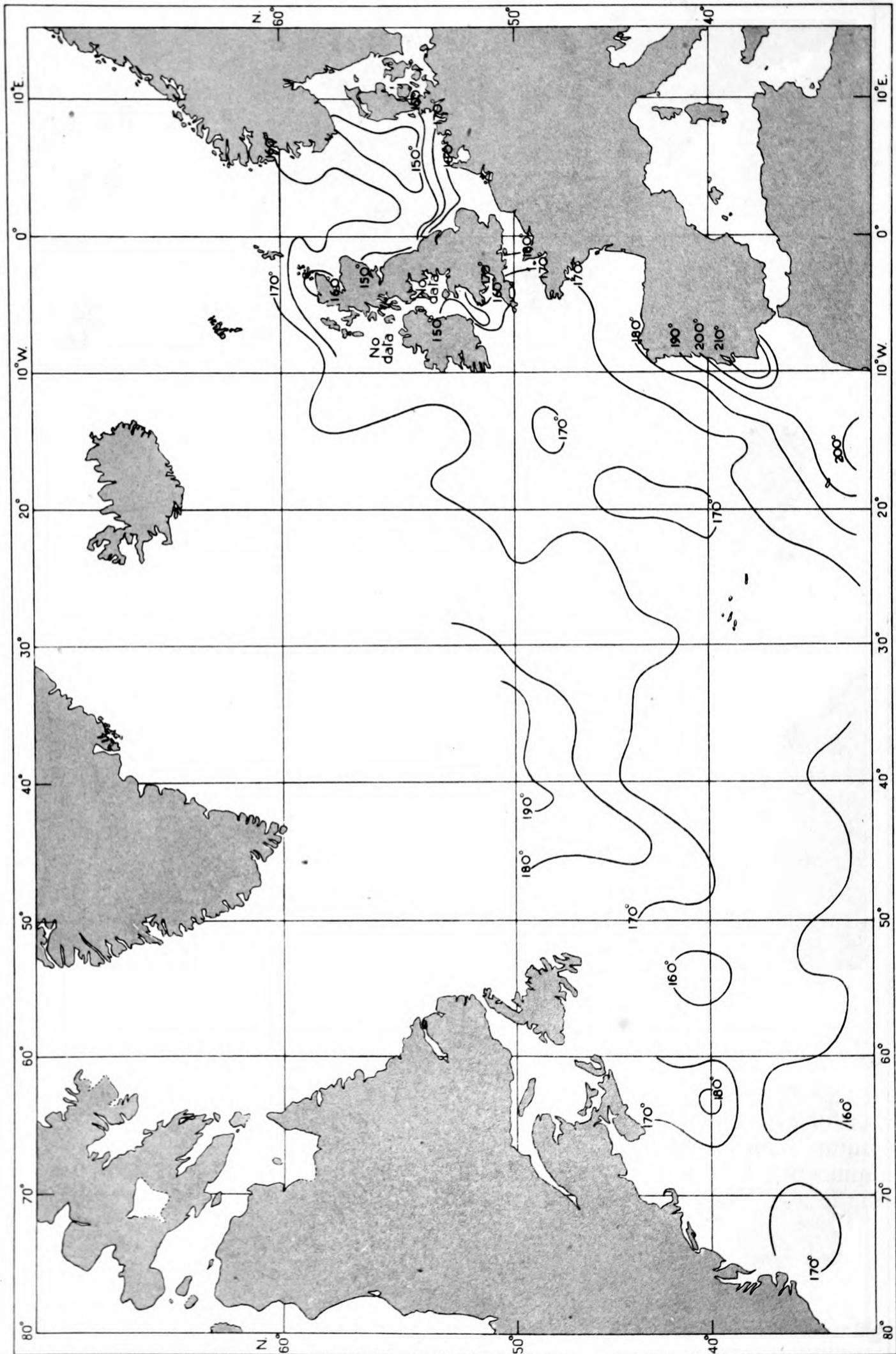


FIG.10—DISTRIBUTION OF  $F = \frac{1}{2}(2A_1 - A_2 - 90^\circ)$

(iii) There is some evidence of a ridge of high values extending south-west from the British Isles.

*Phase of semi-annual component.* The phase angle of the semi-annual component ( $A_2$ ) modifies the times of maximum and minimum values determined primarily by  $A_1$ . Fig. 9 shows the following main features :—

(i) A belt of relatively high values extends from the British Isles south-westward to the Azores and thence westward to the American continent.

(ii) Low values occur in the upwelling areas off the coasts of Portugal and Morocco and in the region centred at  $50^\circ$  N.,  $40^\circ$  W.

(iii) Both high and low values occur in the North Sea, where the distribution is complex.

If the semi-annual component is regarded as modifying the annual component then some method of representing its phase relative to that of the annual component must be found. The maximum value of the annual component is given by

$$t_1 + A_1 = 360^\circ + 90^\circ.$$

The maximum value of the second component is given by

$$2t_2 + A_2 = 360^\circ + 90^\circ.$$

Therefore,

$$t_2 - t_1 = \frac{1}{2} (2A_1 - A_2 - 90^\circ) - 180^\circ.$$

Denoting by  $F$  the quantity  $\frac{1}{2} (2A_1 - A_2 - 90^\circ)$ , then when  $F = 180^\circ$  the maxima of the two components occur at the same time. At the time of minimum value of the annual component, however, the semi-annual component is then a maximum and is thus completely out of phase.

*Function  $F$ .*—The distribution of function  $F$ , given in Fig. 10, shows :—

(i) All values are relatively close to  $180^\circ$ . This means that the semi-annual component reinforces the annual component at its maximum value and weakens the annual component at its minimum value. The physical significance of this will be dealt with later.

(ii) Values greater than  $180^\circ$  occur in the upwelling areas off the coasts of Portugal and Morocco and also in an area centred about  $50^\circ$  N.,  $40^\circ$  W.

(iii) Low values, less than  $180^\circ$ , occur in a relatively uniform belt extending from the British Isles south-westward to the Azores and thence westward to the American continent. The lowest values occur in an irregular belt extending across the southern half of the North Sea, particularly in the south-east.

At this stage the significance of a value of  $F$  differing from  $180^\circ$  may be noted. When  $F$  is less than  $180^\circ$  the time of occurrence of the maximum value of the annual variation is brought forward and the time of occurrence of the minimum value is set back or retarded. The time interval between minimum and maximum for increasing temperature is therefore less than the time interval for decreasing temperature. When  $F$  is greater than  $180^\circ$ , the time of occurrence of the maximum value of the annual variation is set back or retarded and the time of occurrence of the minimum value is brought forward. The time interval between minimum and maximum for increasing temperature is therefore greater than the time interval for decreasing temperature.

## § 5—THEORETICAL CONSIDERATIONS

In previous sections the facts of the process of seasonal change have been set out in terms of the harmonic parameters and their distribution in space. The physical factors concerned in

determining the seasonal variation of sea-surface temperature are :—

- (i) Total incoming radiation (direct and diffuse).
- (ii) Exchange of heat between ocean and atmosphere.
- (iii) Vertical transfer of heat in the ocean (convection and upwelling).
- (iv) Horizontal transport of heat by ocean currents.

*Total incoming radiation* for certain ocean areas has been given by Kimball<sup>3</sup>, taking account of the effect of variations in the amount of cloudiness and of the distribution of water vapour in the atmosphere. His data are given in Table I.

TABLE I—AVERAGE DAILY TOTAL OF SOLAR RADIATION (DIRECT + DIFFUSE) RECEIVED ON A HORIZONTAL SURFACE taken at the 21st of each month

		Jan.	Feb.	Mar.	Apr.	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.
° N.	° W.	<i>gramme calories per square centimetre</i>											
56	7	50	109	206	308	372	389	328	229	182	107	49	..
52	10	74	146	228	331	378	383	354	288	212	140	80	54
48	60	114	206	270	345	397	424	422	364	284	165	108	78
48	4	94	157	259	339	414	405	388	335	255	153	90	71
42	66-70	139	223	327	402	449	477	421	376	317	235	153	120
36	6	225	280	378	472	498	522	538	496	371	285	225	196
30	65-77	212	247	365	420	462	441	432	399	326	259	244	197
30	15	306	364	415	482	476	482	449	437	420	340	301	281

TABLE II—HARMONIC ANALYSIS OF THE DATA OF TABLE I

		$a_1'$	$A_1'$	$a_2'$	$A_2'$
° N.	° W.	gm. cal./m. <sup>2</sup>	°	gm. cal./m. <sup>2</sup>	°
52	10	166	310	11	261
48	60	172	306	18	26
48	4	175	307	7	309
42	66-70	172	301	36	316
36	6	174	304	13	21
30	65-77	130	310	15	271
30	15	98	313	11	320

Table II suggests that  $a_1'$ , the annual amplitude of the total incoming radiation, reaches a maximum in a latitude between 36° N. and 48° N. and decreases to north and south, the decrease towards the equator being particularly rapid. Table II also suggests that  $A_1'$  has only a small latitudinal variation. If this can be regarded as real, values increase to both north and south of the minimum value in latitude 42° N. However, owing to the large differences of longitude the interpretation of the data is doubtful. Values of  $a_2'$  and  $A_2'$  appear to be too scattered to permit of generalization with respect to latitude.

While sea-surface temperature cannot be regarded as determined solely by radiation income, it is nevertheless significant that the amplitude of the yearly component of the radiation income has a latitudinal maximum corresponding to the latitudinal belt of maximum values of  $a_1$  shown in Fig. 4.

Sverdrup<sup>4</sup> has stated that whereas in the southern hemisphere the latitudinal variation of the annual range of sea-surface temperature appears to be closely connected with that of the radiation income, no such correspondence is evident in the North Atlantic. This rather anomalous result he explains by the effect of the greater distribution of land in the northern hemisphere permitting the cooling of the seas by outbursts of cold continental air in winter. In reaching this conclusion, however, Sverdrup used values for different latitudes averaged over all longitudes of the oceans. It is easily appreciated from Fig. 4 how this procedure must necessarily mask the effect of the radiation income. The present results on the other hand demonstrate the influence of the radiation income outside coastal areas in the North Atlantic. Near the coasts the effects of other factors are sufficiently great to mask that of the radiation income.

*Exchange of heat between ocean and atmosphere.*—Although it has been shown that the effect of radiation income can be traced in the distribution of  $a_1$  it is at once apparent that other factors can be much more effective; for example, the high values of  $a_1$  off the American coast and in the North Sea at once suggest the influence of cold outbreaks of continental air during the winter months. Off the American coast the highest values occur because the wind is predominately from the west. The high values in the North Sea, on the other hand, must be due to the winter occurrence of easterly winds. A full discussion would necessitate examining the major problem of the heat exchange between atmosphere and ocean.

*Vertical transfer of heat in the ocean.*—Convection in the ocean is also of primary importance. When the sea cools in winter the cooling takes place at the surface; the surface layer cools, becomes denser than the water below and hence sinks, warmer water rising by convection to take its place. This warmer water becomes cooled in its turn and is again replaced. Convection, therefore, ensures that the cooling process is not confined to the surface layers but is distributed over a great depth of water. Helland-Hansen<sup>5</sup> has stated that towards the end of the winter isothermal conditions may extend to great depths. In the relatively shallow waters of the continental shelves this isothermal state may be reached relatively early in the winter and then a progressive cooling takes place. In shallow waters, therefore, the annual amplitude tends to be greater than in the open ocean where vast under-water reserves of heat are available to off-set the winter cooling. Although the winter effect is greater, it is worth noting that in summer, too, the shallow waters near the coastline tend to heat up more rapidly than the open sea. Fig. 4, showing the distribution of  $a_1$ , illustrates how the isopleths follow the contours of the continental shelf off the American coast.

There is a fundamental difference between the cooling and heating processes in the ocean. In autumn and winter, as already noted, convection helps to maintain the surface temperature by making available the under-water reserves of heat. In spring and summer, on the other hand, the surface water is warmed, but as the warmer water is less dense than the colder water below there is no tendency for convection and the ocean warms progressively from the surface. The turbulence set up by ocean waves can ensure a certain equalization of temperature near the surface, but the effect of waves becomes negligible at a relatively small depth. As the heating continues a progressively greater stratification of temperature is set up. If the effect on surface temperature of the different characteristics of the cooling and heating processes is considered, it is seen that in winter convection affects the temperature by diminishing its rate of fall and in summer the stratification also affects the temperature by increasing its rate of rise. The effect is to introduce a six-monthly oscillation into the annual variation of the temperature, and it is suggested that the six-monthly component, that has been found, can to some extent be explained in this way. This suggestion is supported by the following considerations. The phase of the second component is such that extreme values are reached very close to the maximum and minimum values of the annual component. Over the greater part of the ocean  $F$  is less than  $180^\circ$ , and, as has already been seen, the effect of the second component is to advance the

maximum value and retard the minimum value. In one of the areas where  $F$  exceeds  $180^\circ$  it is known that upwelling in spring prevents stratification and delays the time of maximum temperature. The amplitude of the six-monthly component is also small in this area.

Turning to the charts showing the distribution of  $a_2$  and  $100 a_2/a_1$ , it is easily seen that there is no definite relation between the amplitudes of the two components. This suggests that the explanation advanced above can only account for a part of the six-monthly component and that other factors are also important. It is obvious, for example, that the distribution of salinity must be taken into account in any full discussion, for density is a function of salinity as well as of temperature.

Vertical transfer can also take place by the process known as upwelling which occurs on steep coasts when the wind blows from a suitable direction. In the northern hemisphere, for example, a wind blowing with a component parallel to the coastline tends to heap up water to the right of its direction; if the wind is blowing with the land to the left of its direction the water is driven away from the coast and upwelling of water at the coastline must then necessarily occur. This process can explain the low values of  $a_1$  and  $a_2$  found off the coasts of Portugal and north-west Africa.

*Horizontal transport of heat by ocean currents.*—A perusal of the charts suggests that the horizontal transfer of heat by ocean currents is of some importance. For example, relatively low values of  $a_1$ , the annual amplitude, are associated with the Gulf Stream and the North Atlantic Current. This effect, however, may, at least in part, be explained by selective convection. The surface waters of the Gulf Stream and the North Atlantic Current have a high salinity which would favour the convection process already discussed. The seasonal change of surface temperature is further complicated by the fact that the strength and position of the ocean currents also vary seasonally.

#### § 6—RATE OF CHANGE OF SEA-SURFACE TEMPERATURE

Although the distributions of the harmonic parameters are theoretically sufficient for the discussion of the seasonal variation of sea-surface temperature their practical application is not easy. Of some practical importance would be a knowledge of the rate of change of sea temperature as a function of time and space.

The sea-surface temperature  $T$  at any place can be represented by the expression

$$a_0 + a_1 \sin (t + A_1) + a_2 \sin (2t + A_2)$$

where the harmonic parameters are known. The expression for the rate of change of sea temperature  $\partial T/\partial t$  is, therefore, by differentiation

$$a_1 \cos (t + A_1) + 2a_2 \cos (2t + A_2).$$

Values of this expression can be computed for different values of  $t$  ( $0^\circ, 30^\circ, 60^\circ, \dots, 330^\circ$ ) and the variation of  $\partial T/\partial t$  throughout the year determined. Fig. 11 shows an example, for the  $2^\circ$  square  $30\text{--}32^\circ \text{ N.}, 60\text{--}62^\circ \text{ W.}$ , of the seasonal variation of  $\partial T/\partial t$  compounded from the simple harmonic curves  $a_1 \cos (t + A_1)$  and  $2a_2 \cos (2t + A_2)$ . Notable features of this curve are the high value of  $\partial T/\partial t$  at its maximum and the difference of shape of the crest and trough.

This computation has been made for all the  $2^\circ$  and  $1^\circ$  squares under consideration, and a new series of charts constructed to show the distribution of  $\partial T/\partial t$  for each month of the year. They are given in Fig. 12. The values of  $\partial T/\partial t$ , expressed in degrees Fahrenheit per radian, may for practical purposes be converted into degrees Fahrenheit per month by multiplying by the factor one half.

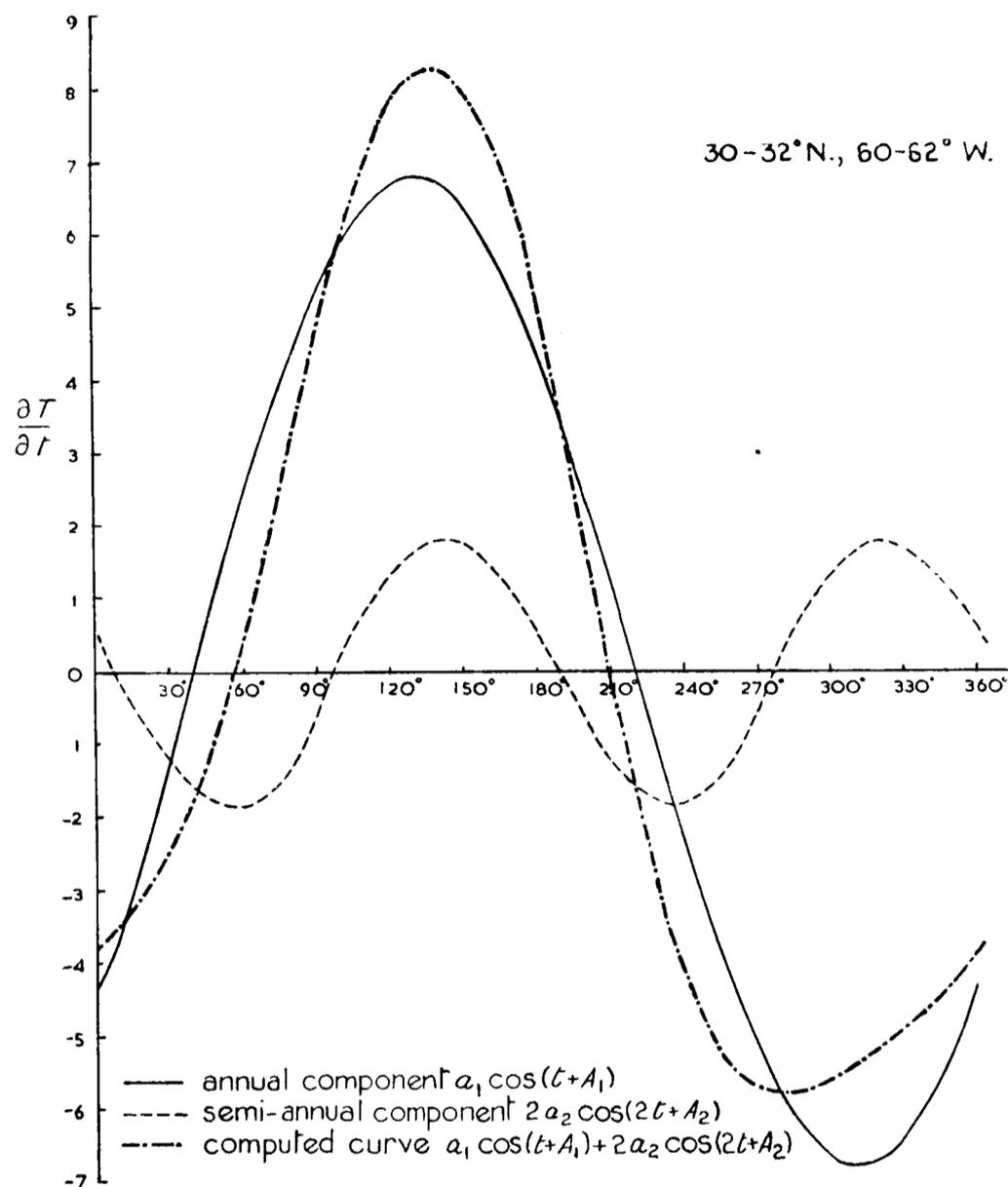


FIG. 11—SEASONAL VARIATION OF  $\partial T/\partial t$   
 Unit :—1° F. per radian where  $2\pi$  radians = 12 months

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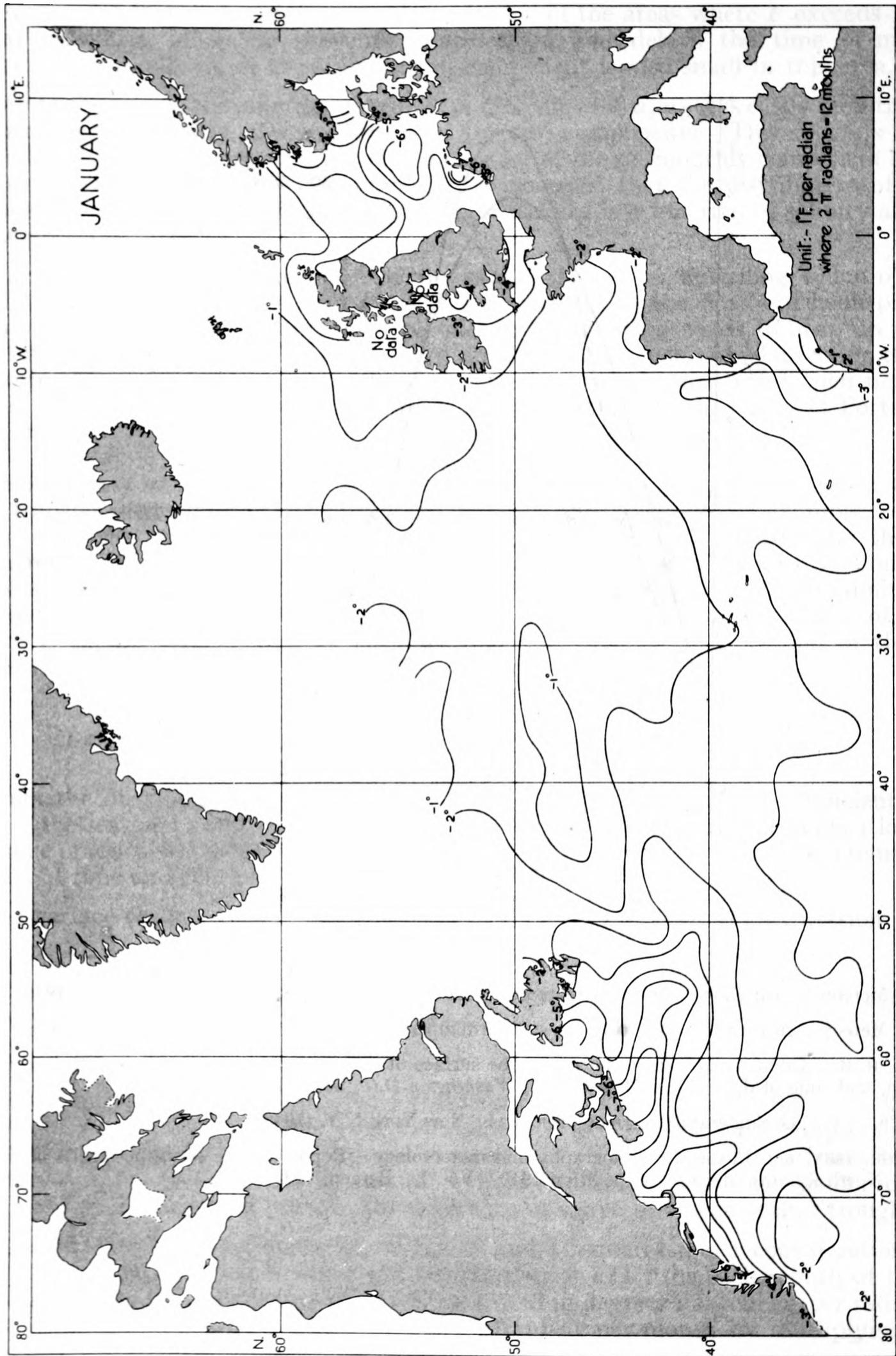


FIG.12—DISTRIBUTION OF RATE OF CHANGE OF MEAN SEA-SURFACE TEMPERATURE

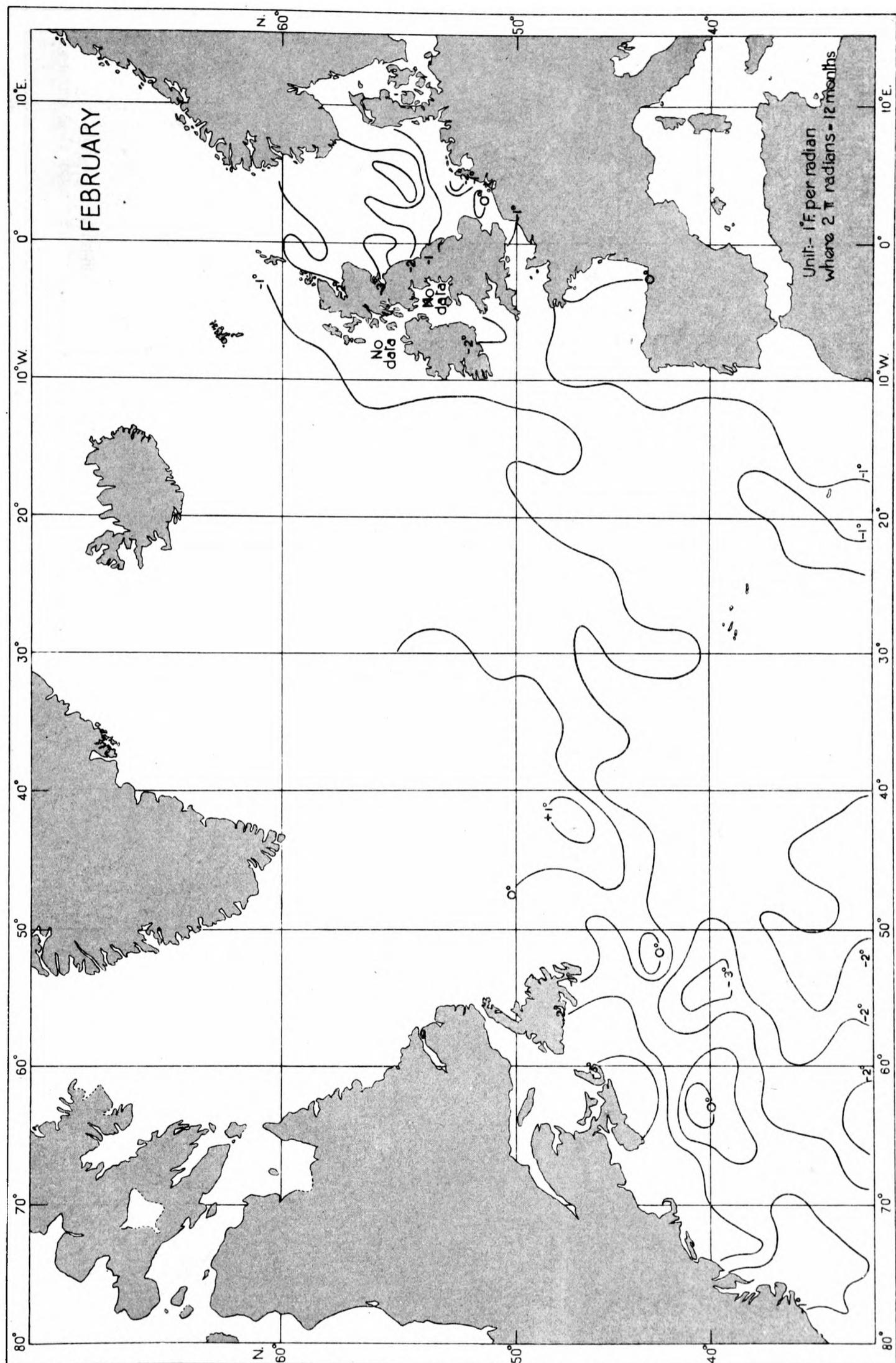


FIG. 12— continued

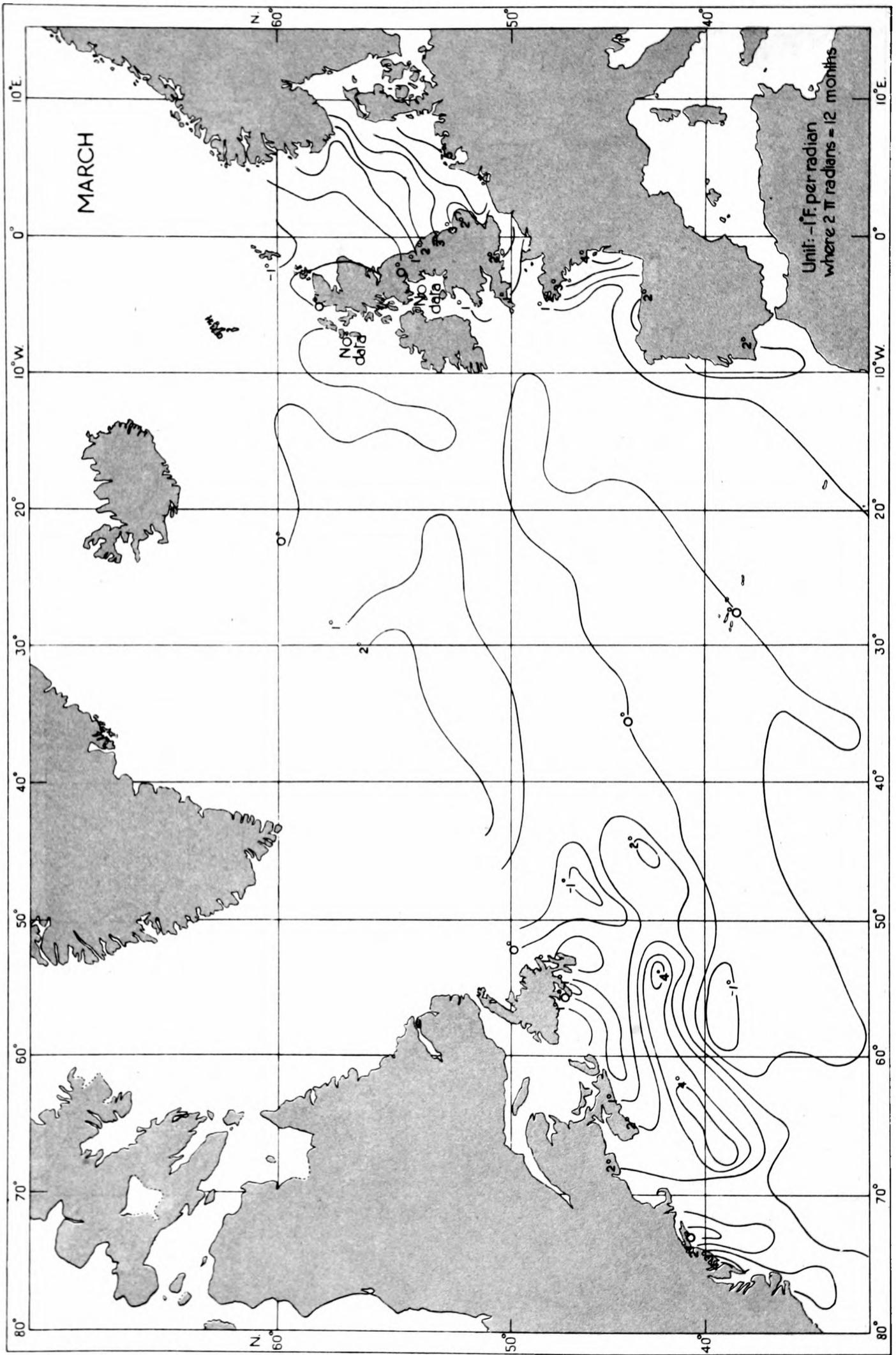


FIG.12 -- continued

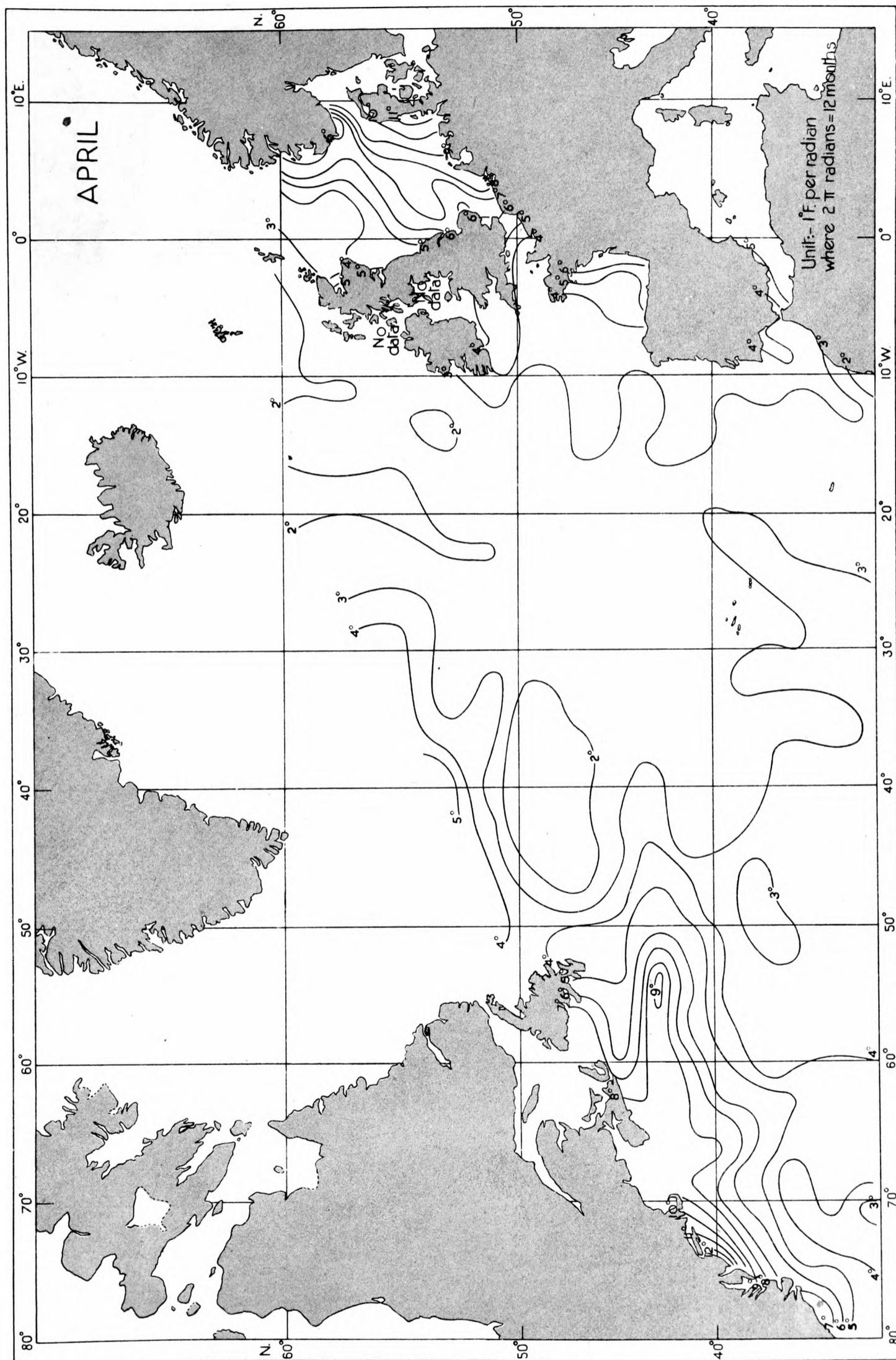


FIG. 12 — continued

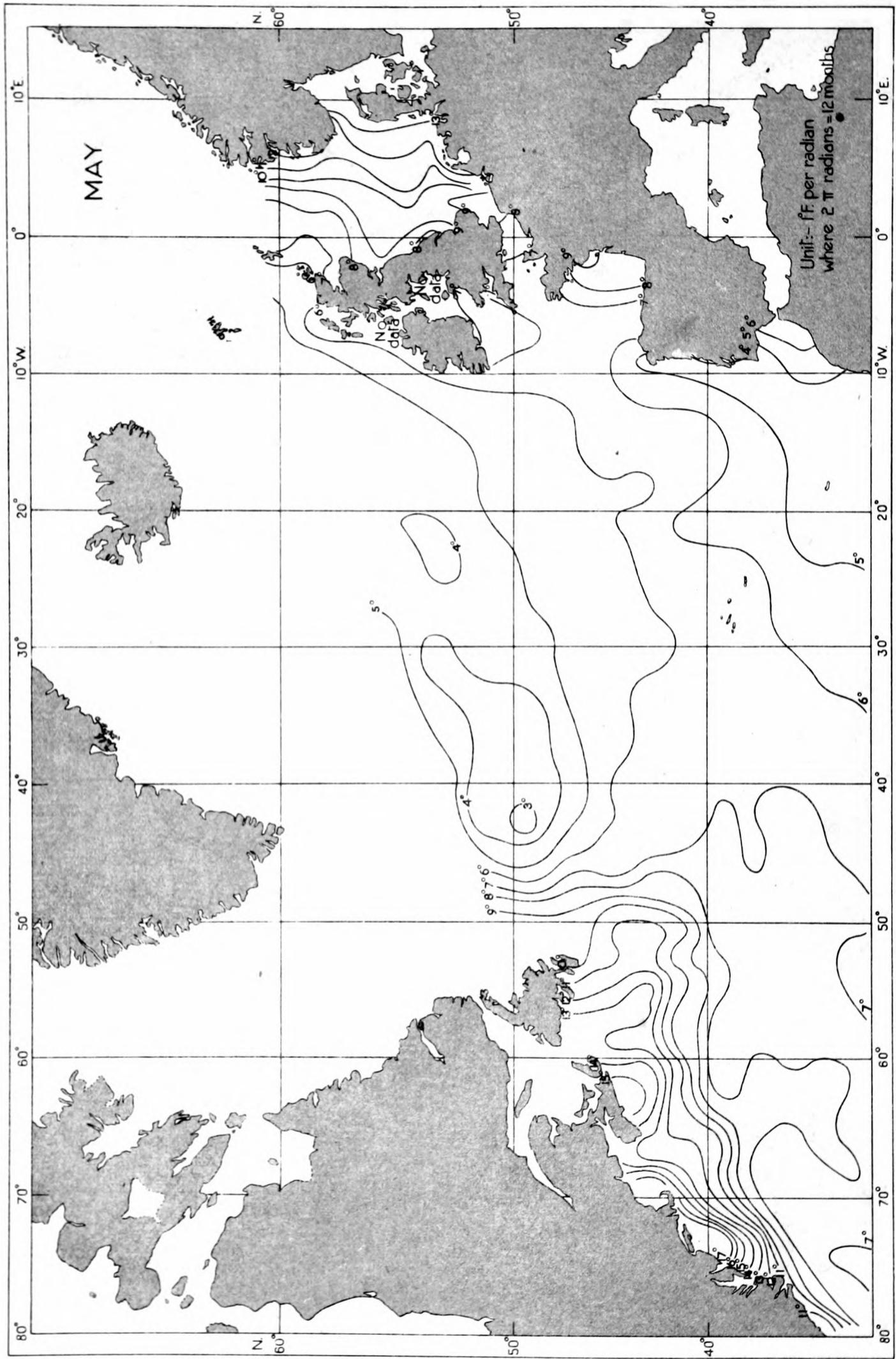


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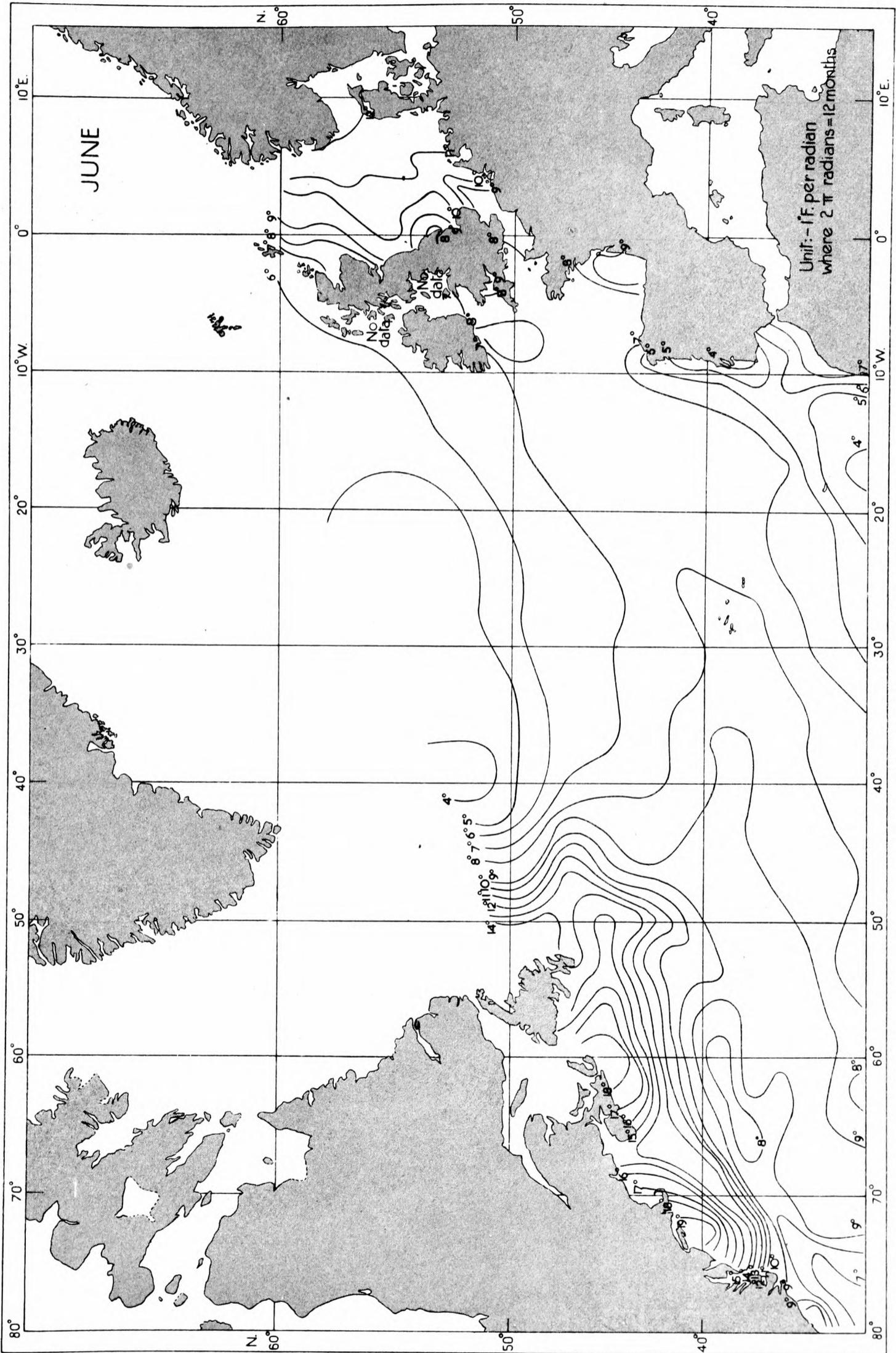


FIG. 12 — continued

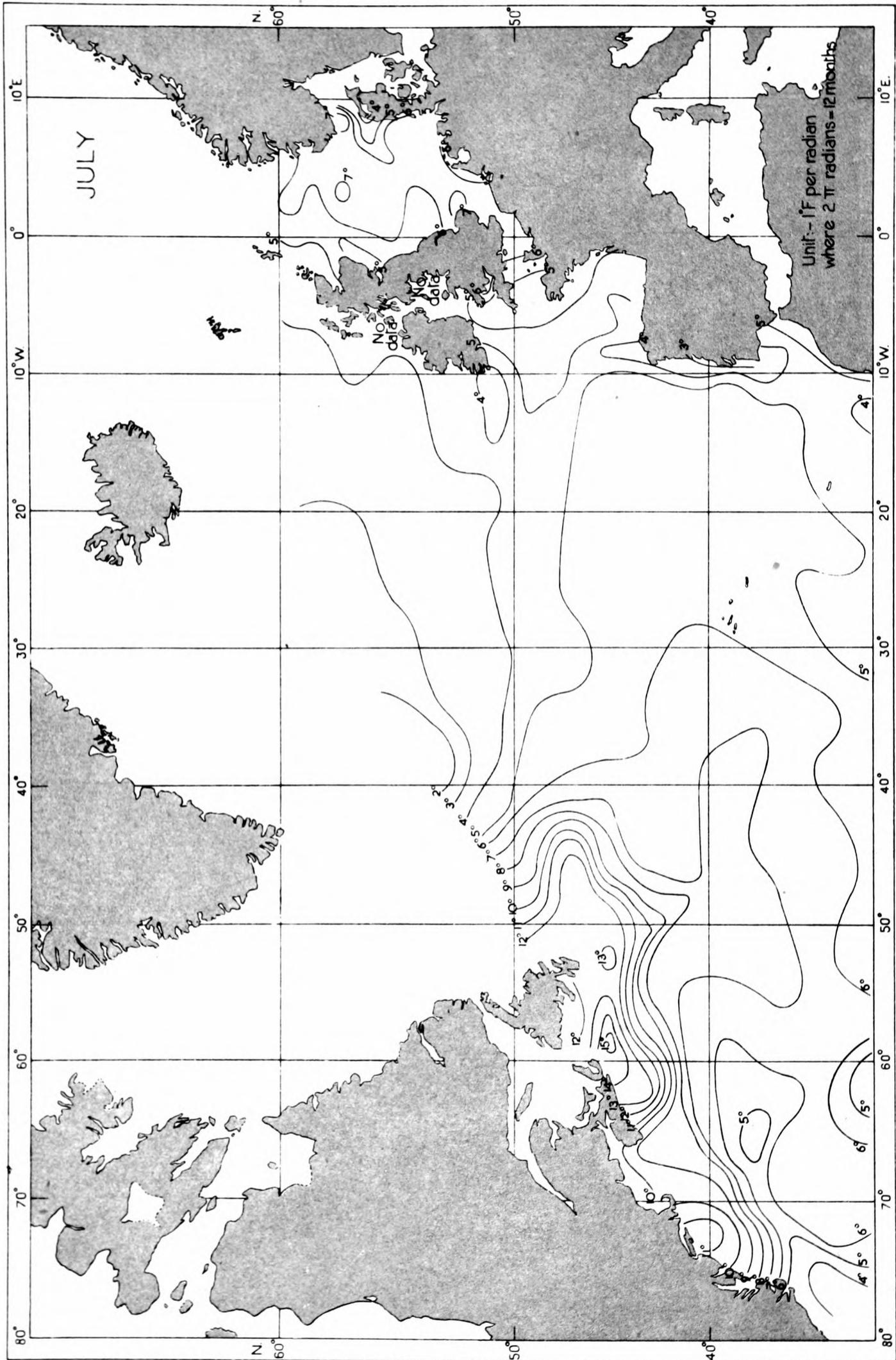


FIG.12— continued

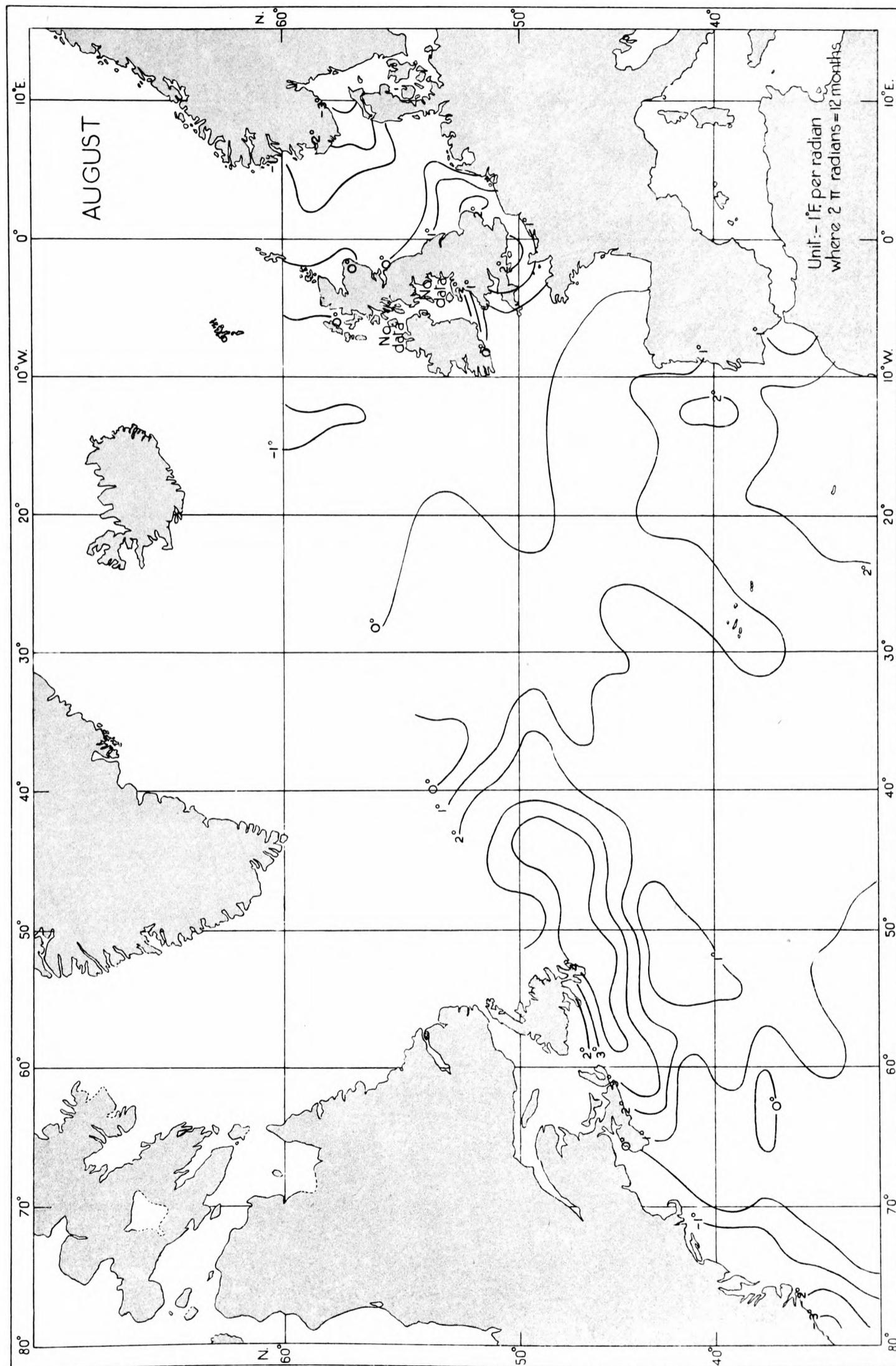


FIG. 12 — continued

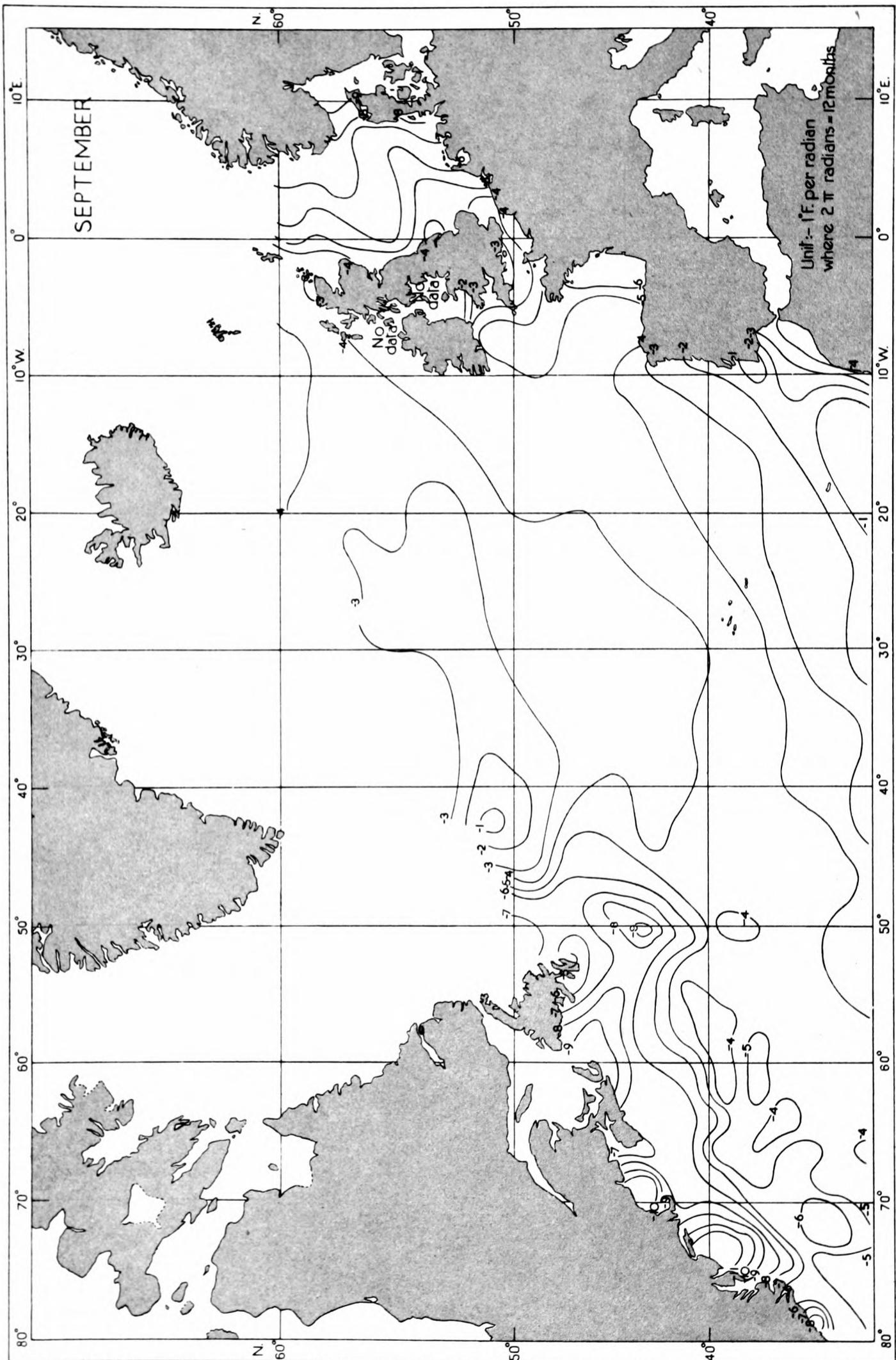


FIG.12 — continued

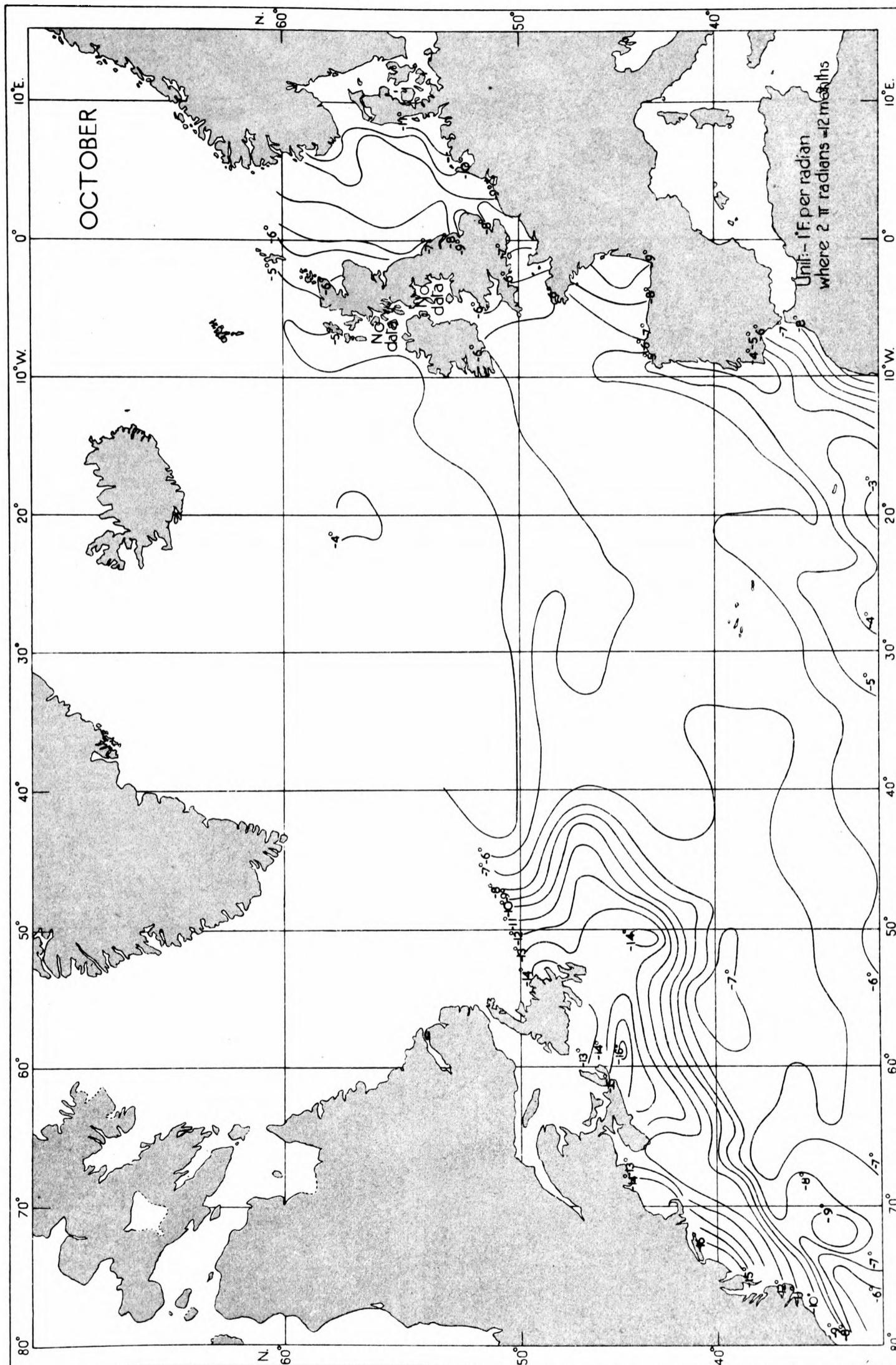


FIG. 12 — continued



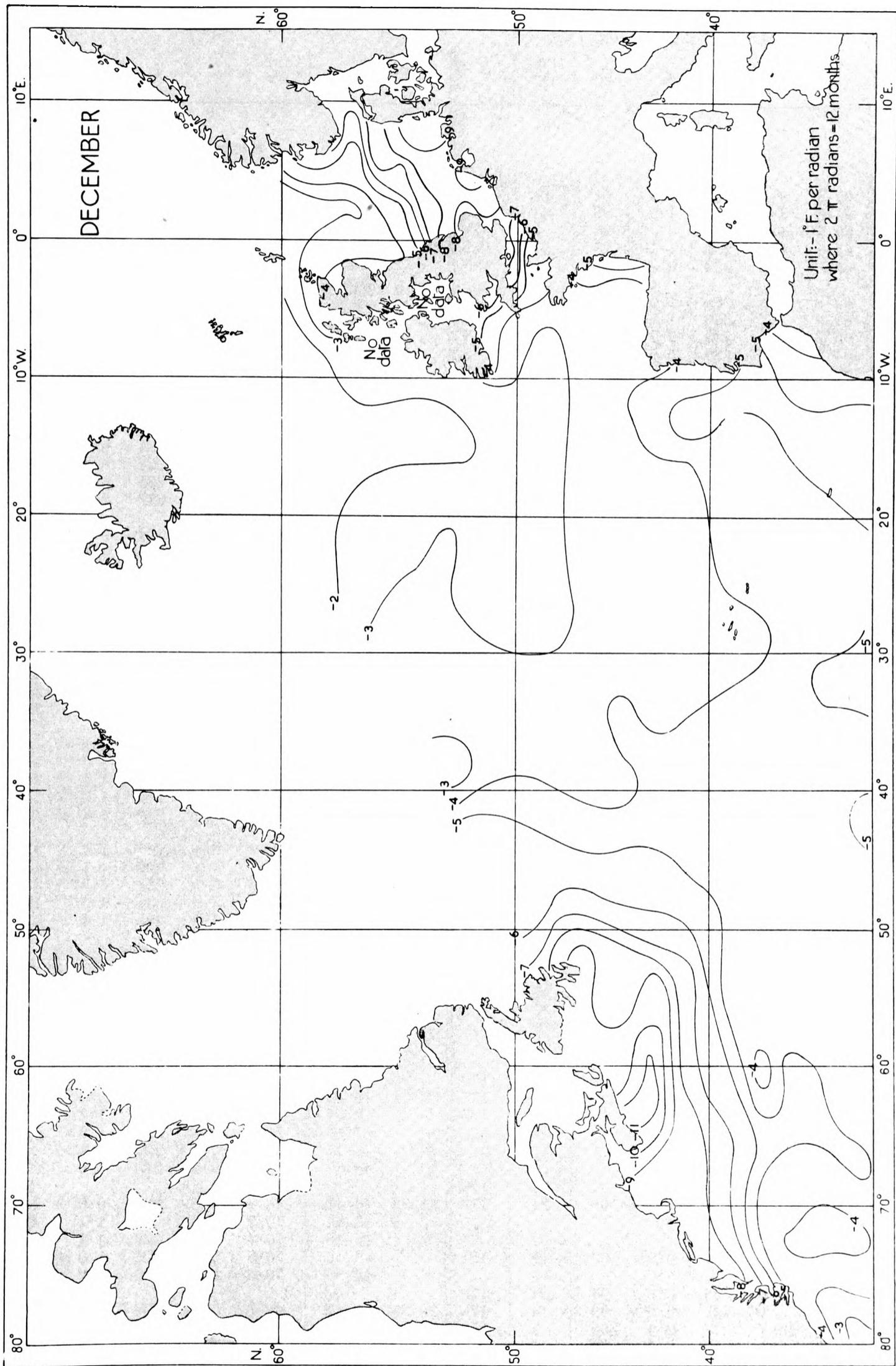


FIG.12 — continued

APPENDIX—TABULATION OF HARMONIC PARAMETERS

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
°N.	°W.	°F.	°F.	°	°F.	°		°	°N.	°W.	°F.	°F.	°	°F.	°		°
Square 109									Square 111— <i>continued</i>								
34-36	00-02	65.5	8.4	240	1.4	51	17	169	36-38	20-22	65.3	6.3	225	0.8	44	13	158
	02-04	64.8	8.3	243	1.9	58	23	169		22-24	65.5	6.2	226	0.7	25	11	169
	04-06	63.5	5.8	236	0.4	26	7	178		24-26	65.5	6.2	228	0.9	34	15	166
	06-08	64.8	6.4	238	1.1	27	17	179		26-28	66.0	6.3	229	1.2	28	19	170
	08-10	65.3	5.9	233	0.8	347	14	195		28-30	66.4	6.1	230	1.3	40	21	165
36-38	00-02	64.8	9.2	238	1.5	22	16	182	38-40	20-22	63.7	5.9	230	1.1	28	19	171
	02-04	63.8	7.8	240	1.3	25	17	183		22-24	63.9	6.1	230	1.0	32	16	169
	04-06	63.2	6.4	235	0.7	34	11	173		24-26	64.7	6.2	229	1.1	30	18	169
	06-08	64.3	6.3	235	0.6	14	10	183		26-28	64.4	6.3	230	1.3	47	21	161
	08-10	62.7	4.8	230	0.4	265	8	233		28-30	64.6	6.3	230	1.3	38	21	166
38-40	08-10	60.9	4.7	232	0.3	270	6	232	Square 112								
30-32	08-10	60.4	7.0	233	1.8	358	26	189	30-32	30-32	..	..	..	..	..	..	..
Square 110									30-32	32-34	70.9	6.1	224	0.4	24	7	167
30-32	10-12	66.1	3.6	215	0.5	296	14	202		34-36	71.2	6.4	224	0.9	28	14	165
	12-14	66.9	4.8	222	0.3	330	6	192		36-38	71.4	6.0	225	0.9	40	15	160
	14-16	67.3	4.9	219	0.6	304	12	202		38-40	71.9	6.1	227	0.6	53	10	155
	16-18	67.9	5.0	220	0.4	319	8	195	32-34	30-32	69.2	6.2	224	0.5	33	8	163
	18-20	68.5	5.2	217	0.4	270	8	217		32-34	69.8	6.4	223	0.6	22	9	167
32-34	10-12	66.5	4.7	229	1.2	301	26	213		34-36	70.1	6.6	224	1.1	27	17	165
	12-14	66.3	5.2	222	0.4	319	8	197		36-38	70.3	6.4	226	1.0	27	16	167
	14-16	66.7	5.1	220	0.4	335	8	187		38-40	70.6	6.5	227	0.7	63	11	151
	16-18	67.1	5.3	224	0.4	315	7	201	34-36	30-32	68.2	6.2	228	0.8	36	13	165
	18-20	67.5	5.4	223	0.5	15	9	171		32-34	68.5	6.9	226	1.2	31	17	165
34-36	10-12	65.5	5.6	228	0.6	27	11	169		34-36	68.8	6.5	228	1.1	28	17	169
	12-14	65.5	5.6	223	0.6	330	11	193		36-38	69.1	6.8	229	1.2	25	18	171
	14-16	65.5	5.6	222	0.6	341	11	187		38-40	69.6	6.9	226	0.9	31	13	165
	16-18	66.1	6.0	225	0.9	15	15	173	36-38	30-32	66.8	6.6	230	1.2	45	18	163
	18-20	66.3	6.0	226	0.8	001	13	181		32-34	67.0	6.8	228	1.2	37	18	165
36-38	10-12	63.6	5.2	224	0.3	290	6	214		34-36	67.5	6.7	226	1.2	25	18	169
	12-14	63.9	5.8	222	0.7	342	12	186		36-38	68.0	7.0	227	1.4	27	20	169
	14-16	64.6	6.2	228	1.0	35	16	165		38-40	68.2	7.2	229	1.4	20	19	174
	16-18	64.8	6.3	227	1.4	13	22	175	38-40	30-32	65.2	6.4	227	1.2	37	19	163
	18-20	64.9	6.1	225	1.0	10	16	175		32-34	66.1	6.4	228	1.1	45	17	161
38-40	10-12	62.5	6.0	227	0.5	11	8	177		34-36	66.3	6.7	227	1.3	27	19	169
	12-14	62.6	5.8	225	1.0	355	17	183		36-38	67.0	6.9	230	1.5	42	22	164
	14-16	63.0	6.1	228	1.0	33	16	167		38-40	67.3	6.8	226	1.4	27	21	167
	16-18	63.2	6.2	226	1.0	32	16	165	Square 113								
	18-20	63.1	6.2	228	1.1	19	18	173	30-32	40-42	72.1	6.5	225	0.6	58	9	151
Square 111										42-44	72.3	6.4	223	0.6	46	9	155
30-32	20-22	68.6	5.0	219	0.3	359	6	175		44-46	72.6	6.4	225	1.0	38	16	161
	22-24	68.8	5.3	222	0.8	358	15	178		46-48	72.8	6.7	225	1.4	41	21	159
	24-26	69.3	5.7	224	0.6	47	11	155		48-50	73.1	6.7	227	1.0	51	15	157
	26-28	69.5	5.3	223	0.2	35	4	161	32-34	40-42	71.1	6.7	226	0.9	40	13	161
	28-30	..	..	..	..	..	..	..		42-44	71.4	6.9	228	1.2	34	17	166
32-34	20-22	67.3	5.8	225	1.0	01	17	179		44-46	71.6	6.8	227	1.3	42	19	161
	22-24	67.8	5.3	226	1.1	06	21	178		46-48	71.8	7.0	227	1.1	43	16	161
	24-26	..	..	..	..	..	..	..		48-50	72.0	7.2	228	1.0	37	14	165
	26-28	..	..	..	..	..	..	..	34-36	40-42	69.8	7.0	228	0.9	42	13	162
	28-30	68.7	5.6	226	0.9	60	16	151		42-44	70.2	7.2	229	1.1	42	15	163
34-36	20-22	66.6	5.8	225	0.8	04	14	178		44-46	70.4	7.1	228	1.1	44	15	161
	22-24	66.9	5.9	229	0.8	09	14	179		46-48	70.5	7.3	226	1.0	34	14	164
	24-26	67.2	5.9	228	0.4	50	7	158		48-50	70.5	7.0	228	1.2	35	17	165
	26-28	67.5	6.1	227	0.9	39	15	163	36-38	40-42	68.6	7.2	226	1.4	30	19	166
	28-30	67.6	6.1	226	1.0	13	16	175		42-44	69.0	6.8	227	1.2	38	18	163
										44-46	69.5	6.9	225	1.1	34	16	163
										46-48	69.6	7.2	225	1.5	31	21	165
										48-50	69.5	7.2	225	1.4	34	19	163



APPENDIX—continued

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° W.	° F.	° F.	°	° F.	°		°
Square 146—continued									Square 148—continued								
44-46	10-12	58.4	6.3	229	1.1	35	17	167	44-46	30-32	61.0	5.6	230	1.2	31	21	169
	12-14	58.7	6.2	232	1.1	46	18	164		32-34	60.8	5.6	228	1.0	15	18	175
	14-16	58.7	5.8	232	1.2	46	21	164		34-36	60.6	5.8	228	0.8	26	14	170
	16-18	58.9	5.8	232	1.1	32	19	171		36-38	60.7	5.7	230	1.0	14	18	178
	18-20	59.2	5.7	232	1.1	31	19	171		38-40	60.9	6.0	225	1.2	38	20	161
46-48	10-12	57.1	5.8	234	1.1	44	19	167	46-48	30-32	58.2	5.4	234	0.9	44	17	167
	12-14	57.2	5.8	233	0.9	46	16	165		32-34	57.9	5.2	232	1.1	39	21	167
	14-16	57.5	5.8	234	1.0	35	17	171		34-36	58.0	5.3	235	1.1	19	21	181
	16-18	57.6	5.6	233	1.0	38	17	169		36-38	58.1	5.3	234	1.4	25	26	177
	18-20	57.9	5.4	231	1.3	32	24	170		38-40	58.3	5.3	230	1.3	19	25	175
48-50	10-12	55.7	5.4	234	1.4	46	26	166	48-50	30-32	55.8	5.1	235	1.0	20	20	180
	12-14	56.0	5.2	237	1.4	35	27	175		32-34	55.4	4.7	236	1.2	15	25	183
	14-16	56.3	4.8	243	1.7	44	35	176		34-36	55.3	4.7	235	1.3	356	28	192
	16-18	56.4	5.2	235	1.1	50	21	165		36-38	55.7	4.8	229	1.1	351	23	189
	18-20	56.9	5.0	236	1.2	47	24	167		38-40	55.3	5.2	227	1.1	353	21	185
Square 147									Square 149								
40-42	20-22	62.4	6.0	231	1.0	13	17	179	40-42	40-42	65.9	6.4	229	1.1	26	17	171
	22-24	62.5	5.9	230	1.2	38	20	166		42-44	65.8	6.1	227	1.3	36	21	164
	24-26	62.7	6.2	230	1.3	31	21	169		44-46	65.6	6.8	228	1.4	38	21	164
	26-28	62.9	6.2	232	1.2	43	19	165		46-48	64.1	8.1	229	0.8	360	10	166
	28-30	63.0	6.0	228	1.3	22	22	172		48-50	61.8	8.9	230	1.4	24	16	173
42-44	20-22	60.6	6.2	229	1.1	36	18	166	42-44	40-42	63.3	6.6	228	1.0	38	15	164
	22-24	61.0	6.2	230	1.1	41	18	165		42-44	63.5	6.8	229	1.0	20	15	174
	24-26	61.5	5.9	230	1.2	34	20	168		44-46	62.4	7.5	231	0.6	350	8	191
	26-28	61.8	5.6	226	1.2	29	21	167		46-48	57.4	8.5	232	1.2	31	14	171
	28-30	62.3	5.7	229	1.1	25	19	171		48-50	48.9	10.1	235	1.7	32	15	174
44-46	20-22	59.4	5.7	232	1.3	36	23	169	44-46	40-42	60.8	6.5	228	1.4	24	21	171
	22-24	59.6	5.4	231	1.4	32	26	170		42-44	59.6	7.1	232	1.3	04	18	185
	24-26	60.2	5.6	231	0.8	30	14	171		44-46	55.0	7.7	233	1.9	14	25	181
	26-28	60.4	5.5	228	1.0	23	18	171		46-48	49.3	8.5	232	1.8	06	21	184
	28-30	60.8	5.6	231	1.0	29	18	171		48-50	43.1	10.8	231	2.8	28	26	172
46-48	20-22	58.3	5.4	228	1.0	33	19	167	46-48	40-42	56.9	6.0	234	1.4	354	23	192
	22-24	58.4	5.4	229	1.0	26	19	171		42-44	51.1	7.4	235	2.5	02	34	189
	24-26	58.3	5.3	232	1.3	20	25	177		44-46	45.7	8.6	225	2.8	02	33	179
	26-28	58.4	5.3	232	1.2	36	23	169		46-48	42.0	10.0	224	2.8	10	28	174
	28-30	58.3	5.2	232	0.9	39	17	167		48-50	40.4	10.8	226	2.5	12	23	175
48-50	20-22	56.5	4.7	236	1.1	42	23	170	48-50	40-42	54.8	5.0	228	1.2	342	24	192
	22-24	56.3	4.8	235	0.9	43	19	169		42-44	51.2	5.7	221	1.7	342	30	185
	24-26	56.4	5.1	236	0.8	35	16	173		44-46	46.2	7.0	222	1.8	346	26	184
	26-28	56.4	5.1	233	1.0	30	20	173		46-48	43.1	7.5	225	1.6	357	21	181
	28-30	56.2	4.8	233	1.2	21	25	177		48-50	39.9	9.2	230	2.0	17	22	177
Square 148									Square 150								
40-42	30-32	63.7	6.1	227	1.1	15	18	175	40-42	50-52	61.9	9.2	233	1.6	62	17	157
	32-34	64.5	6.0	227	1.1	35	18	165		52-54	63.0	9.3	231	0.9	25	10	173
	34-36	65.1	6.6	230	1.2	22	18	174		54-56	63.8	9.2	225	0.8	78	9	141
	36-38	65.3	6.7	225	1.4	33	21	163		56-58	64.6	8.9	227	0.9	54	10	155
	38-40	65.5	6.3	221	1.6	01	25	175		58-60	63.8	9.3	231	0.7	35	8	169
42-44	30-32	63.0	5.9	230	1.1	22	19	174	42-44	50-52	48.2	11.8	238	2.2	25	19	181
	32-34	63.1	6.2	230	1.3	37	21	167		52-54	52.0	11.8	238	1.1	14	9	186
	34-36	63.5	6.4	228	1.6	38	25	164		54-56	53.3	12.4	235	0.7	67	6	157
	36-38	63.1	6.2	230	0.9	31	14	169		56-58	52.9	12.8	233	1.0	37	8	169
	38-40	63.2	6.1	228	1.2	28	20	169		58-60	51.1	13.3	230	0.9	28	7	171

APPENDIX—continued

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
°N.	°W.	°F.	°F.	°	°F.	°		°	°N.	°W.	°F.	°F.	°	°F.	°		°
Square 150—continued									Square 181 (German data)—continued								
44-46	50-52	44.3	12.4	229	2.4	17	19	175	57-58	0-1	49.2	6.3	233	1.3	66	21	155
	52-54	45.0	12.5	226	2.4	12	19	175		1-2	48.2	6.3	227	0.9	55	14	154
	54-56	45.2	12.6	229	2.4	25	19	171		2-3	49.3	6.5	230	0.9	56	14	157
	56-58	44.6	14.0	228	2.6	28	18	169		3-4	47.9	7.3	234	0.4	40	5	169
	58-60	43.7	14.6	229	3.0	14	21	177									
46-48	50-52	40.5	12.0	228	2.3	03	19	181	58-59	0-1	48.8	5.4	232	1.3	50	24	162
	52-54	40.1	11.9	228	2.1	348	18	189		1-2	48.7	5.5	229	0.9	70	16	149
	54-56	41.7	12.2	229	2.1	19	17	175		2-3	48.5	5.4	229	0.7	30	13	169
	56-58	41.9	12.9	230	1.5	36	12	167		3-4	48.8	5.3	228	0.7	35	13	165
										4-5	49.1	5.1	226	0.8	49	16	156
48-50	50-52	39.0	11.0	230	2.5	23	23	173		5-6	49.6	5.4	227	0.8	58	15	153
	52-54	39.0	11.7	231	2.8	10	24	181		6-7	50.1	5.1	234	0.9	66	18	156
										7-8	50.5	4.5	236	0.9	46	20	168
										8-9	50.6	4.2	241	1.0	38	24	177
										9-10	50.8	4.3	242	0.9	45	23	175
Square 151									Square 182								
40-42	60-62	61.5	10.3	238	0.9	50	9	168	59-60	0-1	48.8	5.8	232	1.7	60	30	157
	62-64	59.2	11.2	242	1.0	14	9	190		1-2	48.6	4.9	226	0.9	54	19	154
	64-66	56.2	11.7	238	1.4	24	12	181		2-3	48.8	5.7	230	0.8	47	14	161
	66-68	52.8	12.1	235	1.3	47	11	167		3-4	49.2	4.6	226	0.9	50	20	156
	68-70	51.5	12.3	232	1.3	49	11	163		4-5	49.6	4.4	232	1.0	51	23	161
										5-6	49.9	4.0	223	1.0	35	25	160
42-44	60-62	49.6	14.6	227	1.5	36	10	164		6-7	50.4	4.4	238	1.5	45	34	170
	62-64	48.5	15.0	227	1.7	35	11	165		7-8	50.1	3.7	238	1.2	40	32	174
	64-66	46.3	13.3	230	1.3	46	10	162		8-9	50.3	3.4	237	1.2	30	35	177
	66-68	46.5	11.7	234	1.0	45	9	167		9-10	50.0	3.3	234	1.4	30	42	174
	68-70	49.2	13.2	238	2.4	53	18	167									
44-46	60-62	44.4	14.8	228	2.7	23	18	171									
Square 181 (German data)									Square 183								
50-51	0-1	52.8	7.9	228	0.5	00	6	183	50-52	20-22	55.0	4.4	236	1.0	50	23	166
	1-2	52.9	7.6	227	0.4	06	5	179		22-24	54.9	4.4	230	1.0	41	23	165
	2-3	53.2	7.0	226	0.5	12	7	175		24-26	54.5	4.6	239	0.9	46	20	171
	3-4	53.5	6.5	228	0.5	47	8	159		26-28	54.4	4.5	233	0.8	31	18	173
	4-5	53.7	6.4	232	0.8	64	12	155		28-30	54.0	4.4	233	0.7	34	16	171
	5-6	53.3	6.0	231	0.7	61	12	155									
	6-7	53.6	6.6	236	1.4	72	21	155									
	7-8	54.1	6.8	237	1.2	39	18	173									
	8-9	54.4	6.8	237	1.3	59	20	162									
	9-10	54.6	6.3	238	0.8	62	13	162									
51-52	3-4	52.5	8.3	232	0.7	30	8	172	52-54	10-12	..	..	..	..	..	..	..
	4-5	52.7	7.4	231	0.8	07	11	182		12-14	53.9	4.5	238	1.3	42	29	172
	5-6	53.0	6.6	231	0.8	93	12	140		14-16	54.3	4.4	238	1.2	35	27	175
	6-7	53.1	6.0	233	1.1	78	19	149		16-18	53.8	4.3	237	0.8	44	19	170
	7-8	53.2	6.4	234	1.3	38	21	170		18-20	53.7	4.1	233	0.5	53	12	161
	8-9	53.1	6.3	237	0.6	61	10	161									
52-53	5-6	51.8	6.2	215	0.4	22	7	159	54-56	10-12	52.6	4.4	240	0.9	71	20	159
	6-7	52.2	6.1	223	0.5	325	8	195		12-14	52.8	4.1	240	1.0	41	24	175
53-54	5-6	51.3	6.5	220	0.6	60	9	145		14-16	52.9	4.0	240	0.8	34	20	178
54-55	0-1	48.9	7.6	234	0.9	75	12	151		16-18	52.9	3.9	239	0.8	34	21	177
	1-2	49.0	7.0	236	1.3	270	18	..		18-20	52.9	3.9	238	1.0	38	26	174
	5-6	50.5	5.8	216	0.2	51	3	146									
55-56	0-1	49.5	7.6	234	1.6	62	21	158	56-58	10-12	52.0	4.1	227	0.9	37	22	163
	1-2	48.9	7.4	225	1.3	75	18	143		12-14	52.3	4.5	237	1.3	65	29	159
56-57	0-1	49.2	6.9	231	1.6	66	23	153		14-16	51.6	4.1	239	0.9	47	22	171
	1-2	48.5	6.6	230	1.0	75	15	148		16-18	51.4	3.9	241	0.8	33	21	179
	2-3	48.4	7.1	233	0.8	87	11	145		18-20	51.4	3.9	240	0.8	15	21	187

APPENDIX I—*continued*

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°	°	°	° N.	° E.	° F.	° F.	°	° F.	°	°	°
Square 183— <i>continued</i>									Square 216 (German data)— <i>continued</i>								
52-54	20-22	53.1	4.2	237	0.3	15	7	185	54-55	1-2	49.5	8.6	235	0.9	73	10	153
	22-24	52.9	4.0	238	0.3	03	7	191		2-3	49.8	9.5	236	0.9	73	10	154
	24-26	52.5	3.7	236	0.4	43	11	169		3-4	49.9	9.8	234	1.0	82	10	148
	26-28	52.1	4.2	235	0.2	38	5	171		4-5	50.3	10.0	231	1.0	86	10	143
	28-30	51.0	4.3	237	0.5	356	12	194		5-6	50.5	10.3	232	0.7	78	7	148
54-56	20-22	52.9	4.0	235	0.8	31	20	175		6-7	50.4	11.2	235	0.9	82	8	149
	22-24	52.6	4.3	235	0.7	43	16	169		7-8	49.8	12.0	237	0.6	98	5	143
	24-26	51.9	4.4	235	0.5	30	11	175		8-9	49.4	12.8	242	0.7	85	6	154
	26-28	51.2	4.8	238	0.3	36	6	175									
	28-30	49.7	5.1	239	0.1	112	2	138	55-56	0-1	49.7	8.1	231	1.7	70	21	151
56-58	20-22	51.4	4.0	239	0.6	60	15	164		1-2	49.6	8.0	235	1.5	55	19	162
	22-24	51.5	3.7	237	0.6	30	16	177		2-3	49.6	8.6	235	1.6	50	19	165
	24-26	50.6	4.2	238	0.7	55	17	165		3-4	49.6	9.2	235	1.1	70	12	155
Square 184										4-5	49.9	9.6	235	1.3	70	13	155
50-52	30-32	53.0	4.0	235	0.3	17	7	181		5-6	50.1	9.9	234	1.3	95	13	142
	32-34	53.0	4.3	238	0.2	350	5	198		6-7	49.9	10.3	232	0.9	85	9	145
	34-36	52.6	4.5	239	0.4	337	9	205		7-8	49.8	11.2	237	0.8	85	7	150
	36-38	52.0	4.7	237	0.4	354	9	195	56-57	0-1	49.6	7.2	232	1.8	63	25	155
	38-40	51.8	4.2	235	0.7	326	17	207		1-2	49.5	7.4	235	1.8	58	24	161
52-54	30-32	50.2	4.4	242	0.6	13	14	191		2-3	49.3	8.0	235	1.7	56	21	162
	32-34	..	..	..	..	..	..	..		3-4	49.2	8.4	235	1.5	53	18	163
	34-36	48.6	4.7	239	0.6	11	13	189		5-6	49.3	9.4	234	1.5	65	17	156
	36-38	48.1	4.3	250	0.4	58	9	176		6-7	49.7	9.8	238	1.3	95	13	146
	38-40	47.5	5.7	242	0.4	98	7	148		7-8	49.3	10.4	238	1.3	105	13	140
Square 185										8-9	48.7	11.2	241	1.2	81	11	156
50-52	40-42	52.0	4.9	231	0.9	332	18	200	57-58	1-2	49.7	7.0	230	1.9	44	24	163
	42-44	51.9	5.4	228	0.8	352	15	187		2-3	49.4	7.5	234	2.0	50	26	164
Square 216 (German data)										3-4	48.8	7.9	235	2.0	50	25	165
50-51	0-1	52.4	8.4	232	0.7	8	8	183		4-5	48.5	8.5	237	1.8	58	21	163
	1-2	52.2	8.7	233	0.5	11	6	182		5-6	49.0	8.7	236	1.9	64	22	159
51-52	1-2	52.1	8.8	233	0.5	0	6	185		6-7	49.0	9.3	238	1.8	70	20	158
	2-3	52.1	9.0	233	0.6	357	7	189		7-8	49.3	9.0	239	2.3	61	26	163
	8-4	51.5	10.4	239	0.4	09	4	189		8-9	49.0	10.3	240	1.8	98	18	146
52-53	1-2	50.5	9.8	235	0.8	14	8	183		9-10	48.8	10.8	244	1.6	86	15	156
	2-3	51.5	9.4	230	0.9	19	10	176	58-59	0-1	49.3	6.6	233	1.5	45	23	165
	3-4	51.5	9.7	234	0.6	10	6	184		1-2	49.0	6.4	234	1.6	59	25	160
	4-5	50.5	11.5	235	0.9	117	7	..		2-3	49.3	6.8	235	1.8	63	26	159
53-54	0-1	49.0	8.2	233	0.4	03	5	182		3-4	49.1	7.6	238	1.7	56	22	165
	1-2	49.4	9.3	233	0.3	60	3	158		4-5	48.6	8.6	236	1.8	72	21	155
	2-3	50.0	9.3	233	0.3	60	3	158		5-6	48.5	9.6	238	1.6	71	16	157
	3-4	50.8	9.7	232	0.5	42	5	166		6-7	48.5	10.4	239	1.6	71	16	158
	5-6	50.7	10.8	239	0.5	46	5	171	59-60	0-1	48.9	6.0	235	1.8	59	30	160
	6-7	50.2	11.5	240	0.6	46	5	172		1-2	48.8	6.3	235	1.8	45	29	167
	7-8	49.8	12.0	240	0.5	47	4	172		2-3	49.0	6.7	240	1.4	55	21	167
										3-4	49.1	7.4	233	2.1	50	28	163
										4-5	48.8	8.6	238	1.8	70	21	158