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# SEASONAL CHANGE OF SURFACE TEMPERATURE OF THE NORTH ATLANTIC OCEAN

BY

T. H. KIRK, B.Sc.

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# SEASONAL CHANGE OF SURFACE TEMPERATURE OF THE NORTH ATLANTIC OCEAN

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## SUMMARY

The facts of the seasonal change of surface temperature of the North Atlantic Ocean are presented by means of charts showing the distribution of harmonic parameters. This method makes it possible to write down by inspection an analytic expression for the process of seasonal change at any position within the area of the charts. The influence of the various factors underlying seasonal change is also briefly discussed. A new series of charts is then derived to show the distribution of the rate of change of mean sea-surface temperature for each month of the year.

## § 1—INTRODUCTION

The seasonal change of sea-surface temperature is of importance not only to oceanographers and meteorologists for its significance in the major problem of the heat exchange between ocean and atmosphere, but also to marine biologists for its effect on the growth and travel of the different forms of marine life. Whoever is interested in the effects of variations of sea-surface temperature requires a knowledge of the seasonal fluctuation, for it would appear unlikely that in temperate latitudes any other fluctuations could exceed in magnitude the seasonal one. A study of the seasonal change of sea-surface temperature should logically, therefore, precede any attempt to apply the method of anomalies of sea-surface temperature to any problem.

Climatic atlases are available depicting the mean distribution of sea-surface temperature for each month of the year, each chart being based on observations taken over a long period of years. Seasonal change can be assessed qualitatively from these charts by noting visually the changes that occur from month to month. For a detailed quantitative analysis, however, it is preferable to use the original observations. This paper summarizes a mass of sea-surface temperature data for the North Atlantic Ocean, and presents the facts of seasonal change in forms suitable for both theoretical investigation and practical use.

## § 2—SOURCES OF DATA

Tabulated values of sea-surface temperature, available for the periods 1887–99 and 1921–38, have been used. These data, based on British ships' logs, had already been used in the preparation of the sea-temperature charts in "Monthly meteorological charts of the Atlantic Ocean"<sup>1\*</sup>, and, recently, in the preparation of more detailed charts of sea temperature for the North Atlantic<sup>2</sup>. Monthly mean values for 2° squares were, therefore, already available. In this later publication<sup>2</sup> some account was given of the limitations attached to the use of sea-temperature data.

The data were found to be relatively scanty in the coastal waters of the British Isles and in the North Sea. In these areas German data have been preferred. The mean values used, for 1°

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\* The index numbers refer to the Bibliography on p. 19.

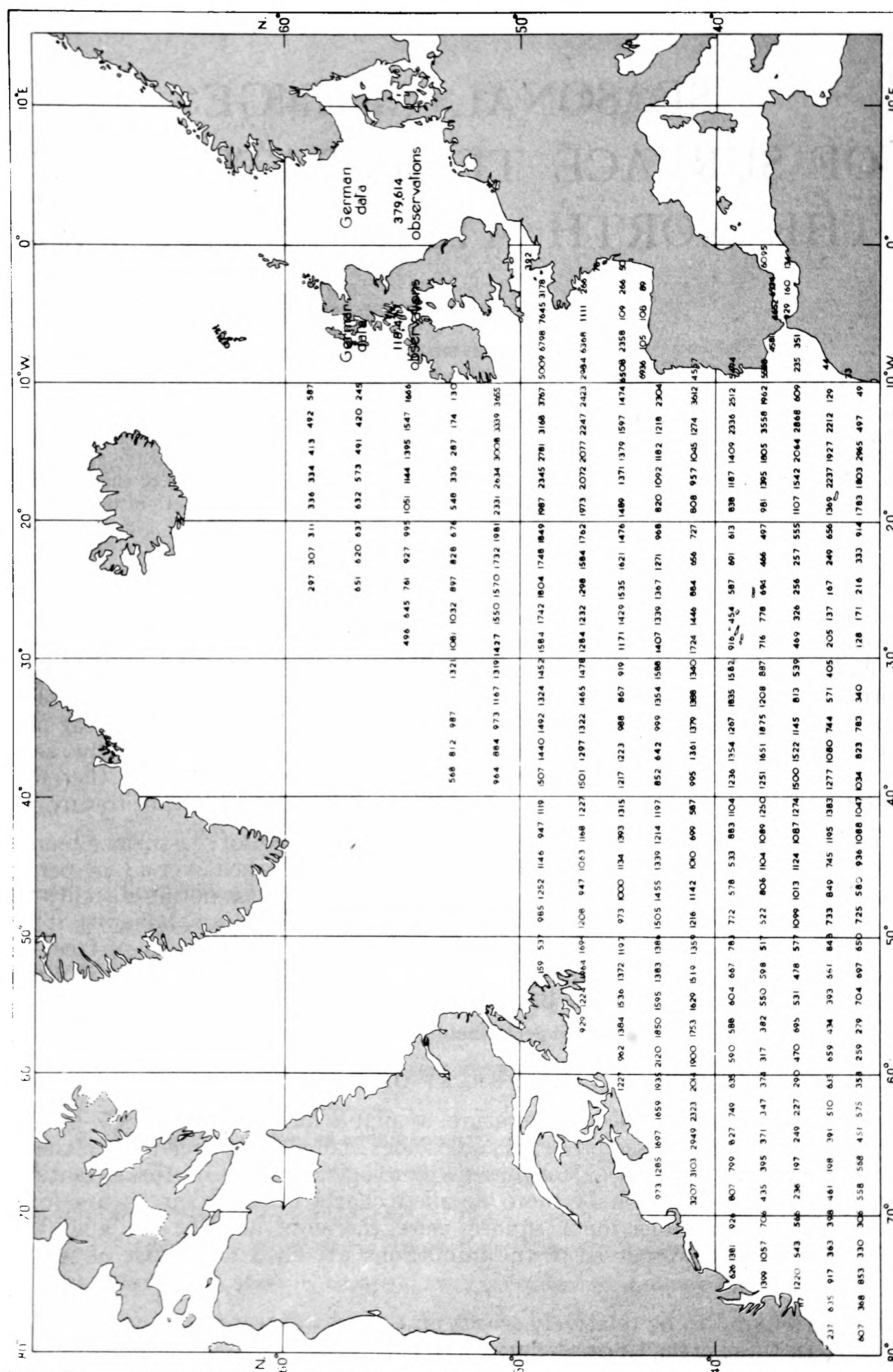


FIG.1-DISTRIBUTION OF NUMBER OF OBSERVATIONS



squares, are based on observations made during the period 1862–1946, and hence are not directly comparable with the British data. There appears no reason to suppose, however, that the mean process of seasonal change can be significantly different.

The distribution of the number of observations used is shown in Fig. 1. Unfortunately, scarcity of observations has not permitted the investigation to be extended to northern waters. The analysis has also not been made for certain squares where the data were few in number or badly distributed throughout the year.

### § 3—ANALYSIS OF DATA

Monthly means for individual squares have been plotted. The smooth curve drawn through the values for the different months represents the course of seasonal change. By plotting data from different squares it is apparent that important differences exist between the characteristic curves. These differences are of :—

- (i) Amplitude ; maximum departure from the yearly mean value varies appreciably.
- (ii) Phase ; slight variations occur in the times of maxima and minima.
- (iii) Shape ; curves show different degrees of asymmetry.

Harmonic analysis has been used to derive parameters which facilitate the examination of variations from square to square. Representing the sea-surface temperature by  $T$ , expressed in degrees Fahrenheit in this paper, the normal expansion in a Fourier series can be written

$$T = a_0 + a_1 \sin(t + A_1) + a_2 \sin(2t + A_2) + a_3 \sin(3t + A_3) + \dots$$

where  $t$ , representing the time, takes values from  $0^\circ$  to  $360^\circ$ .

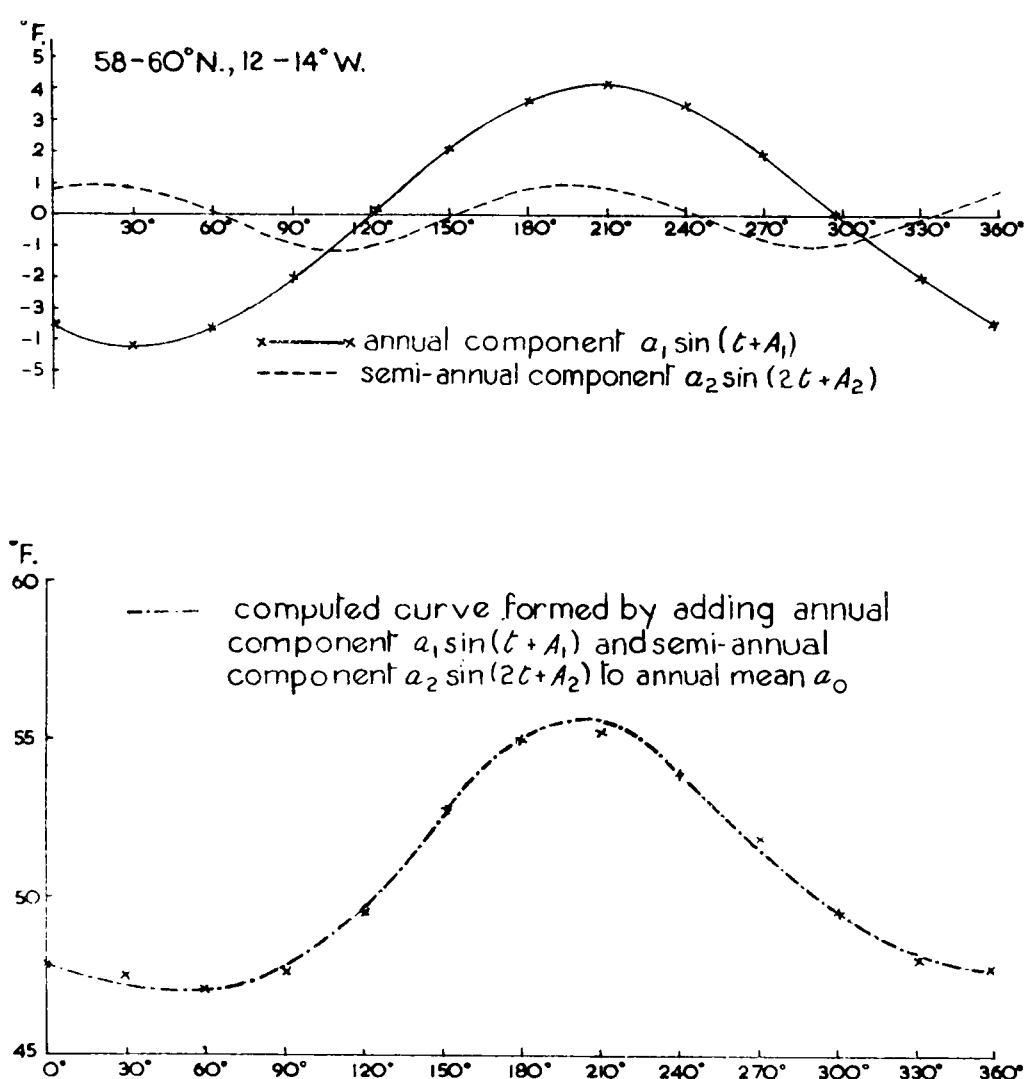
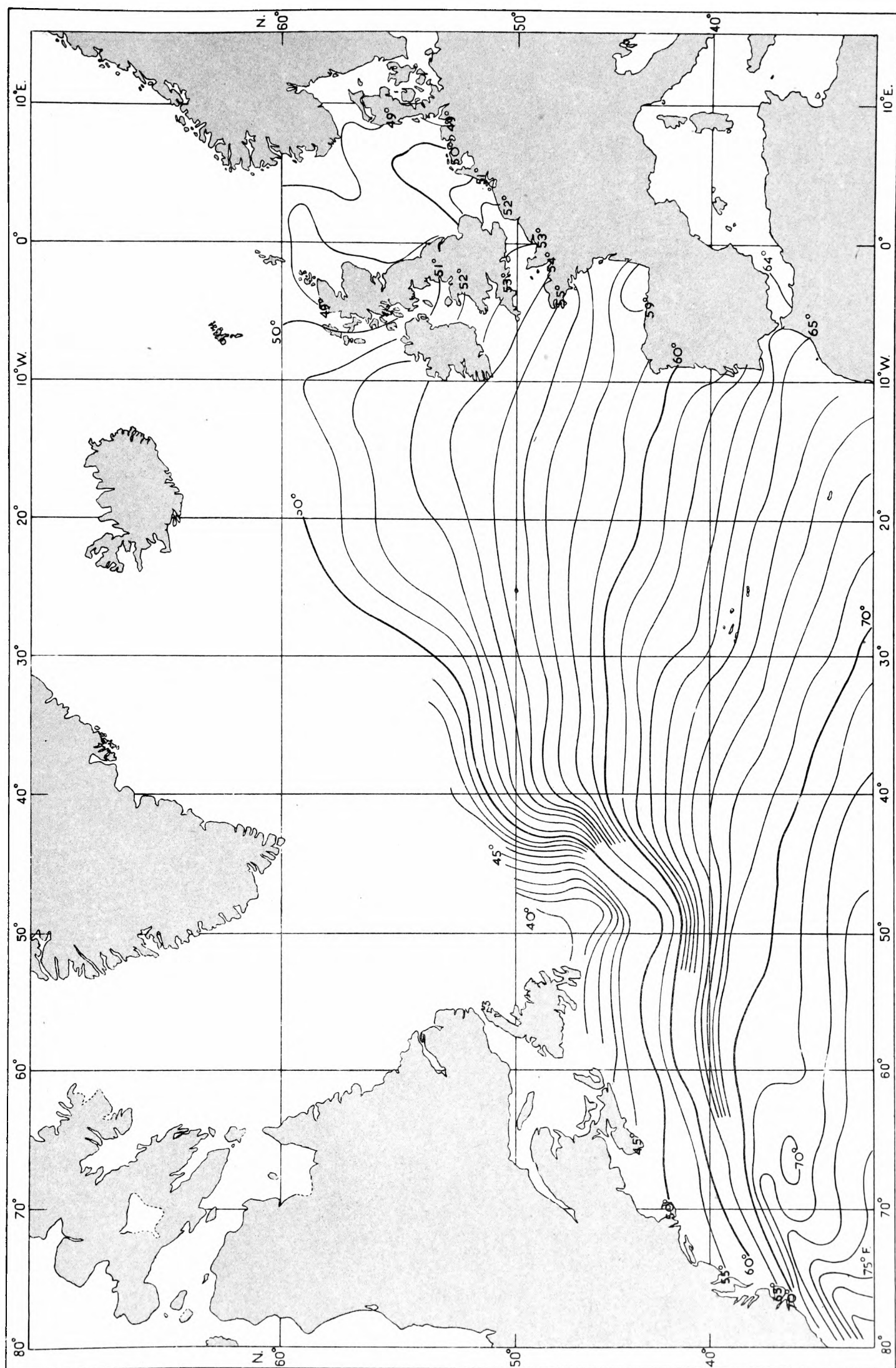


FIG. 2—FIT AFFORDED BY COMPUTED CURVE



FIG. 3—DISTRIBUTION OF ANNUAL MEAN SEA-SURFACE TEMPERATURE ( $T_s$ )

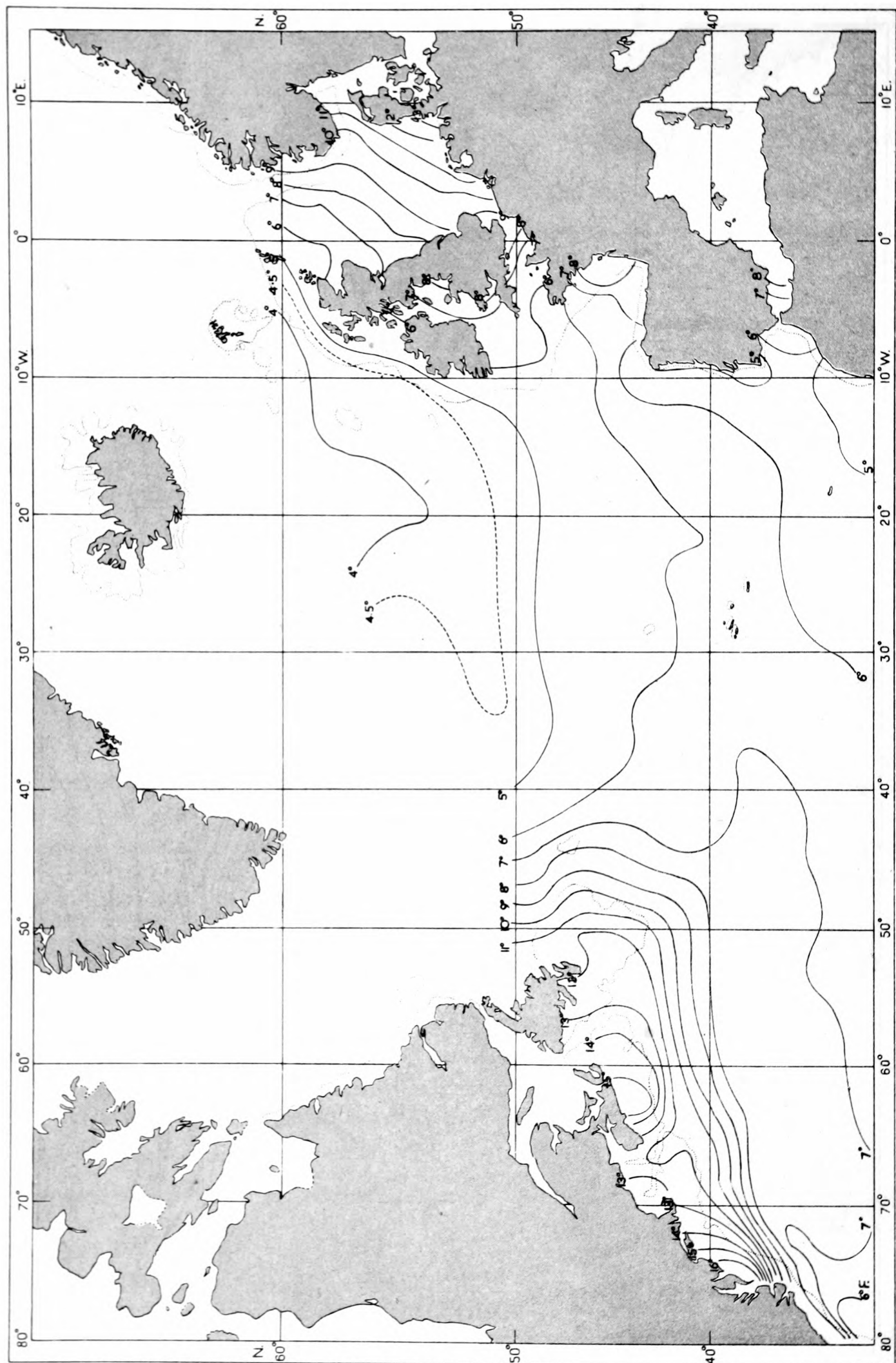


FIG 4-DISTRIBUTION OF AMPLITUDE OF ANNUAL COMPONENT ( $a_1$ )



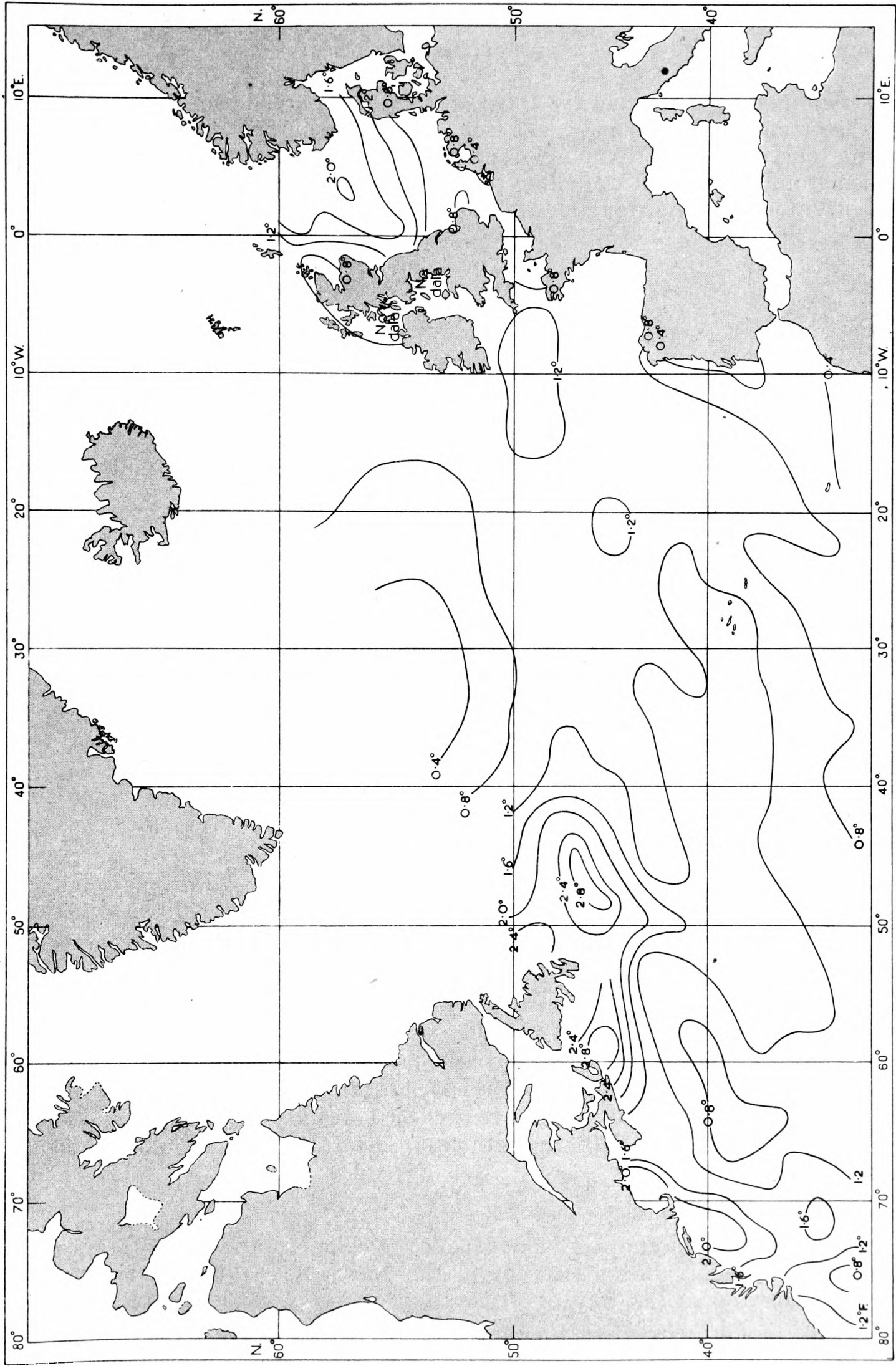


FIG.5 - DISTRIBUTION OF AMPLITUDE OF SEMI-ANNUAL COMPONENT ( $a_2$ )

- (iv) Small values occur in the upwelling areas off the coasts of Portugal and Morocco.
- (v) A small area of high values occurs in the North Sea.

*Ratio of amplitudes.*—The quantity  $100a_2/a_1$  may be regarded as a measure of the degree of skewness or distortion of the seasonal curve from a pure sine curve. In areas where this quantity is small a sine curve will approximately represent the seasonal variation. Fig. 6 shows an example taken from the area of upwelling off Portugal (see p. 18). It is easily seen that the first component affords a good representation of the seasonal variation.

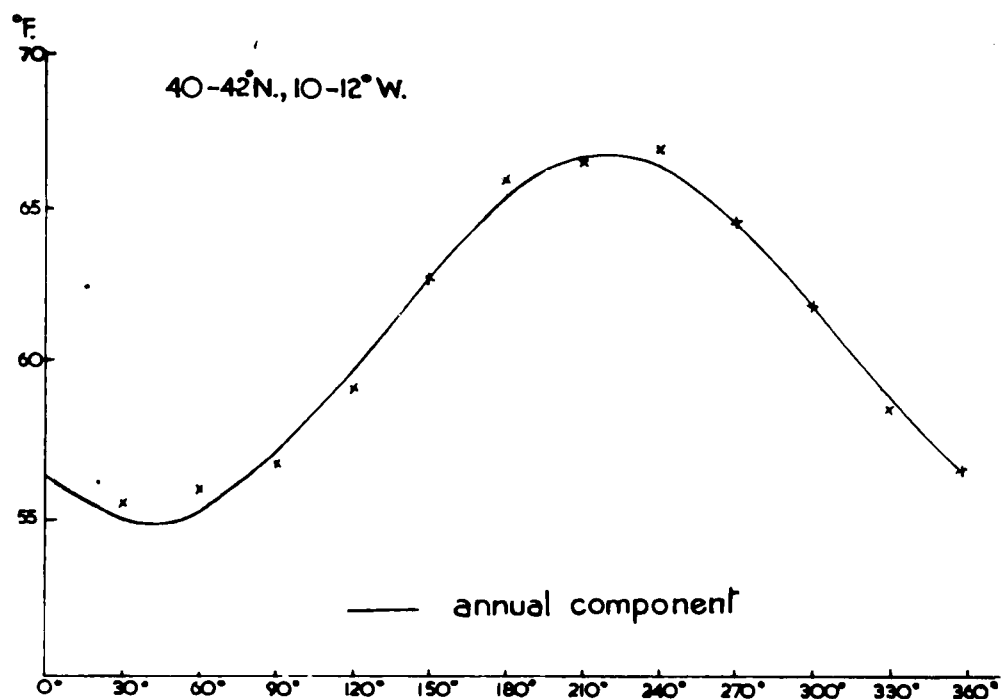


FIG. 6—GOODNESS OF FIT AFFORDED BY ANNUAL COMPONENT

Fig. 7 shows the following features :—

- (i) The maximum values (over 30 per cent.) are reached in the northern part of the North Sea, north-west of Scotland and east of Newfoundland. Relatively high values also occur in a broad belt extending south-westward from the British Isles.
- (ii) Low values occur in the upwelling areas off the coasts of Portugal and Morocco and south of the main belt of high values. There are also low values off the American coast, in the mid Atlantic north of  $50^{\circ}$  N., and in the southern coastal waters of the British Isles.
- (iii) The greatest variability occurs in the North Sea and in the coastal waters of the British Isles.

*Phase of annual component.*—The phase angle  $A_1$  of the annual component is important inasmuch as it largely determines the time at which the sea temperature reaches maximum and minimum values. It varies for the most part between  $220^{\circ}$  and  $240^{\circ}$ . An angle of  $240^{\circ}$  indicates that the minimum value of the component occurs on February 14 and the maximum value on August 16. When the angle is  $220^{\circ}$  the minimum occurs on March 7 and the maximum on September 7.

Fig. 8 shows the following characteristics :—

- (i) Centres of both high and low values flank the course of the Gulf Stream and the North Atlantic Current. High values also occur in the North Sea, along the coasts of Germany, Denmark and Norway, in the Bay of Biscay and off the north coast of Spain.
- (ii) A trough of low values off the Portuguese coast appears to be associated with the course of the Portugal Current.

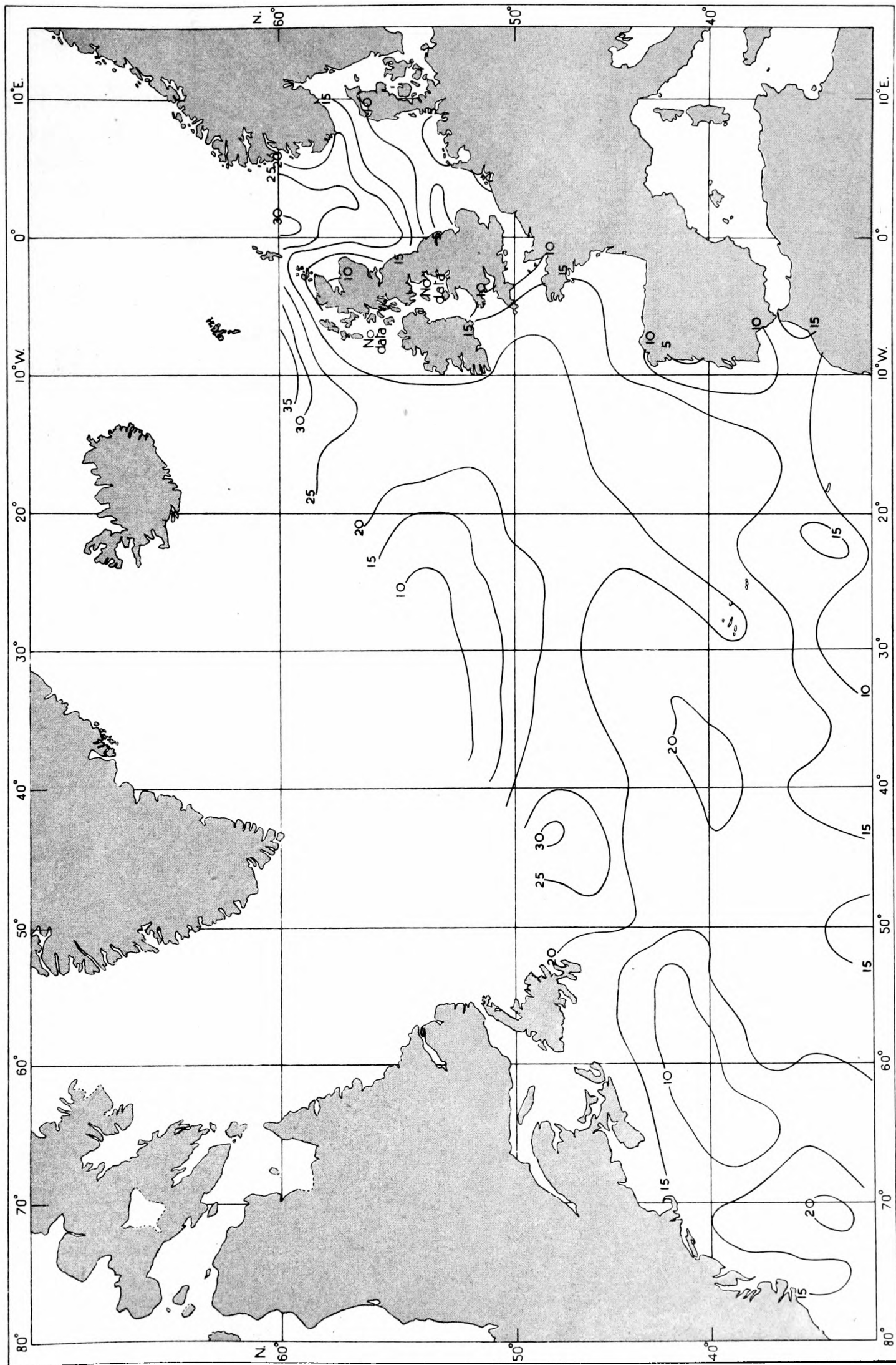


FIG. 7 — DISTRIBUTION OF  $100 a_2/a_1$



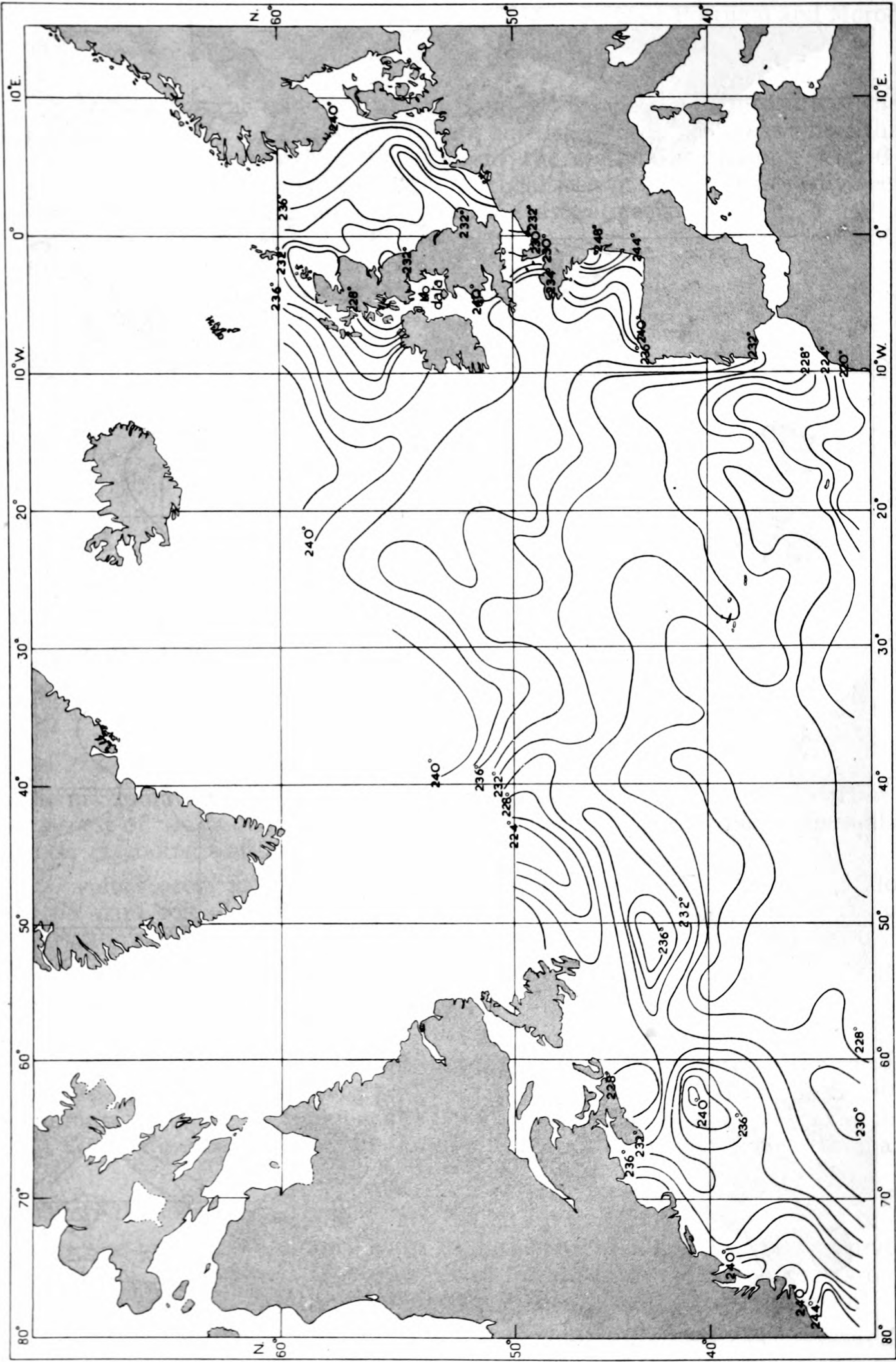


FIG.8—DISTRIBUTION OF PHASE OF ANNUAL COMPONENT ( $A_1$ )



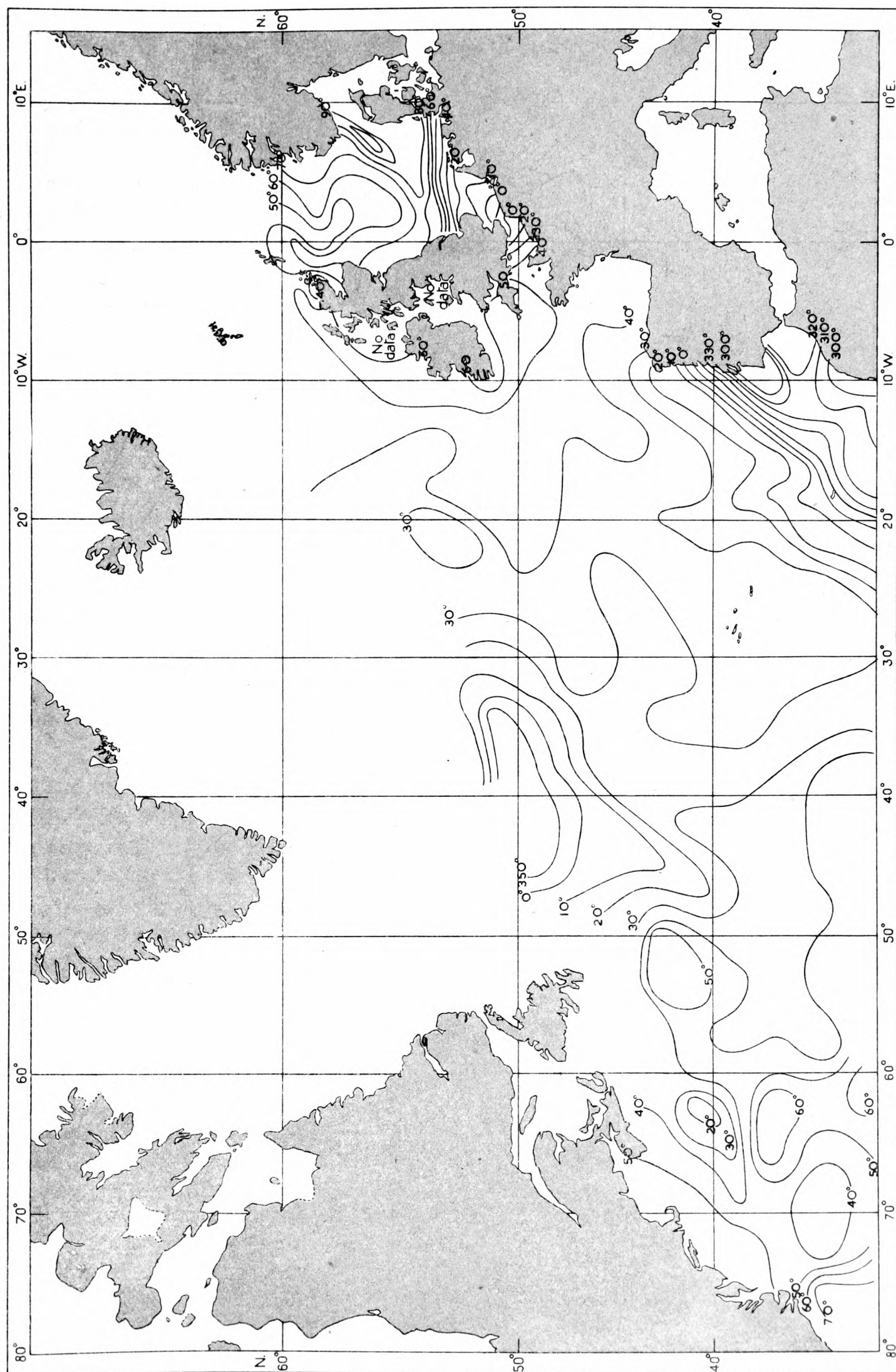
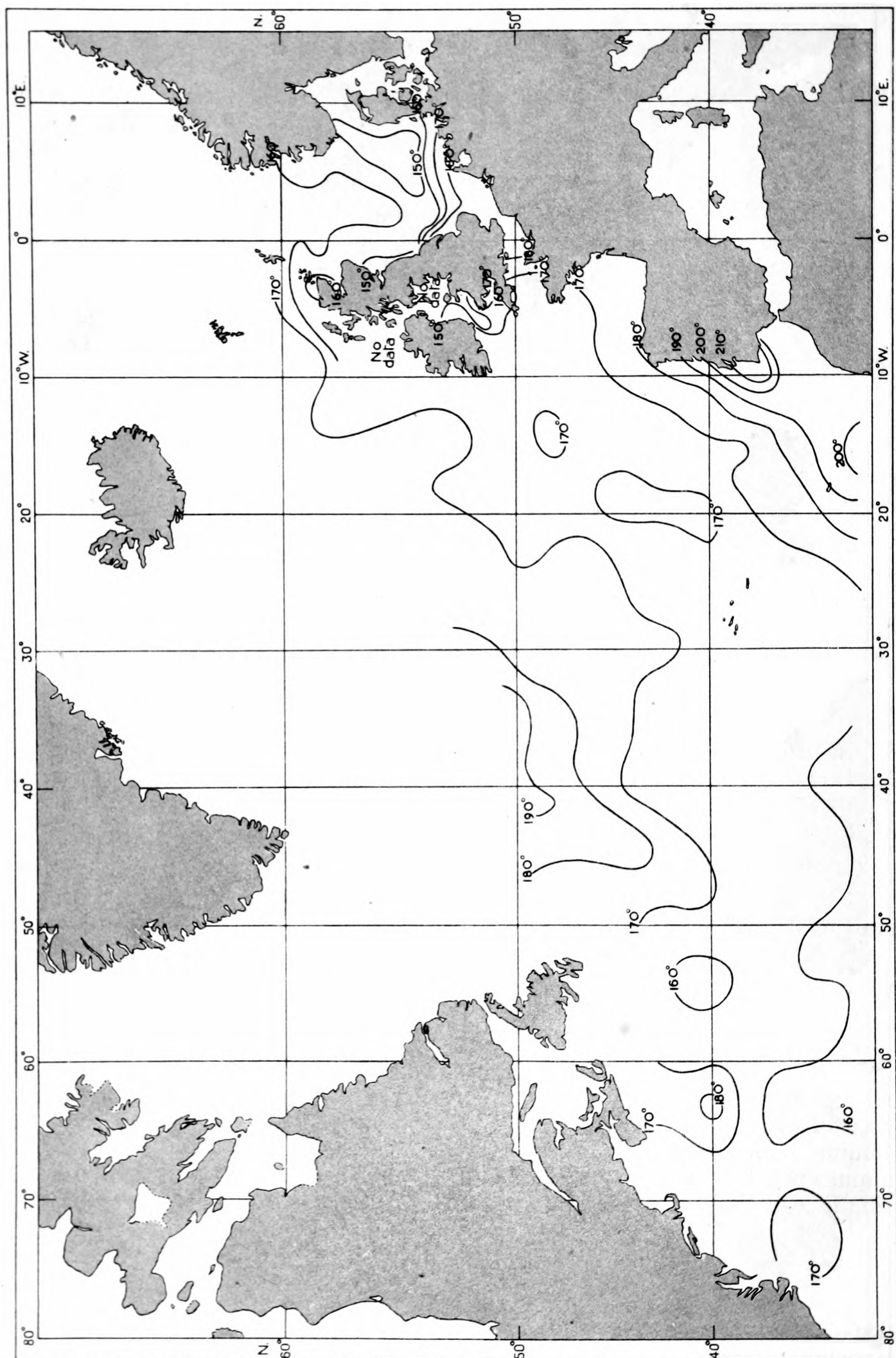


FIG. 9 — DISTRIBUTION OF PHASE OF SEMI-ANNUAL COMPONENT ( $A_2$ )

FIG.10—DISTRIBUTION OF  $F = \frac{1}{2} (2A_1 - A_2 - 90^\circ)$

(iii) There is some evidence of a ridge of high values extending south-west from the British Isles.

*Phase of semi-annual component.* The phase angle of the semi-annual component ( $A_2$ ) modifies the times of maximum and minimum values determined primarily by  $A_1$ . Fig. 9 shows the following main features :—

(i) A belt of relatively high values extends from the British Isles south-westward to the Azores and thence westward to the American continent.

(ii) Low values occur in the upwelling areas off the coasts of Portugal and Morocco and in the region centred at  $50^\circ$  N.,  $40^\circ$  W.

(iii) Both high and low values occur in the North Sea, where the distribution is complex.

If the semi-annual component is regarded as modifying the annual component then some method of representing its phase relative to that of the annual component must be found. The maximum value of the annual component is given by

$$t_1 + A_1 = 360^\circ + 90^\circ.$$

The maximum value of the second component is given by

$$2t_2 + A_2 = 360^\circ + 90^\circ.$$

Therefore,

$$t_2 - t_1 = \frac{1}{2} (2A_1 - A_2 - 90^\circ) - 180^\circ.$$

Denoting by  $F$  the quantity  $\frac{1}{2} (2A_1 - A_2 - 90^\circ)$ , then when  $F = 180^\circ$  the maxima of the two components occur at the same time. At the time of minimum value of the annual component, however, the semi-annual component is then a maximum and is thus completely out of phase.

*Function  $F$ .*—The distribution of function  $F$ , given in Fig. 10, shows :—

(i) All values are relatively close to  $180^\circ$ . This means that the semi-annual component reinforces the annual component at its maximum value and weakens the annual component at its minimum value. The physical significance of this will be dealt with later.

(ii) Values greater than  $180^\circ$  occur in the upwelling areas off the coasts of Portugal and Morocco and also in an area centred about  $50^\circ$  N.,  $40^\circ$  W.

(iii) Low values, less than  $180^\circ$ , occur in a relatively uniform belt extending from the British Isles south-westward to the Azores and thence westward to the American continent. The lowest values occur in an irregular belt extending across the southern half of the North Sea, particularly in the south-east.

At this stage the significance of a value of  $F$  differing from  $180^\circ$  may be noted. When  $F$  is less than  $180^\circ$  the time of occurrence of the maximum value of the annual variation is brought forward and the time of occurrence of the minimum value is set back or retarded. The time interval between minimum and maximum for increasing temperature is therefore less than the time interval for decreasing temperature. When  $F$  is greater than  $180^\circ$ , the time of occurrence of the maximum value of the annual variation is set back or retarded and the time of occurrence of the minimum value is brought forward. The time interval between minimum and maximum for increasing temperature is therefore greater than the time interval for decreasing temperature.

## § 5—THEORETICAL CONSIDERATIONS

In previous sections the facts of the process of seasonal change have been set out in terms of the harmonic parameters and their distribution in space. The physical factors concerned in

determining the seasonal variation of sea-surface temperature are :—

- (i) Total incoming radiation (direct and diffuse).
- (ii) Exchange of heat between ocean and atmosphere.
- (iii) Vertical transfer of heat in the ocean (convection and upwelling).
- (iv) Horizontal transport of heat by ocean currents.

*Total incoming radiation* for certain ocean areas has been given by Kimball<sup>3</sup>, taking account of the effect of variations in the amount of cloudiness and of the distribution of water vapour in the atmosphere. His data are given in Table I.

TABLE I—AVERAGE DAILY TOTAL OF SOLAR RADIATION (DIRECT + DIFFUSE) RECEIVED ON A HORIZONTAL SURFACE taken at the 21st of each month

	Jan.	Feb.	Mar.	Apr.	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.
° N. ° W.	<i>gramme calories per square centimetre</i>											
56 7	50	109	206	308	372	389	328	229	182	107	49	..
52 10	74	146	228	331	378	383	354	288	212	140	80	54
48 60	114	206	270	345	397	424	422	364	284	165	108	78
48 4	94	157	259	339	414	405	388	335	255	153	90	71
42 66-70	139	223	327	402	449	477	421	376	317	235	153	120
36 6	225	280	378	472	498	522	538	496	371	285	225	196
30 65-77	212	247	365	420	462	441	432	399	326	259	244	197
30 15	306	364	415	482	476	482	449	437	420	340	301	281

TABLE II—HARMONIC ANALYSIS OF THE DATA OF TABLE I

	$a_1'$	$A_1'$	$a_2'$	$A_2'$
° N. ° W.	gm. cal./m. <sup>2</sup>	°	gm. cal./m. <sup>2</sup>	°
52 10	166	310	11	261
48 60	172	306	18	26
48 4	175	307	7	309
42 66-70	172	301	36	316
36 6	174	304	13	21
30 65-77	130	310	15	271
30 15	98	313	11	320

Table II suggests that  $a_1'$ , the annual amplitude of the total incoming radiation, reaches a maximum in a latitude between 36° N. and 48° N. and decreases to north and south, the decrease towards the equator being particularly rapid. Table II also suggests that  $A_1'$  has only a small latitudinal variation. If this can be regarded as real, values increase to both north and south of the minimum value in latitude 42° N. However, owing to the large differences of longitude the interpretation of the data is doubtful. Values of  $a_2'$  and  $A_2'$  appear to be too scattered to permit of generalization with respect to latitude.

While sea-surface temperature cannot be regarded as determined solely by radiation income, it is nevertheless significant that the amplitude of the yearly component of the radiation income has a latitudinal maximum corresponding to the latitudinal belt of maximum values of  $a_1$  shown in Fig. 4.



Sverdrup<sup>4</sup> has stated that whereas in the southern hemisphere the latitudinal variation of the annual range of sea-surface temperature appears to be closely connected with that of the radiation income, no such correspondence is evident in the North Atlantic. This rather anomalous result he explains by the effect of the greater distribution of land in the northern hemisphere permitting the cooling of the seas by outbursts of cold continental air in winter. In reaching this conclusion, however, Sverdrup used values for different latitudes averaged over all longitudes of the oceans. It is easily appreciated from Fig. 4 how this procedure must necessarily mask the effect of the radiation income. The present results on the other hand demonstrate the influence of the radiation income outside coastal areas in the North Atlantic. Near the coasts the effects of other factors are sufficiently great to mask that of the radiation income.

*Exchange of heat between ocean and atmosphere.*—Although it has been shown that the effect of radiation income can be traced in the distribution of  $a_1$  it is at once apparent that other factors can be much more effective; for example, the high values of  $a_1$  off the American coast and in the North Sea at once suggest the influence of cold outbreaks of continental air during the winter months. Off the American coast the highest values occur because the wind is predominately from the west. The high values in the North Sea, on the other hand, must be due to the winter occurrence of easterly winds. A full discussion would necessitate examining the major problem of the heat exchange between atmosphere and ocean.

*Vertical transfer of heat in the ocean.*—Convection in the ocean is also of primary importance. When the sea cools in winter the cooling takes place at the surface; the surface layer cools, becomes denser than the water below and hence sinks, warmer water rising by convection to take its place. This warmer water becomes cooled in its turn and is again replaced. Convection, therefore, ensures that the cooling process is not confined to the surface layers but is distributed over a great depth of water. Helland-Hansen<sup>5</sup> has stated that towards the end of the winter isothermal conditions may extend to great depths. In the relatively shallow waters of the continental shelves this isothermal state may be reached relatively early in the winter and then a progressive cooling takes place. In shallow waters, therefore, the annual amplitude tends to be greater than in the open ocean where vast under-water reserves of heat are available to off-set the winter cooling. Although the winter effect is greater, it is worth noting that in summer, too, the shallow waters near the coastline tend to heat up more rapidly than the open sea. Fig. 4, showing the distribution of  $a_1$ , illustrates how the isopleths follow the contours of the continental shelf off the American coast.

There is a fundamental difference between the cooling and heating processes in the ocean. In autumn and winter, as already noted, convection helps to maintain the surface temperature by making available the under-water reserves of heat. In spring and summer, on the other hand, the surface water is warmed, but as the warmer water is less dense than the colder water below there is no tendency for convection and the ocean warms progressively from the surface. The turbulence set up by ocean waves can ensure a certain equalization of temperature near the surface, but the effect of waves becomes negligible at a relatively small depth. As the heating continues a progressively greater stratification of temperature is set up. If the effect on surface temperature of the different characteristics of the cooling and heating processes is considered, it is seen that in winter convection affects the temperature by diminishing its rate of fall and in summer the stratification also affects the temperature by increasing its rate of rise. The effect is to introduce a six-monthly oscillation into the annual variation of the temperature, and it is suggested that the six-monthly component, that has been found, can to some extent be explained in this way. This suggestion is supported by the following considerations. The phase of the second component is such that extreme values are reached very close to the maximum and minimum values of the annual component. Over the greater part of the ocean  $F$  is less than  $180^\circ$ , and, as has already been seen, the effect of the second component is to advance the

maximum value and retard the minimum value. In one of the areas where  $F$  exceeds  $180^\circ$  it is known that upwelling in spring prevents stratification and delays the time of maximum temperature. The amplitude of the six-monthly component is also small in this area.

Turning to the charts showing the distribution of  $a_2$  and  $100 a_2/a_1$ , it is easily seen that there is no definite relation between the amplitudes of the two components. This suggests that the explanation advanced above can only account for a part of the six-monthly component and that other factors are also important. It is obvious, for example, that the distribution of salinity must be taken into account in any full discussion, for density is a function of salinity as well as of temperature.

Vertical transfer can also take place by the process known as upwelling which occurs on steep coasts when the wind blows from a suitable direction. In the northern hemisphere, for example, a wind blowing with a component parallel to the coastline tends to heap up water to the right of its direction; if the wind is blowing with the land to the left of its direction the water is driven away from the coast and upwelling of water at the coastline must then necessarily occur. This process can explain the low values of  $a_1$  and  $a_2$  found off the coasts of Portugal and north-west Africa.

*Horizontal transport of heat by ocean currents.*—A perusal of the charts suggests that the horizontal transfer of heat by ocean currents is of some importance. For example, relatively low values of  $a_1$ , the annual amplitude, are associated with the Gulf Stream and the North Atlantic Current. This effect, however, may, at least in part, be explained by selective convection. The surface waters of the Gulf Stream and the North Atlantic Current have a high salinity which would favour the convection process already discussed. The seasonal change of surface temperature is further complicated by the fact that the strength and position of the ocean currents also vary seasonally.

## § 6—RATE OF CHANGE OF SEA-SURFACE TEMPERATURE

Although the distributions of the harmonic parameters are theoretically sufficient for the discussion of the seasonal variation of sea-surface temperature their practical application is not easy. Of some practical importance would be a knowledge of the rate of change of sea temperature as a function of time and space.

The sea-surface temperature  $T$  at any place can be represented by the expression

$$a_0 + a_1 \sin(t + A_1) + a_2 \sin(2t + A_2)$$

where the harmonic parameters are known. The expression for the rate of change of sea temperature  $\partial T/\partial t$  is, therefore, by differentiation

$$a_1 \cos(t + A_1) + 2a_2 \cos(2t + A_2).$$

Values of this expression can be computed for different values of  $t$  ( $0^\circ, 30^\circ, 60^\circ, \dots, 330^\circ$ ) and the variation of  $\partial T/\partial t$  throughout the year determined. Fig. 11 shows an example, for the  $2^\circ$  square  $30\text{--}32^\circ \text{ N.}, 60\text{--}62^\circ \text{ W.}$ , of the seasonal variation of  $\partial T/\partial t$  compounded from the simple harmonic curves  $a_1 \cos(t + A_1)$  and  $2a_2 \cos(2t + A_2)$ . Notable features of this curve are the high value of  $\partial T/\partial t$  at its maximum and the difference of shape of the crest and trough.

This computation has been made for all the  $2^\circ$  and  $1^\circ$  squares under consideration, and a new series of charts constructed to show the distribution of  $\partial T/\partial t$  for each month of the year. They are given in Fig. 12. The values of  $\partial T/\partial t$ , expressed in degrees Fahrenheit per radian, may for practical purposes be converted into degrees Fahrenheit per month by multiplying by the factor one half.

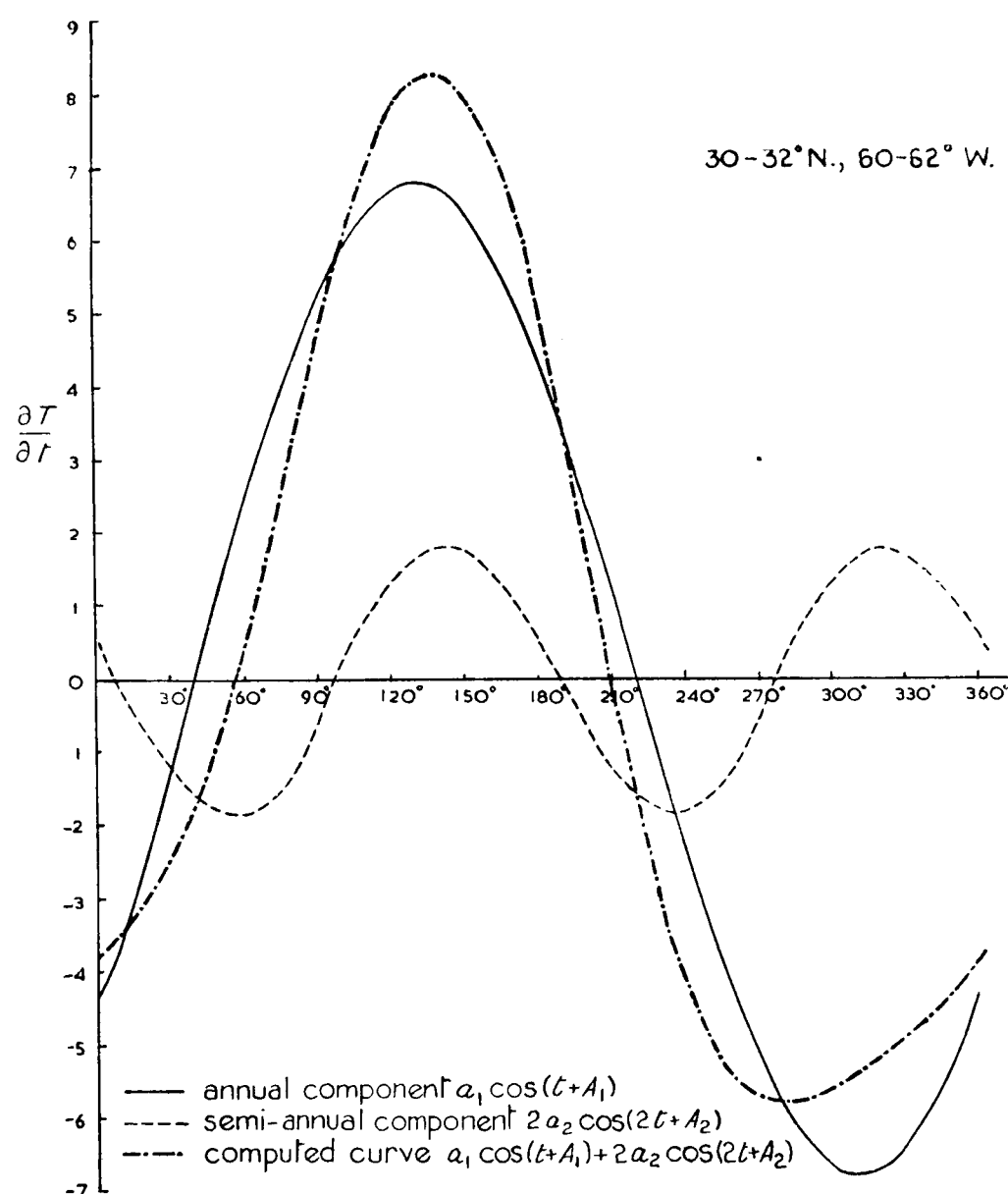


FIG. 11—SEASONAL VARIATION OF  $\partial T/\partial t$   
 Unit :—1° F. per radian where  $2\pi$  radians = 12 months

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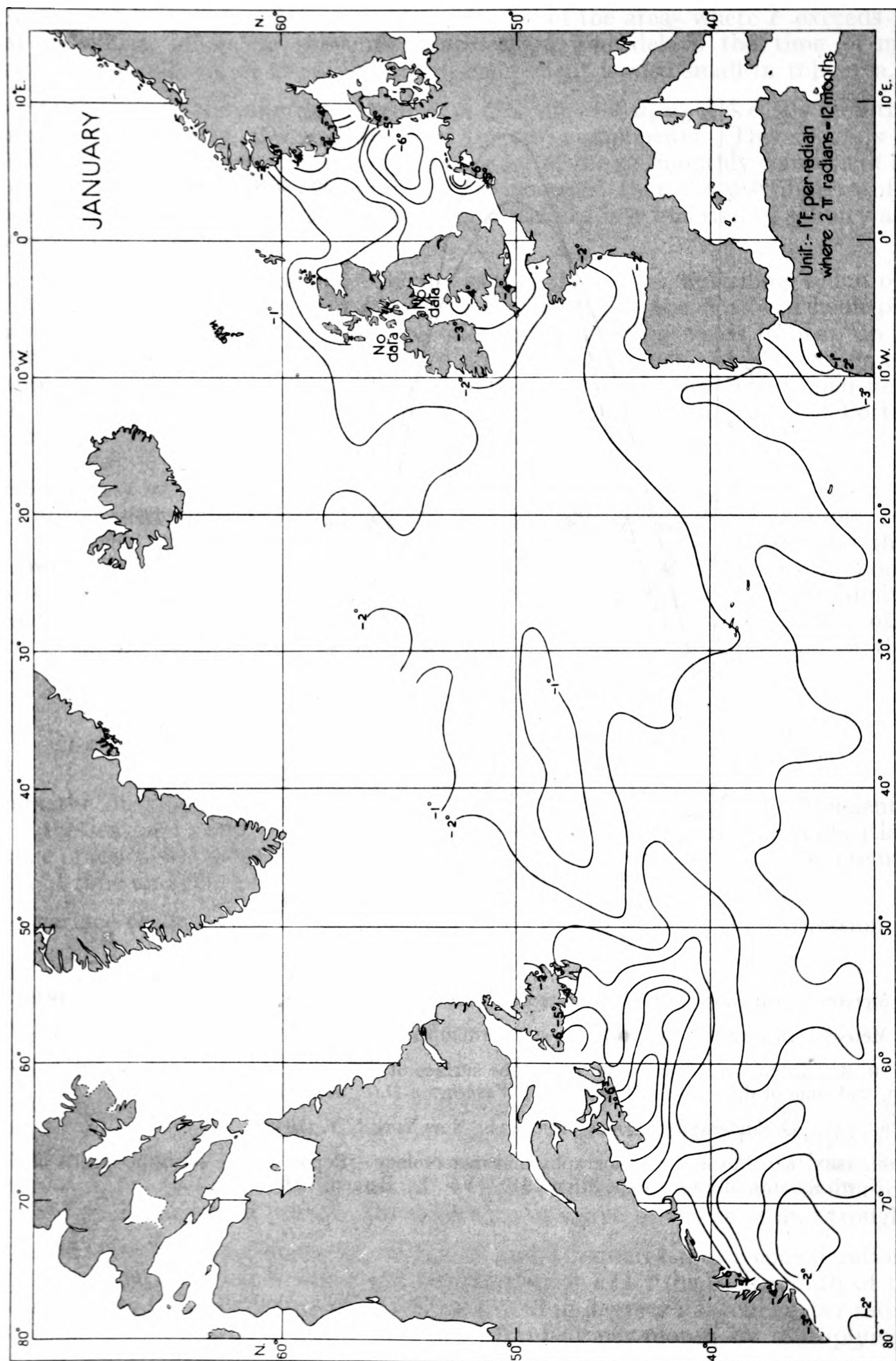


FIG.12—DISTRIBUTION OF RATE OF CHANGE OF MEAN SEA-SURFACE TEMPERATURE



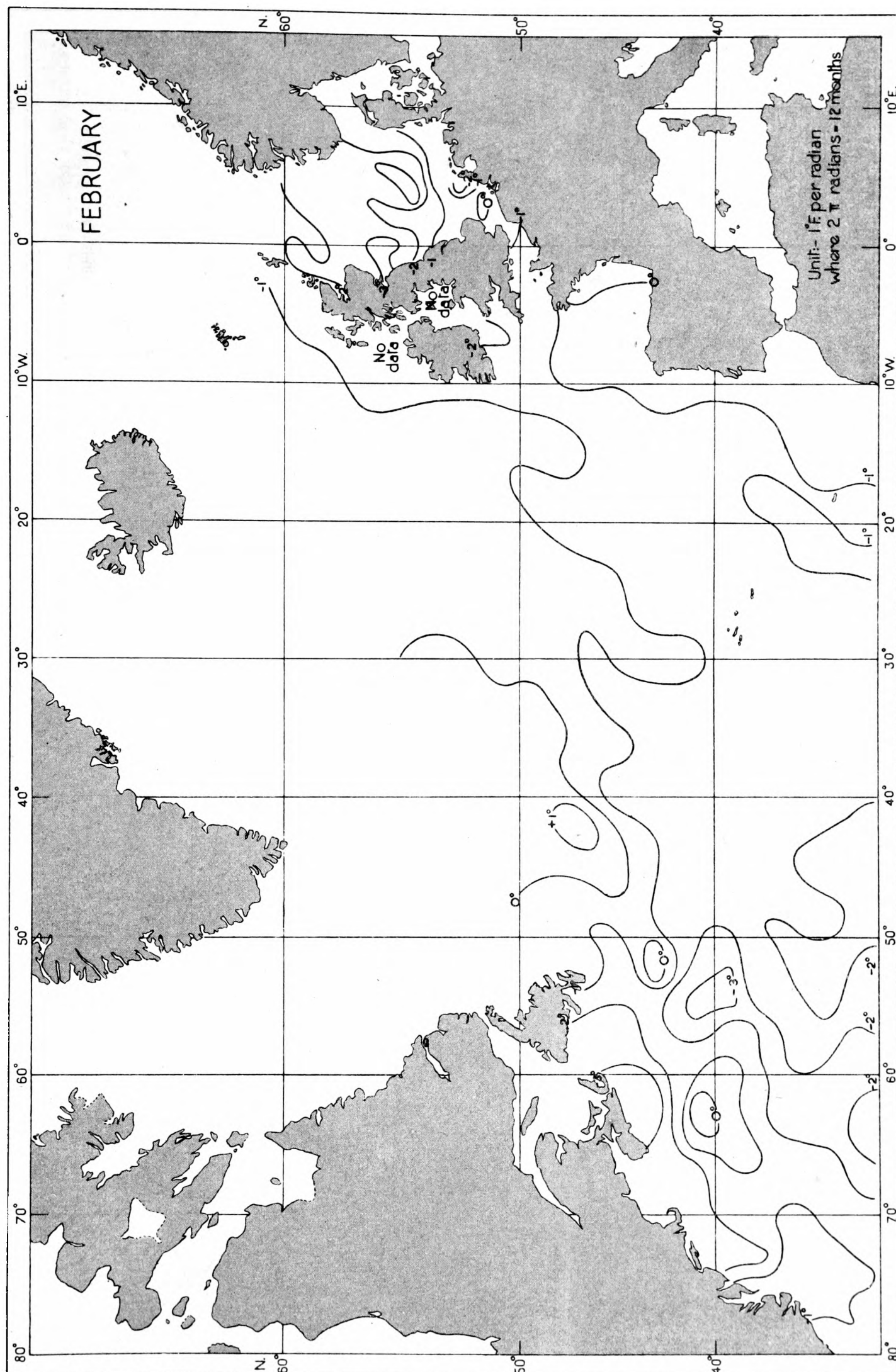


FIG. 12— *continued*

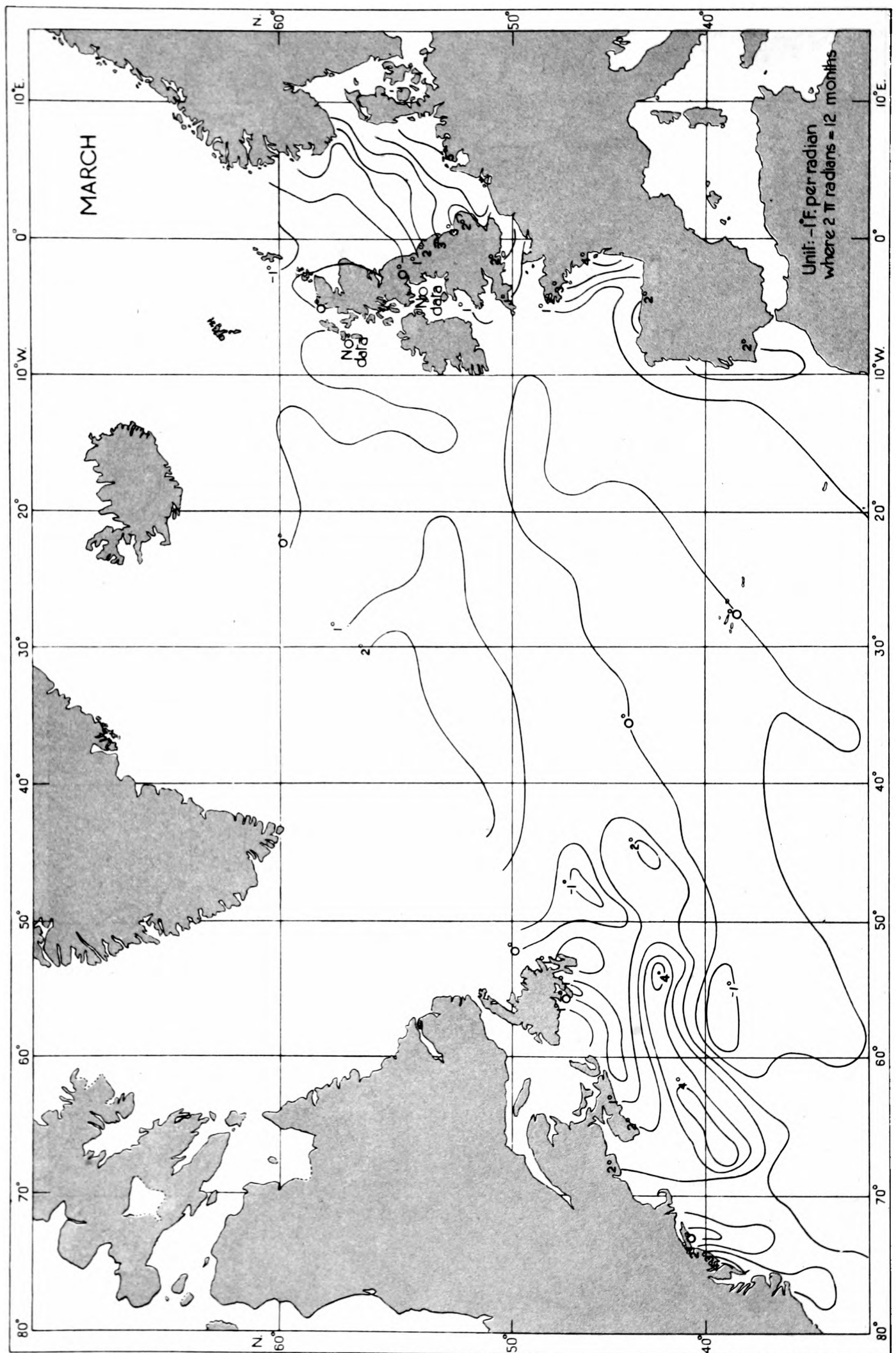


FIG.12 — continued

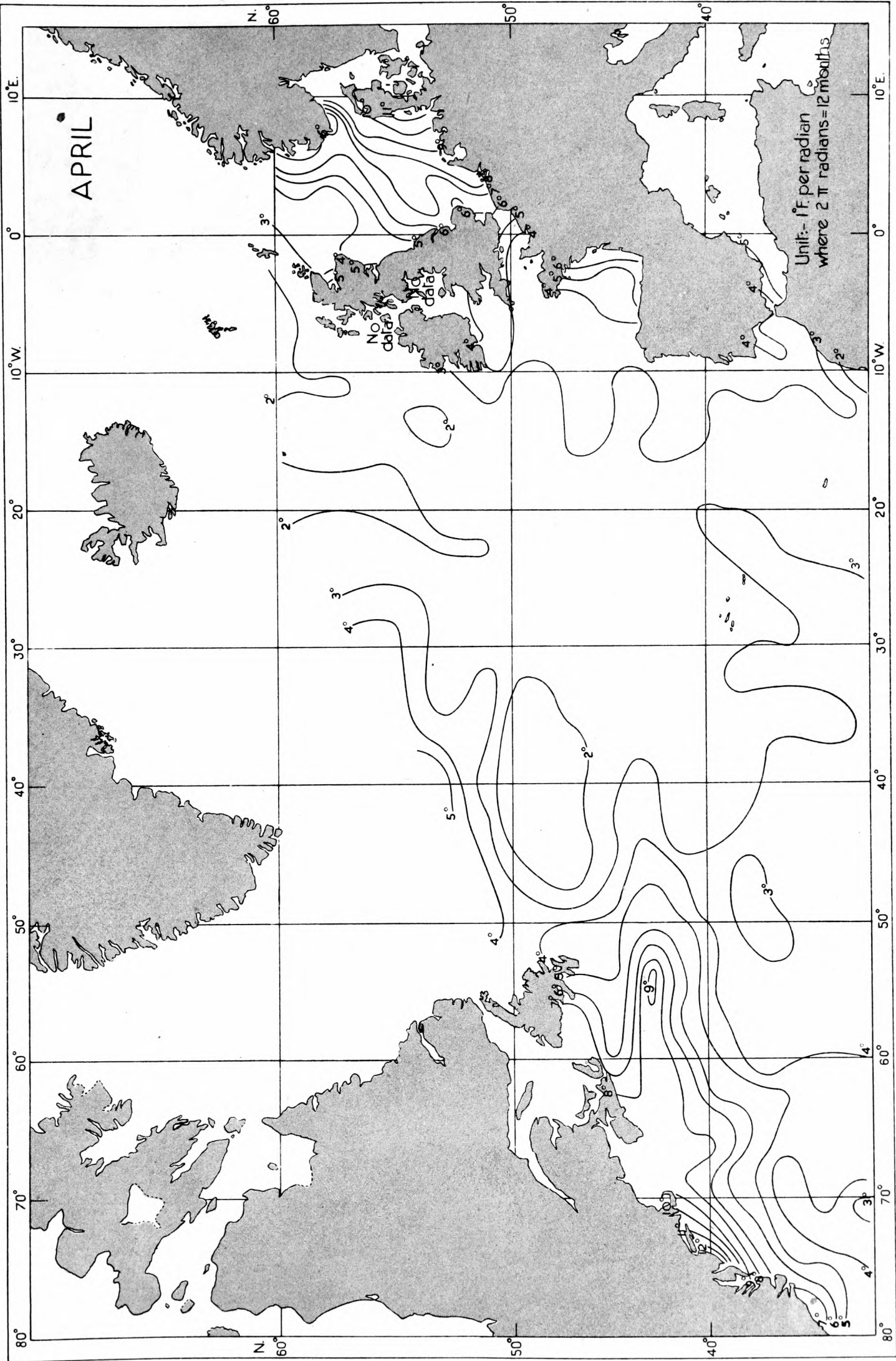


FIG.12 — continued



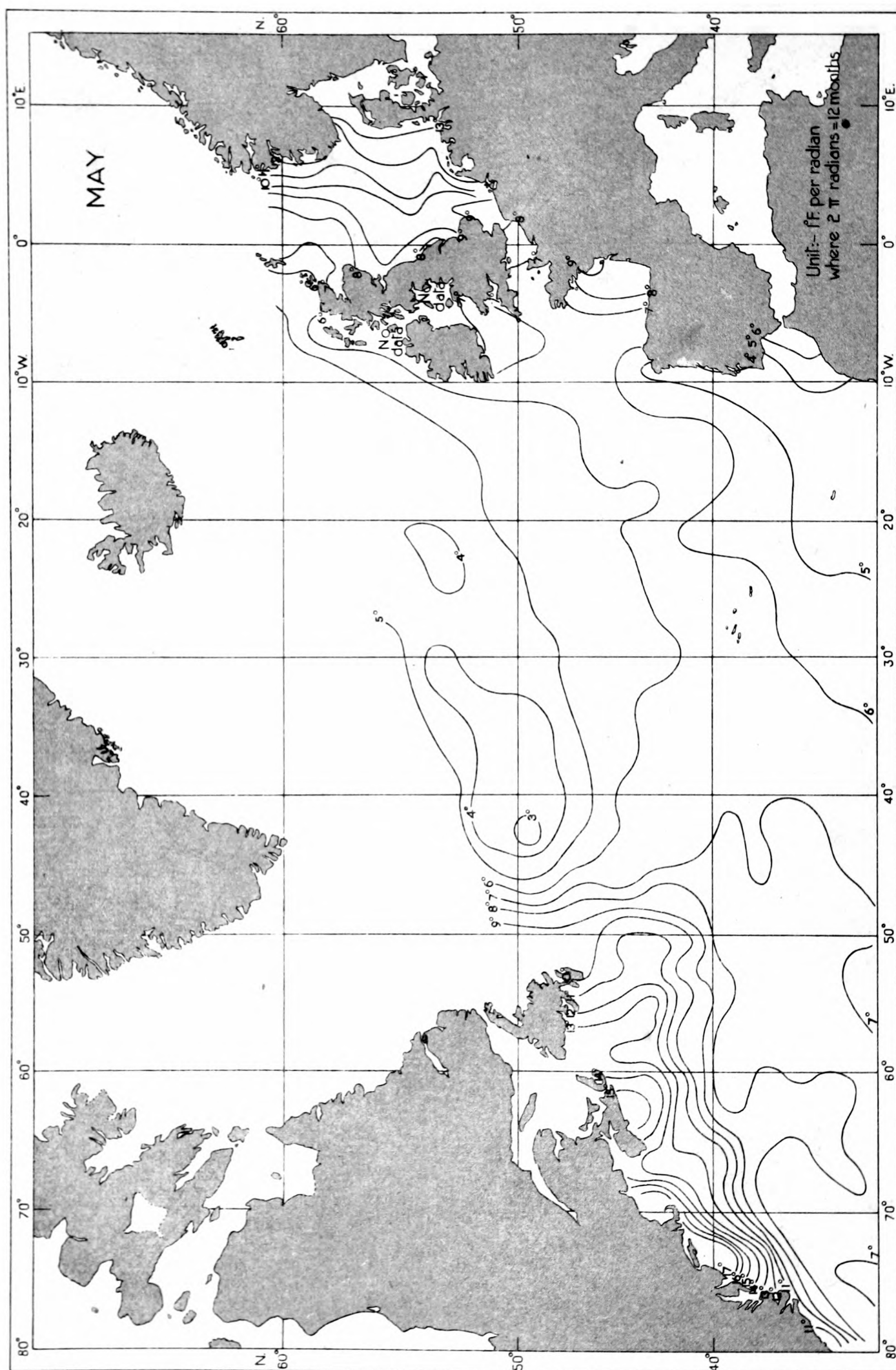


FIG.12— continued

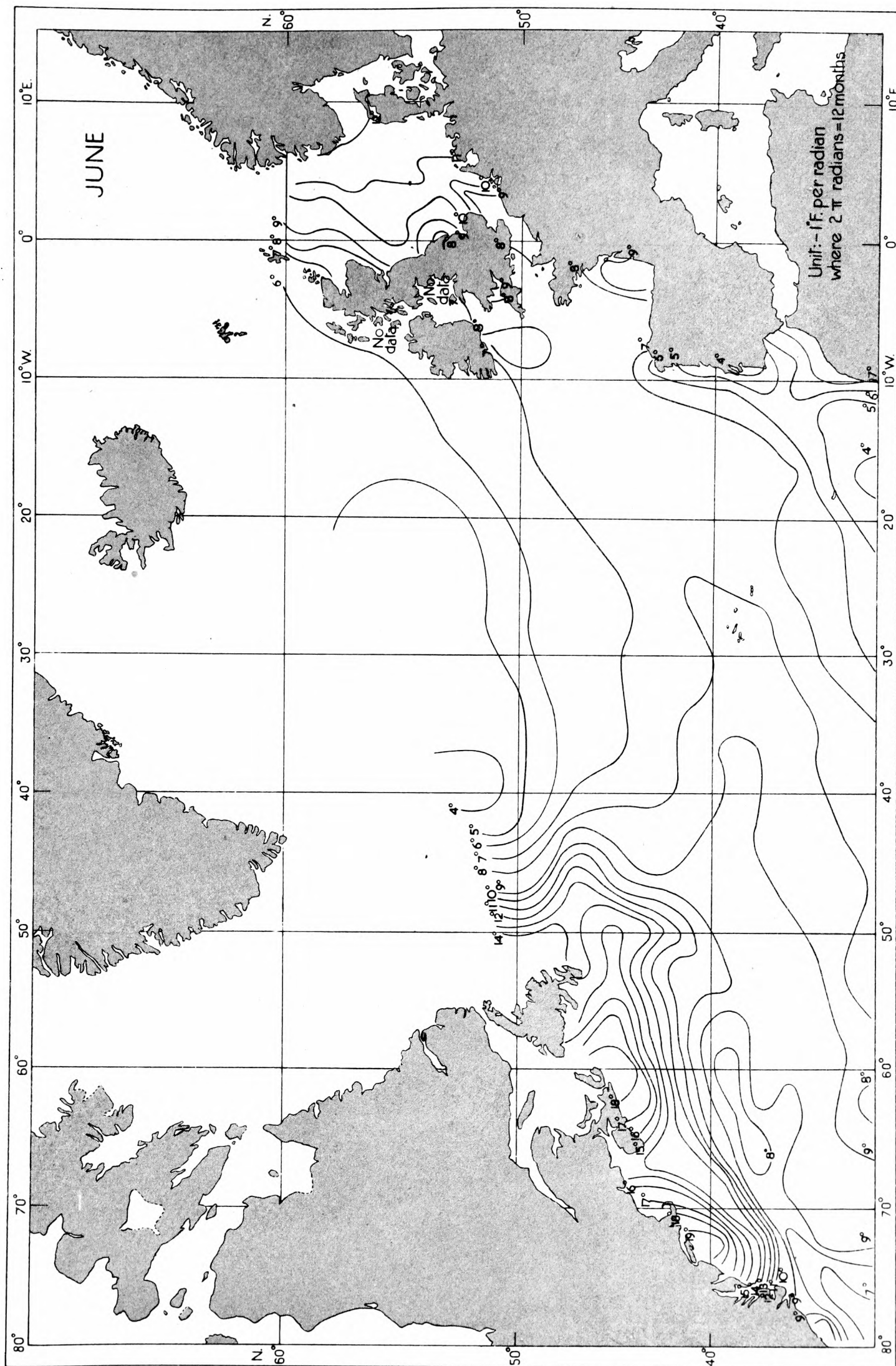


FIG.12— continued

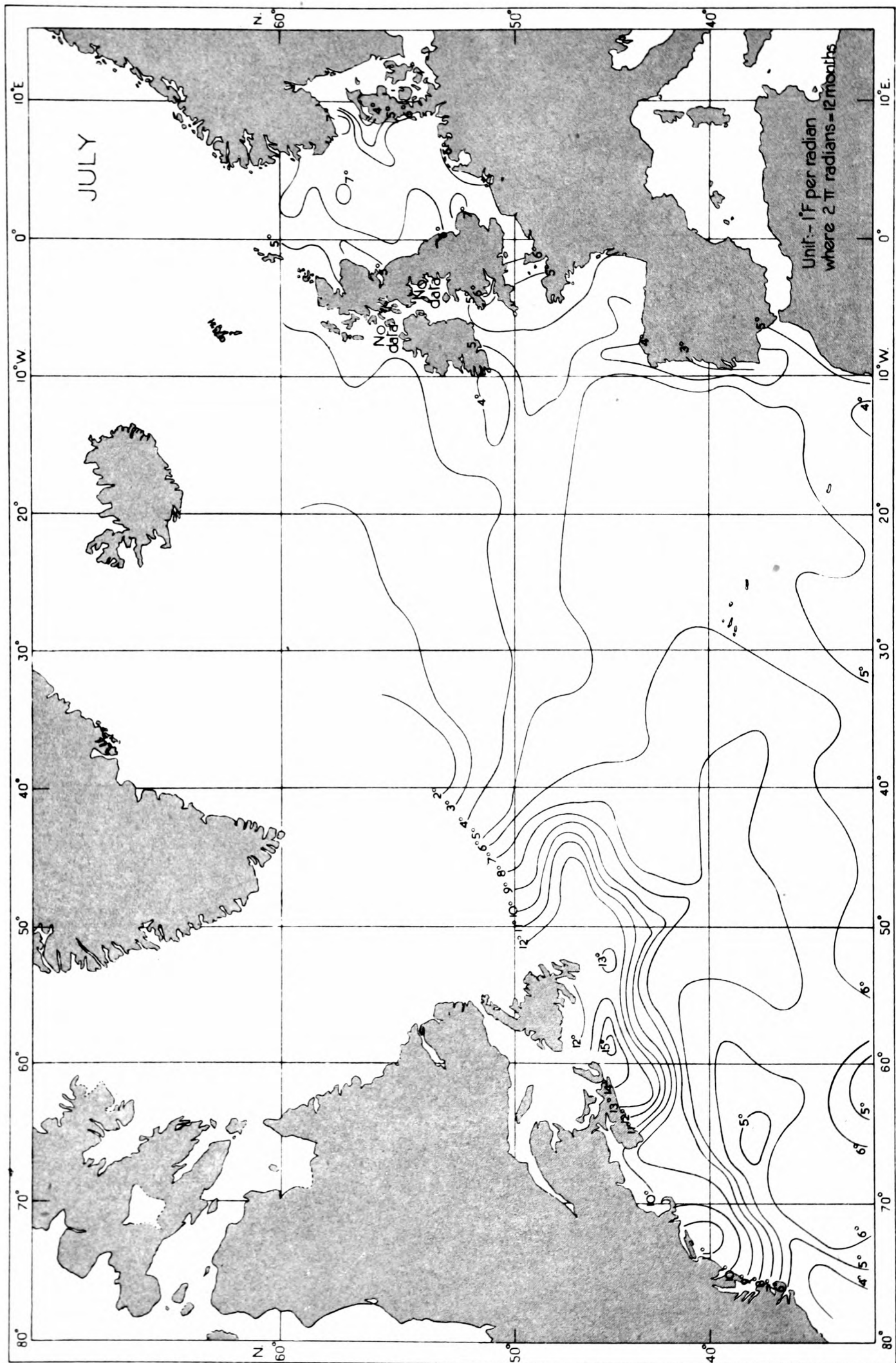


FIG.12— continued



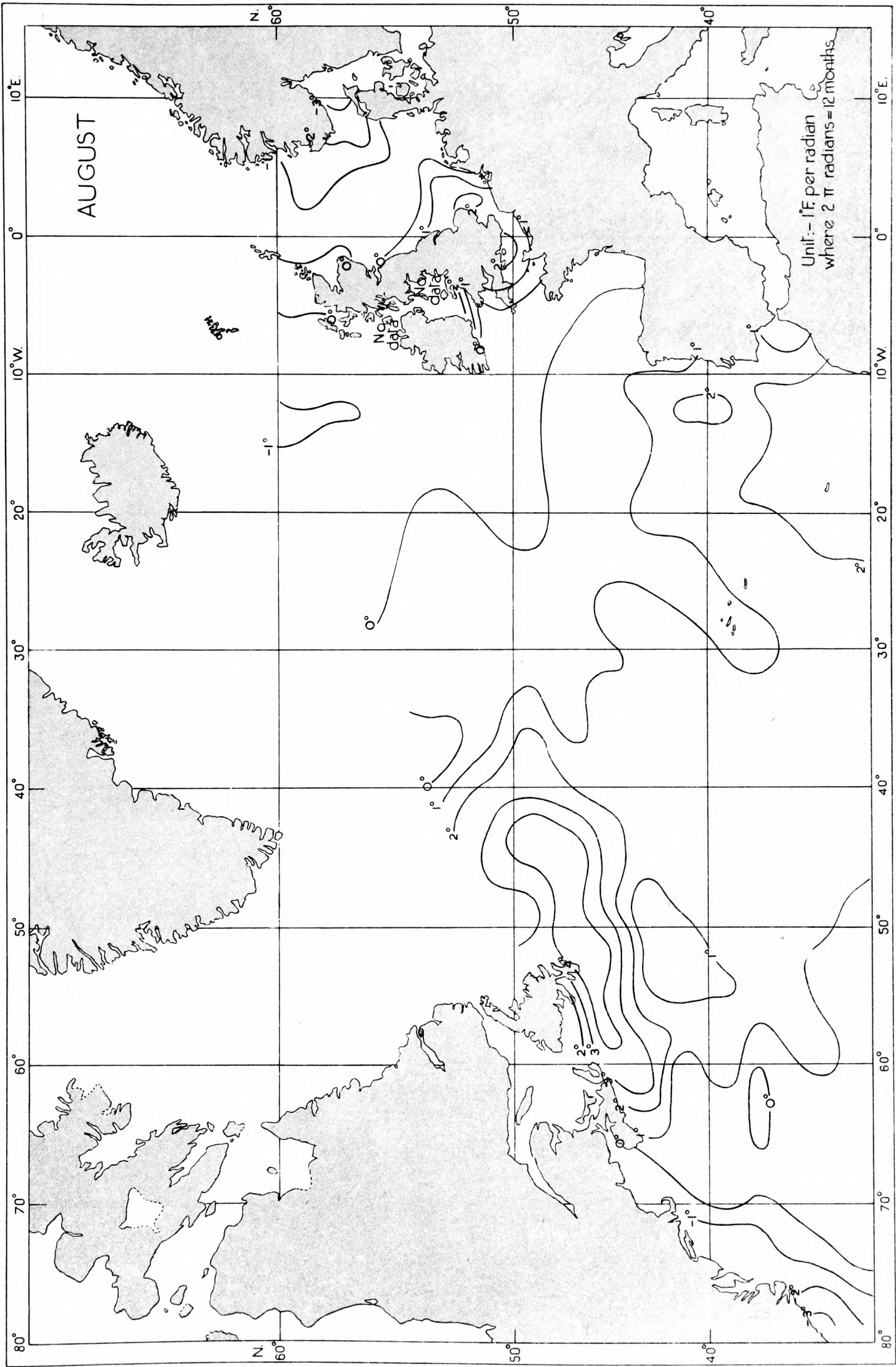


FIG. 12 — continued

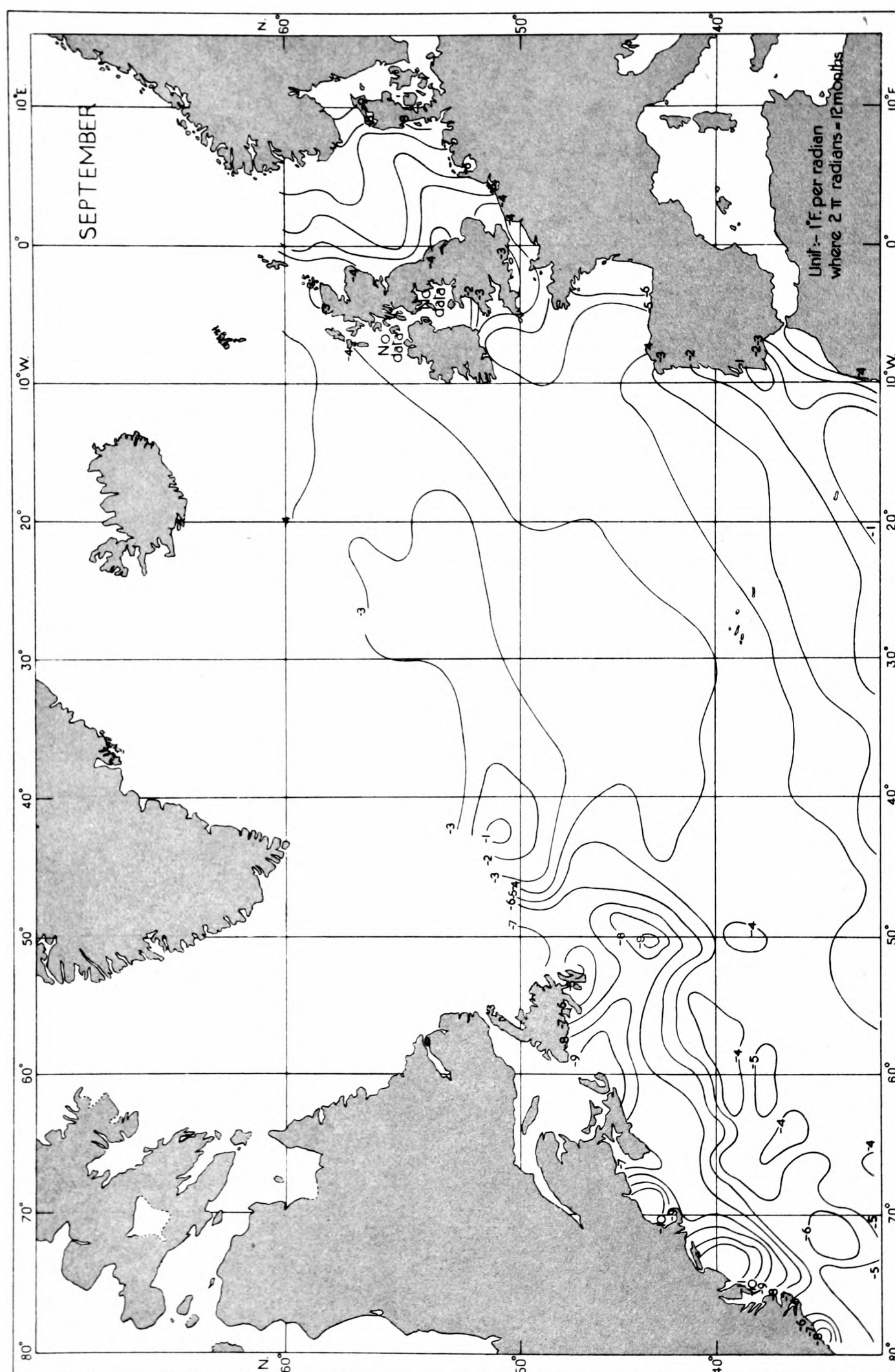


FIG.12 — continued



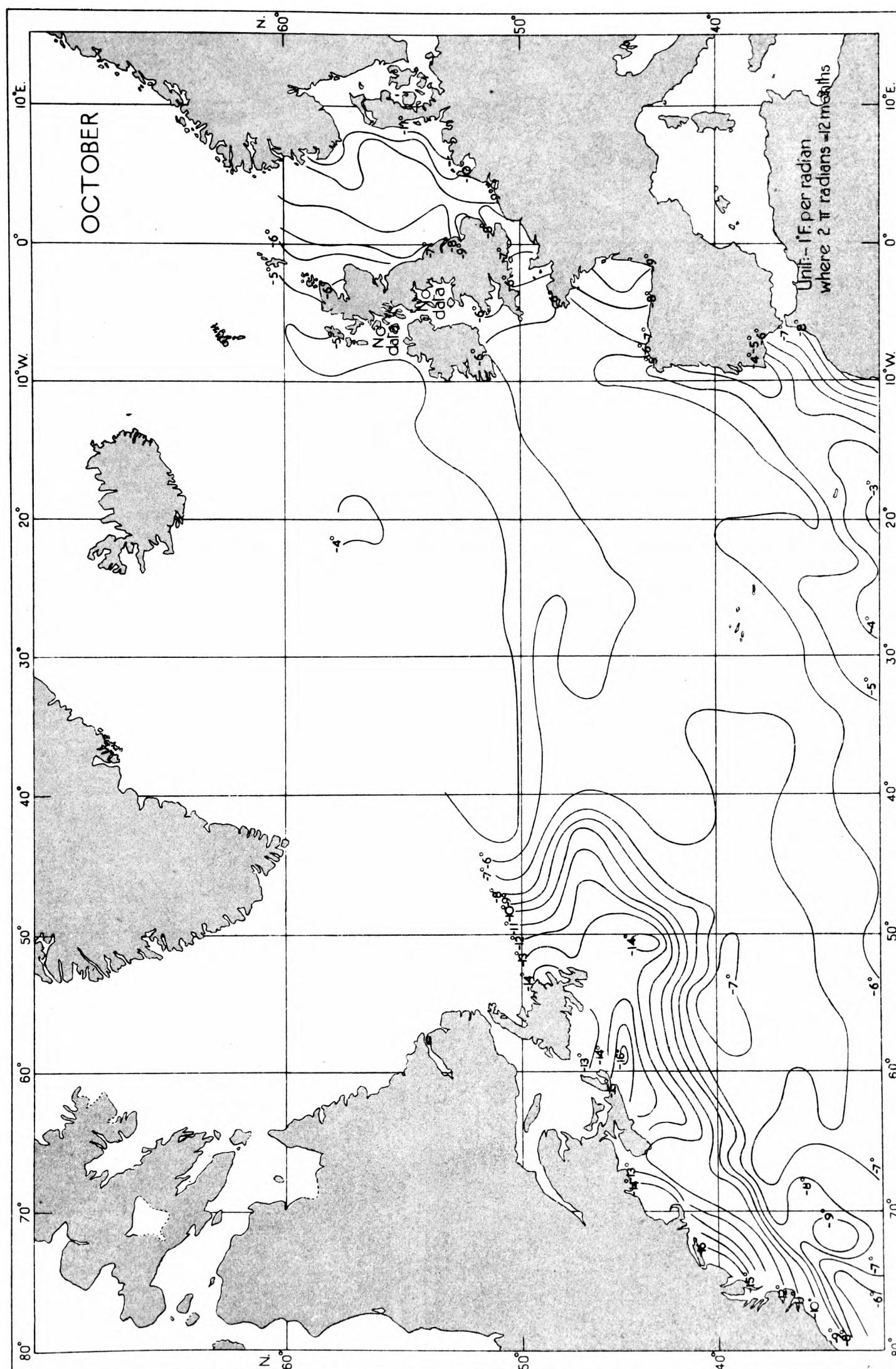


FIG.12 — continued

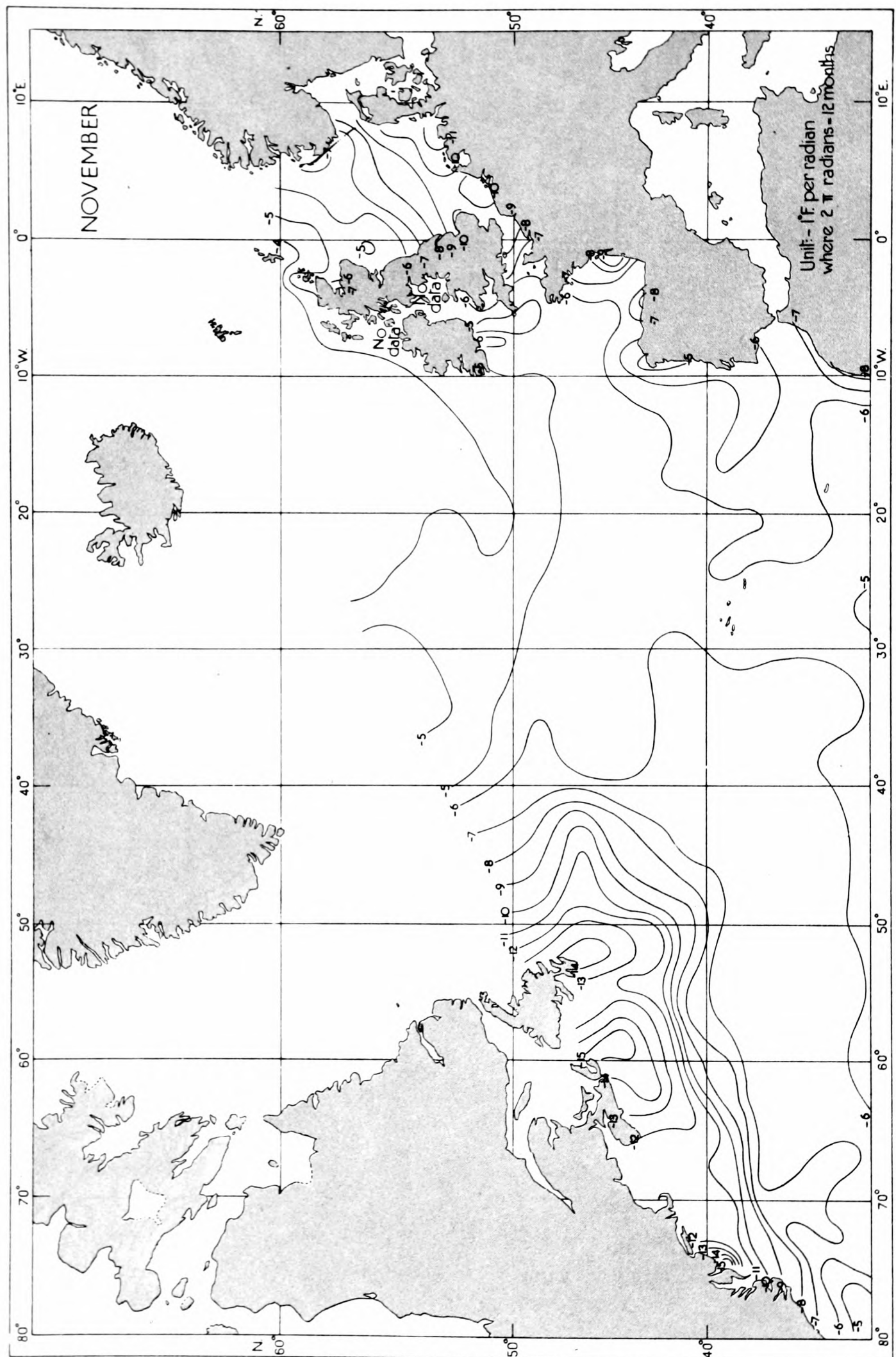


FIG.12— continued

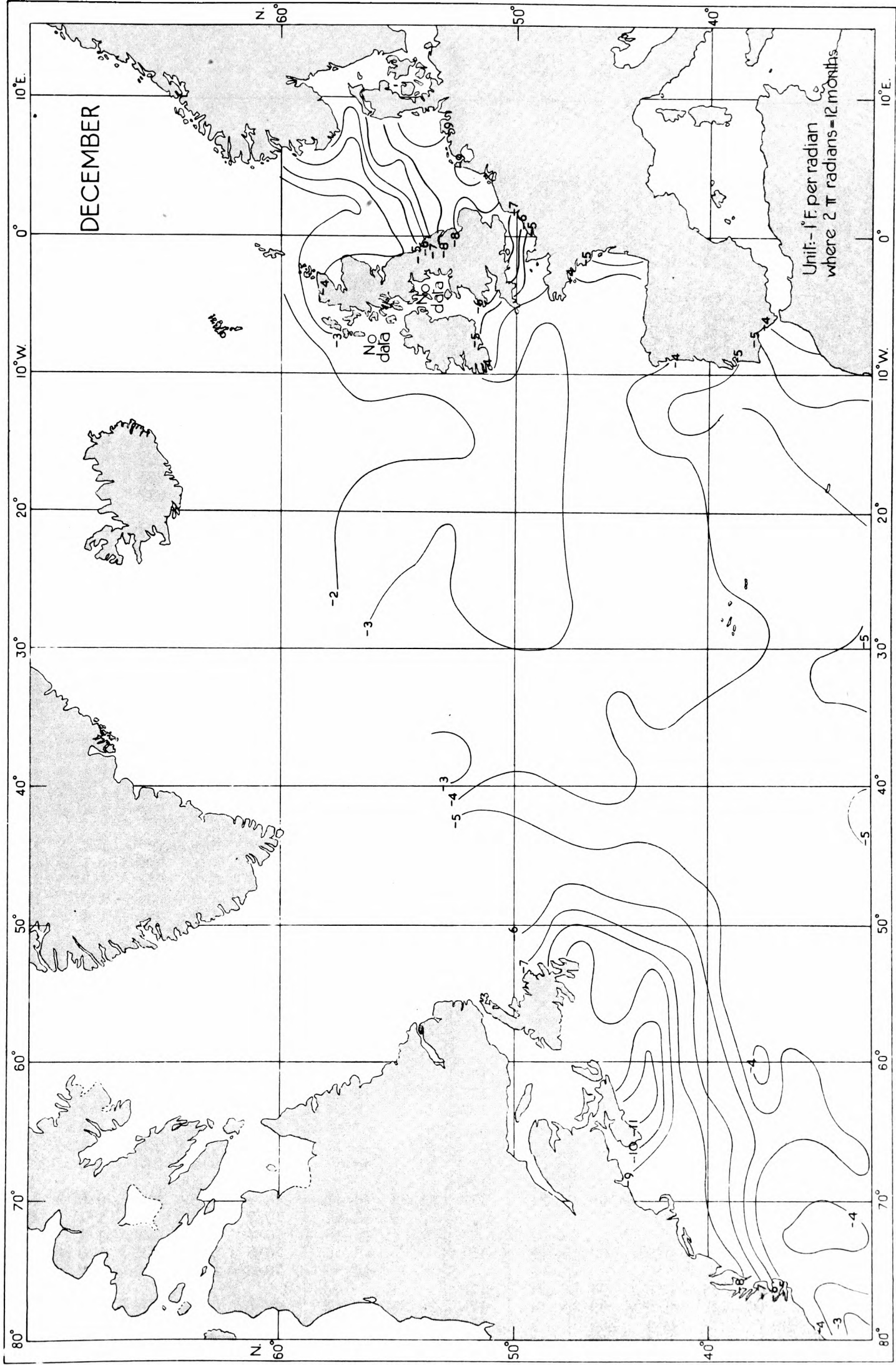


FIG.12 — continued



## APPENDIX—TABULATION OF HARMONIC PARAMETERS

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° W.	° F.	° F.	°	° F.	°		°
Square 109									Square 111— <i>continued</i>								
34-36	00-02	65.5	8.4	240	1.4	51	17	169	36-38	20-22	65.3	6.3	225	0.8	44	13	158
	02-04	64.8	8.3	243	1.9	58	23	169		22-24	65.5	6.2	226	0.7	25	11	169
	04-06	63.5	5.8	236	0.4	26	7	178		24-26	65.5	6.2	228	0.9	34	15	166
	06-08	64.8	6.4	238	1.1	27	17	179		26-28	66.0	6.3	229	1.2	28	19	170
	08-10	65.3	5.9	233	0.8	347	14	195		28-30	66.4	6.1	230	1.3	40	21	165
36-38	00-02	64.8	9.2	238	1.5	22	16	182	38-40	20-22	63.7	5.9	230	1.1	28	19	171
	02-04	63.8	7.8	240	1.3	25	17	183		22-24	63.9	6.1	230	1.0	32	16	169
	04-06	63.2	6.4	235	0.7	34	11	173		24-26	64.7	6.2	229	1.1	30	18	169
	06-08	64.3	6.3	235	0.6	14	10	183		26-28	64.4	6.3	230	1.3	47	21	161
	08-10	62.7	4.8	230	0.4	265	8	233		28-30	64.6	6.3	230	1.3	38	21	166
38-40	08-10	60.9	4.7	232	0.3	270	6	232	Square 112								
30-32	08-10	60.4	7.0	233	1.8	358	26	189	30-32	30-32	70.9	6.1	224	0.4	24	7	167
Square 110										32-34	71.2	6.4	224	0.9	28	14	165
30-32	10-12	66.1	3.6	215	0.5	296	14	202		34-36	71.4	6.0	225	0.9	40	15	160
	12-14	66.9	4.8	222	0.3	330	6	192		36-38	71.9	6.1	227	0.6	53	10	155
	14-16	67.3	4.9	219	0.6	304	12	202	32-34	30-32	69.2	6.2	224	0.5	33	8	163
	16-18	67.9	5.0	220	0.4	319	8	195		32-34	69.8	6.4	223	0.6	22	9	167
	18-20	68.5	5.2	217	0.4	270	8	217		34-36	70.1	6.6	224	1.1	27	17	165
32-34	10-12	66.5	4.7	229	1.2	301	26	213		36-38	70.3	6.4	226	1.0	27	16	167
	12-14	66.3	5.2	222	0.4	319	8	197		38-40	70.6	6.5	227	0.7	63	11	151
	14-16	66.7	5.1	220	0.4	335	8	187	34-36	30-32	68.2	6.2	228	0.8	36	13	165
	16-18	67.1	5.3	224	0.4	315	7	201		32-34	68.5	6.9	226	1.2	31	17	165
	18-20	67.5	5.4	223	0.5	15	9	171		34-36	68.8	6.5	228	1.1	28	17	169
34-36	10-12	65.5	5.6	228	0.6	27	11	169		36-38	69.1	6.8	229	1.2	25	18	171
	12-14	65.5	5.6	223	0.6	330	11	193		38-40	69.6	6.9	226	0.9	31	13	165
	14-16	65.5	5.6	222	0.6	341	11	187	36-38	30-32	66.8	6.6	230	1.2	45	18	163
	16-18	66.1	6.0	225	0.9	15	15	173		32-34	67.0	6.8	228	1.2	37	18	165
	18-20	66.3	6.0	226	0.8	001	13	181		34-36	67.5	6.7	226	1.2	25	18	169
36-38	10-12	63.6	5.2	224	0.3	290	6	214		36-38	68.0	7.0	227	1.4	27	20	169
	12-14	63.9	5.8	222	0.7	342	12	186		38-40	68.2	7.2	229	1.4	20	19	174
	14-16	64.6	6.2	228	1.0	35	16	165	38-40	30-32	65.2	6.4	227	1.2	37	19	163
	16-18	64.8	6.3	227	1.4	13	22	175		32-34	66.1	6.4	228	1.1	45	17	161
	18-20	64.9	6.1	225	1.0	10	16	175		34-36	66.3	6.7	227	1.3	27	19	169
38-40	10-12	62.5	6.0	227	0.5	11	8	177		36-38	67.0	6.9	230	1.5	42	22	164
	12-14	62.6	5.8	225	1.0	355	17	183		38-40	67.3	6.8	226	1.4	27	21	167
	14-16	63.0	6.1	228	1.0	33	16	167	Square 113								
	16-18	63.2	6.2	226	1.0	32	16	165	30-32	40-42	72.1	6.5	225	0.6	58	9	151
	18-20	63.1	6.2	228	1.1	19	18	173		42-44	72.3	6.4	223	0.6	46	9	155
Square 111										44-46	72.6	6.4	225	1.0	38	16	161
30-32	20-22	68.6	5.0	219	0.3	359	6	175		46-48	72.8	6.7	225	1.4	41	21	159
	22-24	68.8	5.3	222	0.8	358	15	178		48-50	73.1	6.7	227	1.0	51	15	157
	24-26	69.3	5.7	224	0.6	47	11	155	32-34	40-42	71.1	6.7	226	0.9	40	13	161
	26-28	69.5	5.3	223	0.2	35	4	161		42-44	71.4	6.9	228	1.2	34	17	166
	28-30	..	..	..	..	..	..	..		44-46	71.6	6.8	227	1.3	42	19	161
32-34	20-22	67.3	5.8	225	1.0	01	17	179		46-48	71.8	7.0	227	1.1	43	16	161
	22-24	67.8	5.3	226	1.1	06	21	178		48-50	72.0	7.2	228	1.0	37	14	165
	24-26	..	..	..	..	..	..	..	34-36	40-42	69.8	7.0	228	0.9	42	13	162
	26-28	..	..	..	..	..	..	..		42-44	70.2	7.2	229	1.1	42	15	163
	28-30	68.7	5.6	226	0.9	60	16	151		44-46	70.4	7.1	228	1.1	44	15	161
34-36	20-22	66.6	5.8	225	0.8	04	14	178		46-48	70.5	7.3	226	1.0	34	14	164
	22-24	66.9	5.9	229	0.8	09	14	179		48-50	70.5	7.0	228	1.2	35	17	165
	24-26	67.2	5.9	228	0.4	50	7	158	36-38	40-42	68.6	7.2	226	1.4	30	19	166
	26-28	67.5	6.1	227	0.9	39	15	163		42-44	69.0	6.8	227	1.2	38	18	163
	28-30	67.6	6.1	226	1.0	13	16	175		44-46	69.5	6.9	225	1.1	34	16	163
										46-48	69.6	7.2	225	1.5	31	21	165
										48-50	69.5	7.2	225	1.4	34	19	163

## APPENDIX—continued

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° W.	° F.	° F.	°	° F.	°		°
Square 113—continued									Square 116								
38-40	40-42	67.5	6.8	225	1.4	36	21	162	30-32	70-72	73.4	7.1	230	1.5	33	21	169
	42-44	68.1	7.2	225	1.5	35	21	163		72-74	74.2	7.4	233	1.6	48	22	164
	44-46	67.9	7.4	228	1.4	30	19	168		74-76	74.6	6.7	237	0.9	27	13	179
	46-48	68.0	7.6	228	1.6	39	21	163		76-78	76.1	6.1	237	0.8	78	13	153
	48-50	68.7	7.3	225	1.2	29	16	165		78-80	77.1	5.8	244	1.1	71	19	163
Square 114									32-34	70-72	70.7	8.1	236	1.8	50	22	166
30-32	50-52	73.6	6.5	228	0.8	56	12	155		72-74	73.1	7.6	237	1.7	30	22	177
	52-54	73.3	6.5	228	0.9	35	14	165		74-76	74.6	6.5	239	0.6	58	9	165
	54-56	73.7	6.6	228	0.9	24	14	171		76-78	75.6	6.7	246	0.8	83	12	159
	56-58	73.6	6.8	227	1.1	43	16	161		78-80	72.5	8.9	245	1.7	72	19	164
	58-60	73.6	6.6	226	1.3	49	20	157	34-36	70-72	71.7	7.3	237	1.4	25	19	179
32-34	50-52	71.9	7.2	226	1.1	42	15	160		72-74	73.3	6.7	241	1.1	38	16	177
	52-54	70.1	6.6	225	1.1	60	17	150		74-76	70.9	8.7	241	1.7	36	20	178
	54-56	71.9	6.7	228	1.6	54	24	156		76-78	72.1	8.3	238	1.1	90	13	148
	56-58	71.8	7.4	230	1.1	38	15	166	36-38	70-72	70.7	8.0	236	1.1	50	14	166
	58-60	71.8	7.6	228	1.3	39	17	163		72-74	65.4	11.0	238	2.3	50	21	168
34-36	50-52	70.6	7.0	226	1.5	45	21	159		74-76	60.0	14.6	242	1.6	51	11	171
	52-54	70.8	7.3	225	1.4	35	19	163	38-40	70-72	60.4	11.7	235	1.8	36	15	172
	54-56	70.7	7.5	227	1.4	35	19	165		72-74	57.3	14.3	234	2.9	62	20	158
	56-58	70.9	7.3	227	1.3	36	18	164		74-76	55.5	16.6	240	1.8	50	11	170
	58-60	70.9	7.4	229	1.1	36	15	166	Square 145								
36-38	50-52	69.8	7.2	227	1.2	20	17	172	40-42	08-10	60.4	4.9	234	0.2	350	4	194
	52-54	69.8	7.2	228	1.3	28	18	169	42-44	02-04	60.1	7.6	241	1.4	49	19	171
	54-56	70.2	6.9	227	1.3	31	19	167		04-06	58.9	7.4	240	0.7	5	9	193
	56-58	70.2	7.2	227	1.3	40	18	162		06-08	58.8	6.4	242	1.1	35	17	179
	58-60	70.7	7.1	230	1.4	51	20	159		08-10	58.9	5.0	234	0.5	36	10	171
38-40	50-52	69.1	7.2	225	1.1	39	15	161	44-46	00-02	57.4	8.9	246	0.7	340	8	211
	52-54	69.0	7.5	223	1.4	48	19	154		02-04	58.7	8.0	241	1.6	45	20	173
	54-56	69.4	7.3	226	1.6	56	22	153		04-06	59.3	6.6	231	0.6	60	9	156
	56-58	69.7	7.4	227	0.8	30	11	167		06-08	57.9	6.3	235	1.0	38	16	171
	58-60	69.7	7.3	230	0.7	20	10	175		08-10	58.4	6.1	235	1.0	30	16	175
Square 115									46-48	00-02	57.4	8.5	248	1.0	54	12	176
30-32	60-62	73.4	6.8	230	0.9	72	13	149		02-04	56.4	7.5	250	1.0	42	13	184
	62-64	73.6	6.9	233	0.8	63	12	157		04-06	56.1	6.1	238	1.2	42	20	172
	64-66	73.0	6.9	233	1.0	52	14	162		06-08	56.8	6.0	235	1.1	40	18	170
	66-68	73.5	7.7	227	0.9	44	12	160		08-10	56.9	5.8	235	1.0	39	17	171
	68-70	73.6	7.6	229	1.2	48	16	160	48-50	00-02	53.2	6.7	229	1.1	40	16	164
32-34	60-62	72.2	7.7	231	1.1	50	14	161		02-04	53.9	6.1	227	0.5	45	8	159
	62-64	72.0	7.8	230	1.2	57	15	157		04-06	54.5	5.7	235	1.0	62	18	159
	64-66	72.1	7.7	229	1.0	53	13	157		06-08	54.9	6.3	237	1.4	55	22	165
	66-68	72.9	7.7	230	1.3	41	17	165		08-10	55.3	6.0	237	1.4	45	23	169
	68-70	72.3	7.8	230	1.0	28	13	171	Square 146								
34-36	60-62	70.9	7.4	228	1.0	48	14	159	40-42	10-12	61.0	5.9	230	0.4	17	7	175
	62-64	71.4	7.3	230	0.8	67	11	151		12-14	61.3	6.3	229	1.1	26	17	171
	64-66	71.1	7.6	228	0.7	47	9	159		14-16	61.4	6.4	228	1.0	31	15	169
	66-68	70.7	7.3	232	1.2	45	16	165		16-18	61.5	6.6	231	1.3	30	20	171
	68-70	71.1	7.4	231	1.6	35	22	169		18-20	62.0	6.2	228	1.1	39	18	163
36-38	60-62	70.8	7.1	232	1.4	50	20	162	42-44	10-12	59.5	5.8	230	0.9	17	16	177
	62-64	71.0	7.7	235	1.2	65	16	157		12-14	59.9	6.1	228	1.2	31	20	167
	64-66	71.3	7.6	235	0.6	75	8	153		14-16	60.3	6.3	231	1.0	45	16	163
	66-68	71.9	7.4	236	0.4	70	5	156		16-18	60.5	6.1	229	1.1	34	18	167
	68-70	72.1	7.3	234	0.9	49	12	165		18-20	60.5	5.8	230	1.3	23	22	167
38-40	60-62	69.3	7.7	235	0.7	..	9	..									
	62-64	69.3	8.0	233	0.5	17	6	179									
	64-66	67.8	9.7	239	0.7	26	7	181									
	66-68	65.2	11.0	235	0.4	..	4	..									
	68-70	64.0	10.5	234	1.5	28	14	175									

APPENDIX—*continued*

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° W.	° F.	° F.	°	° F.	°		°
Square 146— <i>continued</i>									Square 148— <i>continued</i>								
44-46	10-12	58.4	6.3	229	1.1	35	17	167	44-46	30-32	61.0	5.6	230	1.2	31	21	169
	12-14	58.7	6.2	232	1.1	46	18	164		32-34	60.8	5.6	228	1.0	15	18	175
	14-16	58.7	5.8	232	1.2	46	21	164		34-36	60.6	5.8	228	0.8	26	14	170
	16-18	58.9	5.8	232	1.1	32	19	171		36-38	60.7	5.7	230	1.0	14	18	178
	18-20	59.2	5.7	232	1.1	31	19	171		38-40	60.9	6.0	225	1.2	38	20	161
46-48	10-12	57.1	5.8	234	1.1	44	19	167	46-48	30-32	58.2	5.4	234	0.9	44	17	167
	12-14	57.2	5.8	233	0.9	46	16	165		32-34	57.9	5.2	232	1.1	39	21	167
	14-16	57.5	5.8	234	1.0	35	17	171		34-36	58.0	5.3	235	1.1	19	21	181
	16-18	57.6	5.6	233	1.0	38	17	169		36-38	58.1	5.3	234	1.4	25	26	177
	18-20	57.9	5.4	231	1.3	32	24	170		38-40	58.3	5.3	230	1.3	19	25	175
48-50	10-12	55.7	5.4	234	1.4	46	26	166	48-50	30-32	55.8	5.1	235	1.0	20	20	180
	12-14	56.0	5.2	237	1.4	35	27	175		32-34	55.4	4.7	236	1.2	15	25	183
	14-16	56.3	4.8	243	1.7	44	35	176		34-36	55.3	4.7	235	1.3	356	28	192
	16-18	56.4	5.2	235	1.1	50	21	165		36-38	55.7	4.8	229	1.1	351	23	189
	18-20	56.9	5.0	236	1.2	47	24	167		38-40	55.3	5.2	227	1.1	353	21	185
Square 147									Square 149								
40-42	20-22	62.4	6.0	231	1.0	13	17	179	40-42	40-42	65.9	6.4	229	1.1	26	17	171
	22-24	62.5	5.9	230	1.2	38	20	166		42-44	65.8	6.1	227	1.3	36	21	164
	24-26	62.7	6.2	230	1.3	31	21	169		44-46	65.6	6.8	228	1.4	38	21	164
	26-28	62.9	6.2	232	1.2	43	19	165		46-48	64.1	8.1	229	0.8	360	10	166
	28-30	63.0	6.0	228	1.3	22	22	172		48-50	61.8	8.9	230	1.4	24	16	173
42-44	20-22	60.6	6.2	229	1.1	36	18	166	42-44	40-42	63.3	6.6	228	1.0	38	15	164
	22-24	61.0	6.2	230	1.1	41	18	165		42-44	63.5	6.8	229	1.0	20	15	174
	24-26	61.5	5.9	230	1.2	34	20	168		44-46	62.4	7.5	231	0.6	350	8	191
	26-28	61.8	5.6	226	1.2	29	21	167		46-48	57.4	8.5	232	1.2	31	14	171
	28-30	62.3	5.7	229	1.1	25	19	171		48-50	48.9	10.1	235	1.7	32	15	174
44-46	20-22	59.4	5.7	232	1.3	36	23	169	44-46	40-42	60.8	6.5	228	1.4	24	21	171
	22-24	59.6	5.4	231	1.4	32	26	170		42-44	59.6	7.1	232	1.3	04	18	185
	24-26	60.2	5.6	231	0.8	30	14	171		44-46	55.0	7.7	233	1.9	14	25	181
	26-28	60.4	5.5	228	1.0	23	18	171		46-48	49.3	8.5	232	1.8	06	21	184
	28-30	60.8	5.6	231	1.0	29	18	171		48-50	43.1	10.8	231	2.8	28	26	172
46-48	20-22	58.3	5.4	228	1.0	33	19	167	46-48	40-42	56.9	6.0	234	1.4	354	23	192
	22-24	58.4	5.4	229	1.0	26	19	171		42-44	51.1	7.4	235	2.5	02	34	189
	24-26	58.3	5.3	232	1.3	20	25	177		44-46	45.7	8.6	225	2.8	02	33	179
	26-28	58.4	5.3	232	1.2	36	23	169		46-48	42.0	10.0	224	2.8	10	28	174
	28-30	58.3	5.2	232	0.9	39	17	167		48-50	40.4	10.8	226	2.5	12	23	175
48-50	20-22	56.5	4.7	236	1.1	42	23	170	48-50	40-42	54.8	5.0	228	1.2	342	24	192
	22-24	56.3	4.8	235	0.9	43	19	169		42-44	51.2	5.7	221	1.7	342	30	185
	24-26	56.4	5.1	236	0.8	35	16	173		44-46	46.2	7.0	222	1.8	346	26	184
	26-28	56.4	5.1	233	1.0	30	20	173		46-48	43.1	7.5	225	1.6	357	21	181
	28-30	56.2	4.8	233	1.2	21	25	177		48-50	39.9	9.2	230	2.0	17	22	177
Square 148									Square 150								
40-42	30-32	63.7	6.1	227	1.1	15	18	175	40-42	50-52	61.9	9.2	233	1.6	62	17	157
	32-34	64.5	6.0	227	1.1	35	18	165		52-54	63.0	9.3	231	0.9	25	10	173
	34-36	65.1	6.6	230	1.2	22	18	174		54-56	63.8	9.2	225	0.8	78	9	141
	36-38	65.3	6.7	225	1.4	33	21	163		56-58	64.6	8.9	227	0.9	54	10	155
	38-40	65.5	6.3	221	1.6	01	25	175		58-60	63.8	9.3	231	0.7	35	8	169
42-44	30-32	63.0	5.9	230	1.1	22	19	174	42-44	50-52	48.2	11.8	238	2.2	25	19	181
	32-34	63.1	6.2	230	1.3	37	21	167		52-54	52.0	11.8	238	1.1	14	9	186
	34-36	63.5	6.4	228	1.6	38	25	164		54-56	53.3	12.4	235	0.7	67	6	157
	36-38	63.1	6.2	230	0.9	31	14	169		56-58	52.9	12.8	233	1.0	37	8	169
	38-40	63.2	6.1	228	1.2	28	20	169		58-60	51.1	13.3	230	0.9	28	7	171

## APPENDIX—continued

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° W.	° F.	° F.	°	° F.	°		°
Square 150—continued									Square 181 (German data)—continued								
44-46	50-52	44.3	12.4	229	2.4	17	19	175	57-58	0-1	49.2	6.3	233	1.3	66	21	155
	52-54	45.0	12.5	226	2.4	12	19	175		1-2	48.2	6.3	227	0.9	55	14	154
	54-56	45.2	12.6	229	2.4	25	19	171		2-3	49.3	6.5	230	0.9	56	14	157
	56-58	44.6	14.0	228	2.6	28	18	169		3-4	47.9	7.3	234	0.4	40	5	169
	58-60	43.7	14.6	229	3.0	14	21	177									
46-48	50-52	40.5	12.0	228	2.3	03	19	181	58-59	0-1	48.8	5.4	232	1.3	50	24	162
	52-54	40.1	11.9	228	2.1	348	18	189		1-2	48.7	5.5	229	0.9	70	16	149
	54-56	41.7	12.2	229	2.1	19	17	175		2-3	48.5	5.4	229	0.7	30	13	169
	56-58	41.9	12.9	230	1.5	36	12	167		3-4	48.8	5.3	228	0.7	35	13	165
										4-5	49.1	5.1	226	0.8	49	16	156
48-50	50-52	39.0	11.0	230	2.5	23	23	173		5-6	49.6	5.4	227	0.8	58	15	153
	52-54	39.0	11.7	231	2.8	10	24	181		6-7	50.1	5.1	234	0.9	66	18	156
										7-8	50.5	4.5	236	0.9	46	20	168
										8-9	50.6	4.2	241	1.0	38	24	177
										9-10	50.8	4.3	242	0.9	45	23	175
Square 151									59-60	0-1	48.8	5.8	232	1.7	60	30	157
40-42	60-62	61.5	10.3	238	0.9	50	9	168		1-2	48.6	4.9	226	0.9	54	19	154
	62-64	59.2	11.2	242	1.0	14	9	190		2-3	48.8	5.7	230	0.8	47	14	161
	64-66	56.2	11.7	238	1.4	24	12	181		3-4	49.2	4.6	226	0.9	50	20	156
	66-68	52.8	12.1	235	1.3	47	11	167		4-5	49.6	4.4	232	1.0	51	23	161
	68-70	51.5	12.3	232	1.3	49	11	163		5-6	49.9	4.0	223	1.0	35	25	160
42-44	60-62	49.6	14.6	227	1.5	36	10	164		6-7	50.4	4.4	238	1.5	45	34	170
	62-64	48.5	15.0	227	1.7	35	11	165		7-8	50.1	3.7	238	1.2	40	32	174
	64-66	46.3	13.3	230	1.3	46	10	162		8-9	50.3	3.4	237	1.2	30	35	177
	66-68	46.5	11.7	234	1.0	45	9	167		9-10	50.0	3.3	234	1.4	30	42	174
	68-70	49.2	13.2	238	2.4	53	18	167									
44-46	60-62	44.4	14.8	228	2.7	23	18	171	Square 182								
Square 181 (German data)									50-52	10-12	54.4	5.2	240	1.1	61	21	165
50-51	0-1	52.8	7.9	228	0.5	00	6	183		12-14	54.8	4.9	237	1.0	48	20	168
	1-2	52.9	7.6	227	0.4	06	5	179		14-16	54.8	4.6	235	1.0	50	22	165
	2-3	53.2	7.0	226	0.5	12	7	175		16-18	55.0	4.7	237	1.0	42	21	171
	3-4	53.5	6.5	228	0.5	47	8	159		18-20	55.1	4.6	238	1.0	53	22	167
	4-5	53.7	6.4	232	0.8	64	12	155	52-54	10-12	53.9	4.5	238	1.3	42	29	172
	5-6	53.3	6.0	231	0.7	61	12	155		12-14	54.3	4.4	238	1.2	35	27	175
	6-7	53.6	6.6	236	1.4	72	21	155		14-16	54.3	4.4	238	1.2	35	27	175
	7-8	54.1	6.8	237	1.2	39	18	173		16-18	53.8	4.3	237	0.8	44	19	170
	8-9	54.4	6.8	237	1.3	59	20	162		18-20	53.7	4.1	233	0.5	53	12	161
	9-10	54.6	6.3	238	0.8	62	13	162	54-56	10-12	52.6	4.4	240	0.9	71	20	159
51-52	3-4	52.5	8.3	232	0.7	30	8	172		12-14	52.8	4.1	240	1.0	41	24	175
	4-5	52.7	7.4	231	0.8	07	11	182		14-16	52.9	4.0	240	0.8	34	20	178
	5-6	53.0	6.6	231	0.8	93	12	140		16-18	52.9	3.9	239	0.8	34	21	177
	6-7	53.1	6.0	233	1.1	78	19	149		18-20	52.9	3.9	238	1.0	38	26	174
	7-8	53.2	6.4	234	1.3	38	21	170	56-58	10-12	52.0	4.1	227	0.9	37	22	163
	8-9	53.1	6.3	237	0.6	61	10	161		12-14	52.3	4.5	237	1.3	65	29	159
52-53	5-6	51.8	6.2	215	0.4	22	7	159		14-16	51.6	4.1	239	0.9	47	22	171
	6-7	52.2	6.1	223	0.5	325	8	195		16-18	51.4	3.9	241	0.8	33	21	179
53-54	5-6	51.3	6.5	220	0.6	60	9	145		18-20	51.4	3.9	240	0.8	15	21	187
54-55	0-1	48.9	7.6	234	0.9	75	12	151	58-60	10-12	51.1	3.8	242	1.1	47	29	173
	1-2	49.0	7.0	236	1.3	270	18	148		12-14	50.6	4.1	242	1.0	55	24	169
	5-6	50.5	5.8	216	0.2	51	3	146		14-16	50.3	4.0	244	1.1	52	28	173
55-56	0-1	49.5	7.6	234	1.6	62	21	158		16-18	50.3	3.8	243	1.0	48	26	174
	1-2	48.9	7.4	225	1.3	75	18	143		18-20	50.3	3.7	242	1.0	47	27	173
56-57	0-1	49.2	6.9	231	1.6	66	23	153	Square 183								
	1-2	48.5	6.6	230	1.0	75	15	148	50-52	20-22	55.0	4.4	236	1.0	50	23	166
	2-3	48.4	7.1	233	0.8	87	11	145		22-24	54.9	4.4	230	1.0	41	23	165
										24-26	54.5	4.6	239	0.9	46	20	171
										26-28	54.4	4.5	233	0.8	31	18	173
										28-30	54.0	4.4	233	0.7	34	16	171

APPENDIX I—*continued*

Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$	Position		$a_0$	$a_1$	$A_1$	$a_2$	$A_2$	$\frac{100a_2}{a_1}$	$F$
° N.	° W.	° F.	° F.	°	° F.	°		°	° N.	° E.	° F.	° F.	°	° F.	°		°
Square 183— <i>continued</i>									Square 216 (German data)— <i>continued</i>								
52-54	20-22	53.1	4.2	237	0.3	15	7	185	54-55	1-2	49.5	8.6	235	0.9	73	10	153
	22-24	52.9	4.0	238	0.3	03	7	191		2-3	49.8	9.5	236	0.9	73	10	154
	24-26	52.5	3.7	236	0.4	43	11	169		3-4	49.9	9.8	234	1.0	82	10	148
	26-28	52.1	4.2	235	0.2	38	5	171		4-5	50.3	10.0	231	1.0	86	10	143
	28-30	51.0	4.3	237	0.5	356	12	194		5-6	50.5	10.3	232	0.7	78	7	148
54-56	20-22	52.9	4.0	235	0.8	31	20	175		6-7	50.4	11.2	235	0.9	82	8	149
	22-24	52.6	4.3	235	0.7	43	16	169		7-8	49.8	12.0	237	0.6	98	5	143
	24-26	51.9	4.4	235	0.5	30	11	175		8-9	49.4	12.8	242	0.7	85	6	154
	26-28	51.2	4.8	238	0.3	36	6	175	55-56	0-1	49.7	8.1	231	1.7	70	21	151
	28-30	49.7	5.1	239	0.1	112	2	138		1-2	49.6	8.0	235	1.5	55	19	162
56-58	20-22	51.4	4.0	239	0.6	60	15	164		2-3	49.6	8.6	235	1.6	50	19	165
	22-24	51.5	3.7	237	0.6	30	16	177		3-4	49.6	9.2	235	1.1	70	12	155
	24-26	50.6	4.2	238	0.7	55	17	165		4-5	49.9	9.6	235	1.3	70	13	155
Square 184										5-6	50.1	9.9	234	1.3	95	13	142
50-52	30-32	53.0	4.2	235	0.3	17	7	181		6-7	49.9	10.3	232	0.9	85	9	145
	32-34	53.0	4.3	238	0.2	350	5	198		7-8	49.8	11.2	237	0.8	85	7	150
	34-36	52.6	4.5	239	0.4	337	9	205	56-57	0-1	49.6	7.2	232	1.8	63	25	155
	36-38	52.0	4.7	237	0.4	354	9	195		1-2	49.5	7.4	235	1.8	58	24	161
	38-40	51.8	4.2	235	0.7	326	17	207		2-3	49.3	8.0	235	1.7	56	21	162
52-54	30-32	50.2	4.4	242	0.6	13	14	191		3-4	49.2	8.4	235	1.5	53	18	163
	32-34	48.6	4.7	239	0.6	11	13	189		5-6	49.3	9.4	234	1.5	65	17	156
	34-36	48.6	4.7	239	0.6	11	13	189		6-7	49.7	9.8	238	1.3	95	13	146
	36-38	48.1	4.3	250	0.4	58	9	176		7-8	49.3	10.4	238	1.3	105	13	140
	38-40	47.5	5.7	242	0.4	98	7	148		8-9	48.7	11.2	241	1.2	81	11	156
Square 185									57-58	1-2	49.7	7.0	230	1.9	44	24	163
50-52	40-42	52.0	4.9	231	0.9	332	18	200		2-3	49.4	7.5	234	2.0	50	26	164
	42-44	51.9	5.4	228	0.8	352	15	187		3-4	48.8	7.9	235	2.0	50	25	165
Square 216 (German data)										4-5	48.5	8.5	237	1.8	58	21	163
50-51	0-1	52.4	8.4	232	0.7	8	8	183		5-6	49.0	8.7	236	1.9	64	22	159
	1-2	52.2	8.7	233	0.5	11	6	182		6-7	49.0	9.3	238	1.8	70	20	158
51-52	1-2	52.1	8.8	233	0.5	0	6	185		7-8	49.3	9.0	239	2.3	61	26	163
	2-3	52.1	9.0	233	0.6	357	7	189		8-9	49.0	10.3	240	1.8	98	18	146
	3-4	51.5	10.4	239	0.4	09	4	189		9-10	48.8	10.8	244	1.6	86	15	156
52-53	1-2	50.5	9.8	235	0.8	14	8	183	58-59	0-1	49.3	6.6	233	1.5	45	23	165
	2-3	51.5	9.4	230	0.9	19	10	176		1-2	49.0	6.4	234	1.6	59	25	160
	3-4	51.5	9.7	234	0.6	10	6	184		2-3	49.3	6.8	235	1.8	63	26	159
	4-5	50.5	11.5	235	0.9	117	7	..		3-4	49.1	7.6	238	1.7	56	22	165
53-54	0-1	49.0	8.2	233	0.4	03	5	182		4-5	48.6	8.6	236	1.8	72	21	155
	1-2	49.4	9.3	233	0.3	60	3	158		5-6	48.5	9.6	238	1.6	71	16	157
	2-3	50.0	9.3	233	0.3	60	3	158		6-7	48.5	10.4	239	1.6	71	16	158
	3-4	50.8	9.7	232	0.5	42	5	166	59-60	0-1	48.9	6.0	235	1.8	59	30	160
	5-6	50.7	10.8	239	0.5	46	5	171		1-2	48.8	6.3	235	1.8	45	29	167
	6-7	50.2	11.5	240	0.6	46	5	172		2-3	49.0	6.7	240	1.4	55	21	167
	7-8	49.8	12.0	240	0.5	47	4	172		3-4	49.1	7.4	233	2.1	50	28	163
										4-5	48.8	8.6	238	1.8	70	21	158